Analysis of hollow-core photonic bandgap fibers for evanescent wave biosensing

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Abstract. Hollow-core photonic bandgap fiber (HC-PBGF)-based evanescent wave biosensor is demonstrated and analyzed theoretically and experimentally. With 95% of the guided light power residing in the samples, the measured absorbance for a 30-cm-long fiber filled with a 0.2 μM Alexa Fluor 700–labeled DNA Oligo solution is 1.06. This is in good agreement with the theoretical prediction, which is evaluated by using the refractive index scaling law. The HC-PBGFs thus offer both efficiency and simplicity for the detection of biomolecules in ultra-small sample volumes. © 2008 Society of Photo-Optical Instrumentation Engineers.

Keywords: photonic crystal fibers (PCFs); photonic bandgap fibers (PBGFs); evanescent wave; biosensor.

Paper 07504RR received Jan. 1, 2008; revised manuscript received Jul. 7, 2008; accepted for publication Jul. 9, 2008; published online Oct. 3, 2008.

1 Introduction

Over the last two decades, optical fibers and waveguides have been widely used for developing optical biosensors.1 Evanescent wave biosensors are based on interaction of the analyte species with the electromagnetic wave, which extends from the surface of the light-guiding waveguides. The interaction between evanescent wave and analytes produces absorption, the surface of the light-guiding waveguides. The efficiency of this kind of biosensor is determined by sufficient interaction length and large overlap between excitation light and fluorescent dye–labeled analytes.2 Approaches used to realize large overlap between excitation light and fluorescent dye–labeled analytes. Moreover, since the excitation light and the emitted fluorescent light are both confined to the core, their overlap is maximized.

In this paper, the performance of the HC-PBGF for evanescent wave biosensing is analyzed. The principles of operation and performance analysis are described in Sec. 2. Experimental results and discussion are presented in Sec. 3, and a conclusion is given in Sec. 4.

2 Theory and Simulation Results

The structure of the HC-PBGF used in the experiment is illustrated in Fig. 1 and is designed to guide light in the wavelength range from 1400 nm to 1800 nm. Following the designations, the photonic crystal (PC) cladding can be characterized by four parameters: hole-to-hole distance λ, hole diameter d, and refractive indices nα in the holey regions and nβ in the silica regions. The diameter of the hollow core is D.

According to the Beer-Lambert law, a crucial factor determining the amount being absorbed is the absorbance A(λ), which is defined as

\[ A(\lambda) = \log_{10} \left( \frac{I_0(\lambda)}{I(\lambda)} \right) = \varepsilon(\lambda)cL_{eff}. \tag{1} \]

where \( I_0(\lambda) \) and \( I(\lambda) \) are the intensities before and after the sample, respectively. \( \lambda \) is the wavelength of light, and \( \varepsilon(\lambda) \) is called the molar extinction coefficient at wavelength \( \lambda \). \( c \) is the concentration of the sample. \( L_{eff} \) is the effective optical path defined by the length of the sample through which the light travels, supposing 100% overlap between light and sample. The transmission T can be written simply as

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054048-1

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September/October 2008
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\[ T(\lambda) = 10 \log_{10} \left[ \frac{I_0(\lambda)}{I(\lambda)} \right] = 10A(\lambda). \]  

(2)

For evanescent wave biosensors, only part of the guided light interacts with the sample. Therefore, the effective optical path length, which is determined by the fiber length \( l \) and the sensitivity coefficient \( r \), is given by\(^2\)

\[ L_{\text{eff}} = rl. \]  

(3)

The sensitivity coefficient \( r \) is an important parameter in quantifying the fiber efficiency, which is used to describe the overlap between the light and the sample. The fiber efficiency is a measure of the effective interaction length \( L_{\text{eff}} \) of a given optical fiber with length \( l \). It has a value of \( r = (n_r/n_{\text{eff}})f \), where \( n_r \) is the refractive index of the sensed material, \( n_{\text{eff}} \) is the modal effective index, and \( f \) is the percentage of optical power in the holes. This corresponds to introducing effective interaction length \( L_{\text{eff}} \), which is the section of fiber where the light and the sample have 100% overlap. The percentage of optical power in the holes \( f \) is described as\(^1\)

\[ f = \frac{\int_{\text{sample}} \text{Re}(E_xH_y^* - E_yH_x^*) \, dx \, dy}{\int_{\text{total}} \text{Re}(E_xH_y^* - E_yH_x^*) \, dx \, dy}, \]  

(4)

where \( E_{x/y} \) and \( H_{x/y} \) are the electric and magnetic fields along the \( x \) and \( y \) directions.

The performance of the evanescent wave sensor is mainly determined by the modal effective index as well as the percentage of energy in the holes. Tedium numerical simulation is crucial to evaluate these two parameters in the conventional fiber design. This can be avoided for the HC-PBGFs by using refractive index scaling laws.\(^6\) The wave equation for the scalar field distribution in a HC-PBGF can be described in terms of normalized transverse coordinates \( X = x/\Lambda \) and \( Y = y/\Lambda \) and an index distribution function.\(^8\)

\[ g(X, Y) = \begin{cases} 
0 & \text{low index regions} \\
1 & \text{high index regions} 
\end{cases}. \]  

(5)

The resulting normalized scalar wave equation is

\[ \frac{\partial^2 \Phi}{\partial X^2} + \frac{\partial^2 \Phi}{\partial Y^2} + \left[ u^2 g(X, Y) - w^2 \right] \Phi = 0, \]  

(6)

where \( u^2 = \left[ 2\pi(\Lambda/\lambda)^2(n^2_r - n^2) \right], \) and \( w^2 = \left[ 2\pi(\Lambda/\lambda)^2(n^2_{\text{eff}} - n^2) \right]. \)

The frequency parameter \( u^2 \) and eigenvalue \( w^2 \) are directly analogous to the parameters \( V^2 \) and \( W^2 \) of the conventional waveguide theory,\(^9\) with an exception that \( \Lambda \) defines a transverse scale in a structure. The refractive index scaling law can be described as follows: If \( n_r \) is varied, the scalar field distribution can be kept unchanged, supposing that the normalized wavelength \( \lambda/\Lambda \) is adjusted so as to keep the values of \( u \) and \( w \) invariant.\(^6,9\) In particular, the locations of the transmission windows, after the HC-PBGF is filled with aqueous solution, can be estimated by considering the invariant \( v \). Assuming that the bandgap is originally at a wavelength \( \lambda_0 \) for an air-guiding HC-PBGF with \( n_r = 1 \), after the fiber is filled with aqueous solution with \( n_r = n_a \) it shifts to a new wavelength \( \lambda \). The relationship between the wavelengths \( \lambda_0 \) and \( \lambda \) is governed by\(^9\)

\[ \lambda = \lambda_0 \left( \frac{n^2_a - n^2_r}{n^2_r - 1} \right)^{1/2}. \]  

(7)

As the values of \( v \) and \( w \) are invariant, their ratio \( v^2/w^2 \) is also invariant. The modal effective index \( n_{\text{eff}}(\lambda) \) at the wavelength \( \lambda \) after filling can thus be evaluated by the modal effective index \( n_{\text{eff}}(\lambda_0) \) at the wavelength \( \lambda_0 \) before filling, which is given by

\[ \frac{v^2}{w^2} = \frac{n^2_r - 1}{n_{\text{eff}}^2(\lambda_0) - 1} = \frac{n^2_r - n^2_{\text{eff}}(\lambda)}{n^2_r - n^2}, \]  

(8)

\[ n_{\text{eff}}(\lambda) = \frac{n^2_r - [1 - n^2_{\text{eff}}(\lambda_0)] \left( \frac{n^2_r - n^2}{n^2_r - n^2_{\text{eff}}(\lambda_0)} \right)^{1/2}}. \]  

(9)

Since the scalar wave distribution \( E_{x/y} \) and \( H_{x/y} \) are invariant when the bandgaps shift from a wavelength \( \lambda_0 \) to a wavelength \( \lambda \), the percentage of energy in Eq. (4) is also invariant, or

\[ f(\lambda) = f(\lambda_0). \]  

(10)

These equations provide simple tools for estimating the efficiency of HC-PBGF–based biosensors by utilizing the parameters list in the product manual.

In order to demonstrate this idea, Figs. 2(a) and 2(b) show the electric field distribution at \( \lambda_0 = 1.55 \mu m \) before filling with water and \( \lambda = 0.853 \mu m \) after filling with water. A full vectorial beam propagation method was used to evaluate the electric fields with the parameters of \( \Lambda = 3.8 \mu m, n_r = 1.45, n_r = 1 \). Before and after filling with water. As these two wavelengths satisfy the refractive index scaling law, their corresponding electric fields show no difference. The corresponding fractions of light propagating in the air holes or samples are both around 96%. The corresponding modal refractive indices \( n_{\text{eff}} \) are 0.9881 and 1.3267 when \( n_r = 1 \) and \( n_r = 1.33 \), respectively, which also agrees well with the refractive index scaling law described in Eq. (9). The simple meth-
ods for estimating the value of $f$ and $n_{eff}$ greatly facilitate the
design procedure of HC-PBGF–based evanescent wave bio-
sensors.

3 Experimental Results

The schematic diagram of the experimental setup is shown in
Fig. 3. A 30-cm-long HC-PBGF (Crystal-Fiber HC-1550-02) was used in the experiment and had a cladding pitch of 3.8 μm, a core diameter of 10.9 μm, and a center operating
wavelength of 1550 nm. Two ends of the HC-PBGF were mounted in modified V-groove mounts. Light from a super-
continuum (SC) source (KOHERAS SuperK Red) was guided using a single-mode fiber SMF-28, which in turn launched into the core of the PBGF via butt-coupling by using two pairs of three-dimensional (3-D) stages (Newport 561/562 series). The alignment was achieved by tuning the high-
resolution micrometers. When the maximum transmitted optical signal was obtained, the alignment was ready. The transmitted light after the HC-PBGF was guided by using another section of SMF-28 via butt-coupling again and then measured by using an optical spectrum analyzer (OSA; Yokogawa AQ6370), which can measure the spectrum from 600 nm to 1700 nm. The holey region of the HC-PBGF was filled up with the Alexa Fluor 700–labeled DNA Oligo solu-
tion (Invitrogen) by capillary force. Alexa Fluor 700 has an absorption maximum at 696 nm with a molar extinction co-
efficient of 192,000 M$^{-1}$ cm$^{-1}$.

Figure 4 shows the transmission spectra before and after filling with pure water. The transmission spectrum before the filling process spanned a range of 1400 nm to 1700 nm. Af-
ter filling, the transmission spectrum ranged from 600 nm to 1162 nm. This range was broader than the prediction of the scaling law, which had a range from 790 nm to 1020 nm. This is because the refractive index scaling law is derived from scalar wave equations, which neglect the vectorial effects. Therefore, this refractive index scaling law shows a good accordance to the experimental results, especially in the small index contrast region. Deviations are found in the large index contrast region, where vectorial effects start to appear. However, this does not preclude the validity of the refractive index scaling law in evaluating the performance of the HC-PBGF, which was verified both in the theory and experiment. Another issue is that the modal effective index $n_{eff}$ and fraction of power residing in the holes $f$ are related to the operating wavelength. However, as they show small variations across the wavelength ranges of the transmission windows, $n_{eff}$ and $f$ are assumed to be invariant across the wavelength ranges of the transmission windows. The invariances of $n_{eff}$ and $f$ make the analysis easy.
Figure 5 shows the transmission spectra of two 30-cm HC-PBGFs, one filled completely with a 0.2 μM Alexa Fluor 700—labeled DNA Oligo solution and one with pure water. The inset shows the derived absorbance with a maximum value of 1.06 at λ = 696 nm. This could be evaluated by using Eq. (2) and the refractive index scaling law. Since only a fraction of light propagates in the sample, the effective optical path length \( L_{\text{eff}} \) is introduced to describe the absorbance \( A(v) \). As \( L_{\text{eff}} = (n_r / n_{\text{eff}}) f l \), the fraction of power \( f \) and the modal effective index \( n_{\text{eff}} \) should be known to obtain the value of \( L_{\text{eff}} \). However, as described earlier, the refractive index scaling law provides a simple tool to evaluate these two parameters. The HC-PBGF used in the experiment has an effective mode index around 0.99, and the fraction of light propagating in air is around 95% at 1550 nm. Assuming that these two parameters are invariant across the wavelength ranges of the transmission windows, after the fiber is filled with aqueous solution with \( n_r = 1.33 \), the effective mode index is 1.3277, and the fraction of light propagating in the sample is 95%. As a result, the effective optical path length \( L_{\text{eff}} \) for a 30-cm HC-PBGF is 28.6 cm. Considering the molar extinction coefficient of 192,000 M\(^{-1}\) cm\(^{-1}\) at 696 nm and the concentration of 0.2 μM, the expected absorbance is 1.098, which is in good accordance with the measured value.

Alexa Fluor 700—labeled DNA Oligo solutions that have concentrations of 0.1 μM and 0.05 μM were also used to evaluate the sensitivity of the HC-PBGF. The corresponding derived absorbances are illustrated in Fig. 6 and are in good agreement with the analytical results. The minimum detectable concentration is mainly limited by the minimum detectable absorbance. It has been demonstrated that the minimum detectable absorbance can be achieved to be \( A = 0.04 \). Therefore, for an HC-PBGF with a length of 30 cm, this offers the possibility of detecting Alexa Fluor 700—labeled DNA Oligo solution with concentration down to 7 nM, provided that the reference spectra are accurate and stable. With a small sample volume consumption of only 1 μL, this offers the potential for the design of high-sensitivity evanescent wave biosensors.

4 Discussion

The general theory for the HC-PBGF waveguides assumes a nonabsorbing material in the hollow-core region. This means that the dielectric constant \( \varepsilon(r) \) is treated as purely real. Strong water absorption bands occur at wavelengths around 2500, 1950 and 1450 nm, with weaker absorption bands at wavelengths around 1200 and 970 nm and three additional sets of water absorption lines near 930, 820, and 730 nm. All are located in the infrared spectrum. The existence of absorbing material, such as water, within the hollow core would be expected to modify the scaling laws as well as the effective mode index and the fraction of optical power. In order to illustrate the bandgap formation in the presence of the imaginary part of the refractive index, a beam propagation method (BPM) was carried out to model the complex waveguide by taking into account the real and imaginary parts of the refractive index of the water. Figure 7 shows the evaluated transmission spectra for the water-silica HC-PBGF. This was done by launching a Gaussian beam in the center of the core with width equal to that of the core and propagation length 1 cm. Both scalar BPM and vector BPM were carried out in order to illustrate the vectorial effect on the bandgap formation. Comparison of the scalar and vector plots demonstrates...
the basic validity of the scaling laws. The deviation of vector band structure from the scalar case indicates features that arise specifically from the vector nature of the electromagnetic field. In particular, the scalar plot is relatively broader than the vector case, which is due to the overlapping of the bandgaps of two polarization components. This difference also explains the observation of the wavelength deviation reported by Ref. 5. In order to investigate whether the absorption of water modifies the bandgap, a vector BPM was performed by taking into account the imaginary parts of the refractive index of water. The data set of imaginary parts was obtained from Ref. 11. It is found that the transmission spectra, before and after considering the absorption of water, show little difference. There is only a slight fall of optical power around 1200 nm after considering the absorption. Therefore, it is the vectorial effect that causes the wavelength deviation observed in Ref. 5 rather than the absorption of water. The general theory for nonabsorbing material has been applied for several low-loss dielectric waveguide structures, such as the microstructured polymer fibers, liquid-crystal photonic crystal fibers, and solid-core index-guiding PCF-based evanescent wave sensor, which has an evanescent field within the holes of 3.3% (Ref. 23). The demonstrated HC-PBGFs have the advantage of large overlap between the light and the sample residing in the holey areas, which is 28 times larger. This provides high efficiency for the evanescent wave biosensing applications. Fini has proposed a water-core PCF structure for biosensing applications, which is based on an index-guiding mechanism. Although it was possible to achieve 90% overlap between the light and the samples, this method required a selective filling technique, which is a method to fill only some holes of the fiber, such as the central hollow core, rather than the entire holey region. In addition, the analysis and design procedure needed tedious numerical work. A similar method was also proposed by selective filling the hollow core with sample solution, but the guiding mechanism was based on the bandgap guiding. This method evidently experienced the same problems, including the selective filling process and the tedious numerical work. Another type of hollow-core PCF-based evanescent sensor was demonstrated by filling the entire holey region with samples. Although the fiber structures and filling technique seem similar, the guiding mechanisms were totally different. In Ref. 10, light was guided through the silica in the entire cladding rather than the hollow core. In other words, light was not guided by bandgap effects. Therefore, only a 5.2% fraction of optical power resided in the samples. This value was much smaller than the HC-PBGFs used in this experiment, which had an overlap of 95%. In addition, as the light dissipated in the cladding, the loss was significantly large, which also introduced the difficulty into the spectral measurement.

The PBGF-based sensor has so far been tested in applications only as a nonspecific biosensor, which shows its potential to measure the concentration of a specific analyte solution. The use of the PBGF sensor to distinguish different solutions appears possible, assuming that a biorecognition element is immobilized on the inner surface of the holey region of the fiber by physical or chemical methods. One of the surface-binding PCF-based sensors uses streptavidin molecules (antigen) as a biorecognition element to detect a specific biomolecule, α-streptavidin (antibody). This concept may be used for a variety of biodetection, such as various enzymes and antibodies.

Another important practical consideration is the potential for the reuse of the HC-PBGF for multiple tests during semi-continuous on-line monitoring. For the demonstrated nonspecific sensing system, the HC-PBGF can be cleaned with acetone and isopropanol. The filling and cleaning processes can be achieved with the aid of a pressure chamber. A HC-PBGF-based sensor can be developed for detecting specific targets, for example, by depositing a sensor layer of complementary biomolecules immobilized inside the air holes of the HC-PBGFs. Regeneration of the HC-PBGF sensor for antibody-antigen detection is also possible, since many techniques have been demonstrated to dissociate antibody-antigen

**Table 1 Effective mode indices and fractions of optical power at different wavelengths.**

<table>
<thead>
<tr>
<th>Wavelength</th>
<th>Effective mode index ($n_{eff}$)</th>
<th>Fraction of optical power ($f$)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>No absorption</td>
<td>Absorption</td>
</tr>
<tr>
<td>600 nm</td>
<td>1.3279</td>
<td>1.3274</td>
</tr>
<tr>
<td>800 nm</td>
<td>1.3113</td>
<td>1.3110</td>
</tr>
<tr>
<td>1180 nm</td>
<td>1.2985</td>
<td>1.2968</td>
</tr>
</tbody>
</table>
complexes, including pressure, electrical field, and solvents. The regeneration methods can thus follow those techniques that are commonly used in conventional fiber-optic biosensors.

5 Conclusion
In conclusion, the HC-PBGFs–based evanescent wave sensing technique has been analyzed both theoretically and experimentally. According to the refractive index scaling law, the modal effective index and fraction of optical power residing in the sample after filling process could be derived from the parameters before the filling process. This offers a simple method for both design and analysis procedures. In this type of sensor, light is confined to the central core, with more than 95% of light residing in the samples, which is verified by both theoretical and experimental results. With a small sample consumption of only 1 μL, the measured absorbance for a 30-cm-long fiber filled with a 0.2 μM Alexa Fluor 700–labeled DNA Oligo solution is 1.06. Due to a large part of the evanescent wave residing in the sample, only a short section of HC-PBGF, 30 cm long, is required to obtain high sensitivity. This greatly enhances the detection efficiency. In addition, this method does not require a selective filling technique, which further offers convenience for practical applications.

References