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#### Abstract

About the Author 

Virendra N. Mahajan was born in Vihari, Pakistan, and educated in India and the United States. He received his Ph.D. degree in Optical Sciences from the Optical Sciences Center, University of Arizona, in 1974. He spent nine years at the Charles Stark Draper Laboratory in Cambridge, Massachusetts, where he started and headed an optics group. Since 1983, he has been at The Aerospace Corporation in El Segundo, California, where he works on space defense programs. He is also an adjunct professor at the University of Southern California in the electrical engineering-electrophysics department, where he teaches an advanced course in geometrical and physical optics. He was a visiting professor at the Indian Institute of Technology, New Delhi, under a grant from the United Nations Development Program during spring 1990. He has taught short courses on aberration theory at the National Central University, Chung Li, Taiwan, and at the annual meetings of the Optical Society of America and SPIE. He has published numerous papers on diffraction, aberration theory, adaptive optics, and acousto-optics. He is a member of the Optical Society of America and past chairman of its Astronomical, Aeronautical, and Space Optics technical group. He is also a member of the SPIE and a past member of its Education Committee.


