Selection of optimal wavelengths for spectral reconstruction in diffuse optical tomography

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Abstract. Using lasers with different wavelengths in diffuse optical tomography (spectral DOT) has the advantage that the concentrations of chromophores can be reconstructed quantitatively. In continuous wave spectral DOT, it is furthermore possible to distinguish between scattering and absorption. The choice of the laser wavelengths has a strong impact on how well the scattering parameter and chromophore concentrations can be determined. Current methods to optimize the set of wavelengths disregard the sensitivity of the reconstruction result to uncertainties in the absorption spectra of the chromophores. But since available absorption spectra show significant deviations, it seems to be necessary to take this into account. The wavelength optimization approach presented here is an extension to a method of Corlu et al. The original method optimizes the wavelength sets such that scattering parameters and chromophore concentrations can be separated optimally. We introduce an additional criterion that evaluates the dependence of reconstructed chromophore concentrations on deviations of the extinction coefficients. The wavelength sets found by the new approach are different from those determined with the original method. Reconstructions of simulated data show the effect of using various absorption spectra for reconstruction with different wavelength sets and illustrate the advantages of the new wavelength sets.

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Keywords: diffuse optical tomography (DOT); continuous wave diffuse optical tomography (CW DOT); spectral reconstruction.

Paper 08438R received Dec. 12, 2008; revised manuscript received Mar. 26, 2009; accepted for publication Apr. 30, 2009; published online Jun. 23, 2009. This paper is a revision of a paper presented at the SPIE conference on Diffuse Optical Imaging of Tissue, June 2007, Munich, Germany. The paper presented there appears (unrefered) in SPIE Vol. 6629.

1 Introduction

Diffuse optical tomography (DOT) can be used to image the optical properties of human tissue up to depths of several centimeters. Main clinical applications that are currently explored are breast imaging, functional brain imaging, and imaging of the neonatal brain.1

In typical DOT systems for breast imaging, near-infrared (NIR) laser light is radiated into the tissue successively from different source positions. The light propagates through the tissue and is affected by scattering and absorption. The intensity of the light emanating from the tissue is measured at a number of detector positions for each source position. From these measurements, three-dimensional (3-D) absorption and/or scattering images of the tissue can be reconstructed.

The systems mainly differ in the geometry of source and detector positions, and in the light that is emitted into the tissue. While the geometry primarily affects the field of view and the local resolution and sensitivity in the images, the choice of the light sources has a major impact on what can be reconstructed from the measurements. There are two main aspects regarding the light sources.

The first aspect is the variation of light intensity over time. Three schemes are common: short pulses (\( \leq 1 \) ns),2-4 modulated amplitude,5,6 and continuous wave.7-10 For a short light pulse, a time response of the light intensity can be measured at each detector position [time domain (TD) measurement]. For amplitude modulated light, amplitude and phase of the light intensity can be measured [frequency domain (FD) measurement]. For continuous wave light, only the steady-state amplitude of the light intensity can be measured [continuous wave (CW) measurement]. The different amount of information that is acquired for these three illumination schemes influences the reconstruction. While it is possible to separate scattering and absorption in reconstructions based on TD and FD measurements, this is not possible for CW measurements without a priori knowledge.11

The second aspect is the wavelength of the light. Most DOT systems successively use light with different wavelengths for the measurements (spectral measurement). How many and which wavelengths are used differs from system to system. Spectral measurements are useful, since absorption

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1083-3668/2009/14(3)/034041/10/$25.00 © 2009 SPIE
and scattering in tissue are wavelength dependent.

The wavelength dependency of absorption is dominated by a few chromophores that mainly cause absorption in tissue (for breast: oxyhemoglobin, deoxyhemoglobin, water, and lipid). The chromophores have distinct wavelength dependencies in the relevant NIR band (see the following). Using these dependencies, the spatial distribution of the chromophore concentrations can be derived from the reconstructed absorption images for the different wavelengths, if the wavelengths are chosen properly, i.e., quantitative values of physiological parameters of the tissue can be imaged, allowing us to determine physiological parameters such as blood volume and oxygenation.

The wavelength dependency of the scattering is influenced by the effective size, the number density, and the index of refraction change of the scattering particles in tissue. It can be described in good approximation by a Mie scattering model: $\mu_s' = a \cdot (\lambda / \lambda_0)^b$. The spatial distribution of the model parameters can be calculated based on the reconstructed scattering images for the different wavelengths.

Alternatively, using absorption spectra of the chromophores and a spectral model for the scattering, chromophore concentrations and scattering model parameters can be reconstructed directly from the spectral measurements (spectral reconstruction). This spectral reconstruction leads to improved results, because the spectral dependency of absorption and scattering is used as a priori knowledge.

Furthermore, spectral reconstruction works also for CW measurements. Prerequisites for a good estimation of chromophore concentrations and scattering parameters with spectral CW DOT systems are that the laser wavelengths are chosen properly and that the impact of deviations of a priori knowledge from reality is negligible.

Corlu et al. describe a spectral reconstruction algorithm for spectral CW DOT systems. Moreover, they suggest an approach to determine an optimal set of wavelengths, by considering the separability of absorption and scattering and the separability of the chromophores. Thus, the method of Corlu et al. meets one of the prerequisites stated earlier, and is consequently adequate, if the spectral models for scattering and chromophores are exactly known. If this is not the case, the uncertainties of the spectral models should be taken into account for the optimization of the wavelengths, to minimize reconstruction errors. This seems to be necessary especially for the chromophores, since the reported absorption spectra show significant differences (see the following).

In this paper, an extension to the method given by Corlu et al. is presented, which considers uncertainties in the chromophore absorption spectra. In Sec. 2, the basics of image reconstruction for optical tomography are introduced, and the incorporation of spectral models for scattering and absorption is explained. In Sec. 3, the method of Corlu et al. for wavelength optimization and our extension are described. In Sec. 4, simulations are shown, which are done to analyze the effect of different wavelengths sets on reconstructed images. In Sec. 5, examples for wavelength sets determined with the new method are presented, and the effect of the choice of the wavelengths on the reconstruction is illustrated. In the last section, a conclusion is given.

## 2 Spectral Reconstruction

The propagation of NIR light in breast tissue is dominated by scattering. Thus, light propagation can be described by the diffusion equation, here given for the CW case:

$$- \nabla \cdot D \nabla \Phi + \mu_s \Phi = \frac{1}{\mu_s} T,$$

where $\Phi$ is the photon density, $D = 1 / (3 \mu_s)$ is the diffusion coefficient with $\mu_s'$ being the reduced scattering coefficient, $\mu_s$ is the absorption coefficient, and $v$ is the speed of light in the turbid medium. $T$ models the light source. Note that photon density, absorption, and diffusion coefficient, as well as the light source function, are spatially varying functions, which additionally depend on the wavelength of the light.

Furthermore, a boundary condition is necessary to describe the behavior of light at the boundaries of the imaging region. Commonly, a Robin-type boundary condition is applied:

$$\phi + \frac{D}{\alpha} \frac{d \phi}{dn} = 0,$$

where $n$ is the normal vector of the boundary surface, and $\alpha$ is related to the mismatch of the refractive indices at the boundary.

To come to a description that does not depend on absorption and diffusion coefficients, but on chromophore concentrations and parameters of the scattering model, the relationship between absorption coefficient and chromophore concentrations has to be known, as well as the relationship between reduced scattering coefficient and scattering model parameters.

The relationship for the absorption coefficient is given by Beer’s law:

$$\mu_a(\lambda) = \sum_{k=1}^{K} c_k \cdot \varepsilon_k(\lambda),$$

where $\varepsilon_k$ is the molar absorption coefficient (derived from the absorption spectrum), and $c_k$ is the concentration of the $k$'th of $K$ chromophores.

For the scattering coefficient, the relationship is given by a simplified Mie scattering model:

$$\mu_s'(\lambda) = a \cdot \left( \frac{\lambda}{\lambda_0} \right)^{-b}.$$
reconstruct both scattering parameters. For this reason, the scattering power \( b \) will be set to a constant value in the following reconstructions, i.e., the scattering amplitude \( a \) is the only scattering parameter that will be reconstructed.

3 Wavelength Optimization

In addition to the reconstruction method, Corlu et al. presented an algorithm to optimize the wavelengths of a spectral CW DOT system to optimally determine all parameters estimated by the reconstruction. The algorithm is based on two criteria, which are shortly described in the following.

As stated earlier, CW DOT cannot distinguish scattering and absorption without \textit{a priori} knowledge, because of the nonuniqueness of the solution of Eqs. (1) and (2). Using spectral CW DOT and a spectral model for absorption and scattering, uniqueness is recovered, if the wavelengths are chosen properly. Thus, the first criterion evaluates whether the usage of a certain set of wavelengths leads to a unique solution for the chromophore concentrations and scattering parameters. The derivation is based on the nonuniqueness proof for CW measurements,\(^{1,18}\) and leads to the expression

\[
E = M^{-1}T \cdot L,
\]

\[
r = \|1 - M(M^T M)^{-1} M^T \cdot 1\|,
\]

\[
M = \begin{pmatrix}
\frac{\varepsilon_1(\lambda_i)}{\lambda_i^6} & \cdots & \frac{\varepsilon_k(\lambda_i)}{\lambda_i^6} \\
\vdots & \ddots & \vdots \\
\frac{\varepsilon_1(\lambda_L)}{\lambda_L^6} & \cdots & \frac{\varepsilon_k(\lambda_L)}{\lambda_L^6}
\end{pmatrix},
\]

\( \lambda_i \) are the wavelengths of the laser light used in the CW DOT system \((i = 1, \ldots, L)\). The closer the residual norm \( r \) is to zero, the closer the inverse problem is to nonuniqueness, i.e., the residual \( r \) should be large for a proper set of wavelengths. Note that this automatically implies that the number of wavelengths \( L \) has to be larger than the number of chromophores \( K \) to achieve uniqueness of the inverse problem.

The second criterion evaluates how well the chromophore concentrations can be distinguished. This can be directly derived from Beers law [see Eq. (3)], if it is written in matrix form

\[
\begin{pmatrix}
\mu_a(\lambda_1) \\
\vdots \\
\mu_a(\lambda_L)
\end{pmatrix} = \begin{pmatrix}
\varepsilon_1(\lambda_1) & \cdots & \varepsilon_k(\lambda_1) \\
\vdots & \ddots & \vdots \\
\varepsilon_1(\lambda_L) & \cdots & \varepsilon_k(\lambda_L)
\end{pmatrix} \begin{pmatrix}
c_1 \\
\vdots \\
c_K
\end{pmatrix},
\]

\[
\mathbf{m}_a = E \cdot c.
\]

If the matrix \( E \) with the molar absorption coefficients has a low condition number \( \kappa(E) \), all singular values are to some degree similar. This ensures that the measurements are roughly equally sensitive for all chromophores. Thus, a proper set of wavelengths should lead to a matrix \( E \) with a low condition number.

These two criteria depend, as expected, on the wavelengths of the lasers, on the scattering model, and on the molar absorption coefficients of the chromophores. The wavelengths of the lasers can be adjusted quite accurately. The scattering model appears to be consistent with real breast tissue in the relevant near-infrared band.\(^{23,24}\) But the molar absorption coefficients given in literature for the main chromophores in breast tissue show significant deviations, as will be shown. For this reason, it is advantageous to choose a set of wavelengths that leads to a robust reconstruction of the chromophore concentrations, even if the assumed absorption spectra deviate from reality. In the following, a criterion is derived to allow for this.

The starting point is Beer’s law \((6)\). It is assumed that the matrix \( E \) represents the assumed molar absorption coefficients. In the following, we furthermore introduce a matrix \( \tilde{E} \) that contains the (unknown) correct molar absorption coefficients. The difference between these two matrices is defined as \( \Delta E \). According to Eq. (6), \( c \) is the chromophore concentration vector, which gives the absorption vector \( \mathbf{m}_a \) after multiplication with \( E \). Analogously, we define \( \tilde{c} \) as the concentration vector that gives \( \mathbf{m}_a \) if it is multiplied with \( \tilde{E} \). The difference between the two concentration vectors is \( \Delta c \). Thus, the equation

\[
\mathbf{m}_a = E \cdot c = \tilde{E} \cdot \tilde{c} \Rightarrow E \cdot c = (E + \Delta E) \cdot (c + \Delta c),
\]

holds for any given absorption vector \( \mathbf{m}_a \). In other words: the error \( \Delta E \) of the matrix \( E \) results in an error \( \Delta c \) of the concentration vector \( c \) for a given absorption vector \( \mathbf{m}_a \).

To quantify this error, it is necessary to have an idea of \( \Delta E \), and to know the dependency of \( \Delta c \) on \( E \) and \( \Delta E \). Equation (7) can be solved for \( \Delta c \) with a first-order approximation, if it is assumed that the entries of the matrix \( \Delta E \) are small compared to the entries of \( E \):

\[
\Delta c = -(E^T E)^{-1} E^T \Delta E c.
\]

It should be noted that the absolute errors \( \Delta c \) written in this form depend on \( c \). Since typical concentrations of the chromophores vary by several orders of magnitude, optimizing the absolute errors of \( c \) is not meaningful. The interesting quantity are the relative errors of \( c \). To get these relative errors, we scale the entries of \( E \) and \( \Delta E \) with typical chromophore concentrations. Then, the vector \( c \) becomes a vector of ones for the typical case, and \( \Delta c \) contains the relative errors with respect to this case.

If the standard deviations for the scaled molar absorption coefficients are known, they can be used to generate an assumption for the matrix \( \Delta E \) and to calculate \( \|\Delta c\| \) for a given set of wavelengths.

Recapitulating, the norm of the errors \( \|\Delta c\| \) is a measure for the reconstruction errors that can occur for the chromophore concentrations due to uncertainties in the absorption spectra of the chromophores. Thus, the new criterion is to choose a set of wavelengths with a small value for \( \|\Delta c\| \). All three introduced criteria [derived from the Eqs. (5), (6), and (8)] have to be considered simultaneously for an optimal set of wavelengths.

For wavelength optimization, in the following, the scattering power \( b \) is assumed to be 1, and typical values for the chromophore concentrations are assumed to be \( c_{HBO} = 10 \text{ mM} \) (oxygenated hemoglobin), \( c_{HBO} = 5 \text{ mM} \) (deoxygenated hemoglobin), \( c_{\text{Water}} = 50\% \) and \( c_{\text{Lipid}} = 50\% \). These con-
age artifacts near sources and detectors,27 a spatially varying gradient regularization is used, in contrast to Ref. 26. A more sophisticated approach is given in Ref. 27.

The chromophore absorption spectra and the scattering model can be chosen freely for simulations as well as for reconstruction.

5 Results

Different absorption spectra are available for water,28–32 lipid,32–36 oxyhemoglobin, and deoxyhemoglobin.32,37,38 The spectra used here are presented in Fig. 2, showing significant deviations. Reasons for these deviations are, among others, that the optical properties of oxygenated and deoxygenated hemoglobin as well as human fat cannot be measured directly in vivo but have to be approximated by ex vivo measurements or measurements of similar substances (e.g., vegetable oil for human fat). The amount of deviation depends on the regarded chromophore and wavelength. To consider this chromophore and wavelength-dependent uncertainty, the standard deviations are determined and used as entries for the matrix \( \Delta E \) in Eq. (8):

\[
\Delta E_{jk} = \left\{ \frac{1}{J_k - 1} \frac{1}{J_j - 1} \sum_{j=1}^{J_k} \sum_{j'=1}^{J_j} \frac{\epsilon_i(\lambda_j) - \frac{1}{J_k} \sum_{j'=1}^{J_k} \epsilon_i(\lambda_{j'})}{\left( \epsilon_i(\lambda_j) - \frac{1}{J_k} \sum_{j'=1}^{J_k} \epsilon_i(\lambda_{j'}) \right)^2} \right\}^{1/2},
\]

where \( \epsilon_i(\lambda_j) \) is the molar absorption coefficient of the \( j \)'th of \( J_k \) absorption spectra for the \( k \)'th chromophore at the wavelength \( \lambda_j \).

For the calculation of the three criteria [derived from the Eqs. (5), (6), and (8)], the values of the molar absorption coefficients are set to the mean value of all available spectra:

\[
\epsilon_i(\lambda_j) = \frac{1}{J_k} \sum_{j=1}^{J_k} \epsilon_i(\lambda_j).
\]

To find an optimal set of five wavelengths for the imaging of all four chromophores and the scattering amplitude, the three criteria are computed for all possible combinations of wavelengths between 650 and 930 nm (10-nm step size; approximately 120,000 combinations). The histograms of condition number, residual, and norm of errors are shown in part in Fig. 3. As can be seen, many wavelength sets lead to a good (=low) condition and a low norm of the errors, but only a few lead to a high residual. From this visualization, it does not become clear, if there are wavelength sets, which lead to good values for all three criteria at the same time.

To come to a clearer visualization that illustrates the additional benefit of the new criterion, the two 2-D plots in Fig. 4 are used. Each dot in the plot on the left represents one set of wavelengths and its \( \kappa \) - and \( r \)-values. In the plot on the right, the histogram of \( \| \Delta \mathbf{c} \| \)-values is plotted for all sets of wavelength, for which the values of \( \kappa \) and \( r \) are within a narrow range, indicated by the dotted box in the left plot, i.e., considering only the two criteria based on \( \kappa \) and \( r \), all these sets of wavelengths perform comparably. But looking at the histogram, it can be seen that the distribution of the \( \| \Delta \mathbf{c} \| \)-values is quite wide. In other words, the performance of the sets with respect to uncertainties in the spectra varies a lot. Only those sets with a low value of \( \| \Delta \mathbf{c} \| \) are assumed to be optimal.
Since it is quite difficult to choose an optimal set from this kind of visualizations, a combined value of all three criteria is preferable. A simple weighted summation turned out to be a good solution. The weights are necessary, because the three criteria vary with different order of magnitude, as can be seen in Fig. 3. The combined value is calculated as follows:

\[ S = 50 \cdot \| \Delta c \| + 100 \cdot r + \kappa(E). \]  

(11)

The factors were determined empirically using Fig. 3 and are somewhat arbitrary, but their exact values are not critical for the resulting sets of wavelengths.

Figure 5 shows the 150 best sets of wavelengths (i.e., with the highest value of \( S \)). As could be expected, the sets are very similar. The first wavelength always has a value around 650 nm (mean of the 150 best sets: 653 nm), the second around 720 nm (mean: 719 nm), the third around 810 nm (mean: 810 nm), the fourth around 870 nm (mean: 867 nm), and the fifth around 900 nm (mean 901 nm). To test whether these wavelengths result from the particular assumptions we made on the average tissue composition (50% water, 50% fat), we repeated the whole analysis for a tissue composition that is dominated by fat (70% fat, 30% water) and a tissue composition that is dominated by water (70% water, 30% fat). The resulting sets of wavelengths are only marginally different (mean for 70% water/30% fat: 653, 721, 810, 866, 900 nm; mean for 30% water/70% fat: 653, 718, 809, 863, 896 nm).

These sets of wavelength are different from those obtained without the third criterion, where the five preferred wavelengths have values around 650, 720, 870, 910, and 930 nm (see Corlu et al.21). A probable reason for this discrepancy is the quite large deviations of the absorption spectra for water and lipid for wavelengths above 900 nm (see Fig. 2).
The values of $\kappa$, $r$, and $\|\Delta c\|$ give an initial idea of the performance of a set of wavelengths. As an example, we analyze two sets in greater detail. The first set (650, 720, 810, 870, and 900 nm) is optimal if the norm of errors is ignored; the second set (650, 720, 870, 910, and 930 nm) is optimal if all three criteria are considered (see earlier). The $\kappa$-value, which is a measure for the separability of the chromophores, is 11.2 for the first set and 15.2 for the second set. This is a marginal change for the condition value of a matrix, i.e., the performance of the two sets with respect to the separability of the chromophores should be similar. The residual norm $r$ has a value of 0.39 for both sets; in other words, the uniqueness of the problem is equally assured for both sets. The $\|\Delta c\|$-value is 0.58 for the first set and 0.15 for the second set. This means that the root mean square (RMS) of the relative errors for typical values of water, fat, and hemoglobin is reduced from 58% to 15%, which seems to be a quite significant reduction of the reconstruction errors due to deviations in the absorption spectra.

To verify that the sets shown in Fig. 5 indeed minimize these reconstruction errors, simulated data for the phantom shown in Fig. 1 are reconstructed for the two sets of wavelengths. In the simulation we used, the mean absorption spectra according to Eq. (10) are applied.

For the reconstruction, the spectral power is fixed to 1 (the same value as in the simulations). All combinations of the available water, fat, and hemoglobin spectra are applied successively, leading to 64 different reconstruction results (4 water spectra x 4 fat spectra x 4 hemoglobin spectra). Additionally, a reconstruction is performed using the mean absorption spectra (as in the simulations). For each combination of spectra, three scalar values benchmarking the image quality are determined, concerning the quantification of the chromophores, the cross talk between chromophores, and the artifacts in the images. These scalars are explained in detail in the following.

To evaluate the quantification of the chromophores, in each image the RMS of the pixel values covering the inhomogeneity which is expected to give a signal in the respective image (e.g., in the water image, the RMS of the pixel values covering the water inhomogeneity is determined). The difference between this RMS value and the expected value in the according inhomogeneity is divided by the expected value to derive a relative error. The absolute values of these relative errors are averaged over the five images of one reconstruction. The resulting scalar is called quantification error $\Delta q$ in the following:

$$\Delta q = \frac{\text{RMS}_{\text{image}} - \text{RMS}_{\text{expected}}}{\text{RMS}_{\text{expected}}}$$
Fig. 6 Quantification error $\Delta q$ (left), cross-talk error $\Delta x$ (middle), and artifact error $\Delta a$ (right) for all 64 combinations of water, fat, and hemoglobin spectra. The dots represent the results for the first set of wavelengths (ignoring the norm of errors), the circles the results for the second set of wavelengths (considering the norm of errors). Cross talk is clearly reduced by the second set and artifacts are on average slightly reduced, while quantification errors are comparable.

$$\Delta q = \frac{1}{N} \sum_{n=1}^{N} \left( \frac{\sum_{i \in C_n} u_{n,i}^2}{N_{C_n}} \right)^{1/2} - w_n,$$

(12)

$n$ is the index running over all images ($n=1 \ldots N$), in our case, four chromophore images and the scattering amplitude image ($N=5$). $C_n$ is the set of all pixels covering inhomogeneity $n$ ($n=1 \ldots N$), and $N_{C_n}$ is the number of pixels in this set. The indexing is done such that the $n'$th inhomogeneity is expected to generate a signal in the $n$'th image. $v_{n,i}$ is the pixel value of the $i$'th pixel in the $n$'th image, and $w_n$ is the expected signal in the $n$'th inhomogeneity.

To evaluate the cross talk of the chromophores, in each image the RMS values for all inhomogeneities that are expected to give no signal in the respective image are determined, divided by the expected signal in this image and averaged over all inhomogeneities and images of one reconstruction. The resulting scalar is called cross-talk error $\Delta x$:

$$\Delta x = \frac{1}{N \cdot (N-1)} \sum_{n=1}^{N} \sum_{n'\neq n_2}^{N} \left( \frac{\sum_{i \in C_{n'}} u_{n',i}^2}{N_{C_{n'}}} \right)^{1/2} / w_{n_1}.$$

(13)

To evaluate artifacts in the background, in each image the RMS for the background pixels is calculated and divided by the expected signal in this image. The RMS values are again averaged over all images, leading to the artifact error $\Delta a$:

$$\Delta a = \frac{1}{N} \sum_{n=1}^{N} \left( \frac{\sum_{i \in B} v_{n,i}^2}{N_B} \right)^{1/2} / w_n.$$

(14)

$B$ is the set of all background pixels, and $N_B$ is the number of pixels in this set.

In Fig. 6, these three benchmark values are shown for all 64 reconstruction for both sets of wavelengths. The quantifi-
cation error (left) is comparable for both sets, while the crosstalk error is clearly reduced for the second set of wavelengths, showing the effectiveness of the new criterion for optimization. The artifact level (right) is also in average slightly better for the new set.

To get an idea how the reconstructed images look, three of the 64 reconstruction results are shown for each set of wavelengths:

1. The reconstruction results using the mean absorption spectra (reference).
2. Reconstruction results with strong artifacts for both sets (marked with arrows in the middle plot in Fig. 6).
3. Reconstruction results with strong cross talk for both sets (marked with arrows in the right plot in Fig. 6).

The reconstruction results are presented in Fig. 7 for the first set of wavelengths. The top row shows the chromophore concentrations and scattering amplitude for the case in which the mean absorption spectra are used for reconstruction. Only weak image artifacts and cross talk are present, since the absorption spectra for simulation and reconstruction are identical. The images in the second row show severe imaging artifacts, especially for water. In the third row, the example with strong cross talk between the chromophores and scattering amplitude is given. The oxyhemoglobin image suffers from significant cross talk of water and scattering, the water image shows cross talk of scattering and deoxyhemoglobin, and the lipid image of water.

These findings can now be compared to reconstruction results obtained with the second set of wavelengths (Fig. 8). Again, the top row shows the results for the case in which the mean absorption spectra are used for reconstruction. These images are largely comparable to those of Fig. 7. The artifacts at the rim of the water image are reduced. The images of the second row are reconstructed using the combination of absorption spectra leading to strong image artifacts. Compared to the corresponding images in Fig. 7, the artifacts are slightly reduced. The last row presents the images for the combination of absorption spectra that produces strong cross talk. But here cross talk is nearly not visible and significantly lower than for the first set of wavelengths.

![Fig. 8](https://www.spiedigitallibrary.org/journals/Journal-of-Biomedical-Optics-May-June-2009/Vol.14/l50098/034041-8)

Fig. 8 Reconstruction results for simulated data at 650, 720, 810, 870, and 900 nm. Top: Reconstruction with mean absorption spectra. Middle: Reconstruction showing strongest artifacts (same absorption spectra as in Fig. 7). Bottom: Reconstruction showing strongest cross talk (same absorption spectra as in Fig. 7). The images are scaled the same way as in Fig. 7.

![Fig. 9](https://www.spiedigitallibrary.org/journals/Journal-of-Biomedical-Optics-May-June-2009/Vol.14/l50098/034041-8)

Fig. 9 Cross-talk error $\Delta x$ (left) and artifact error $\Delta a$ (right) averaged for all 64 combinations of water, fat, and hemoglobin spectra for reconstructions with different amounts of relative noise. The dots represent the results for the first set of wavelengths (ignoring the norm of errors), the circles the results for the second set of wavelengths (considering the norm of errors). The advantage of reduced cross talk for the second set is also valid for noisy data. Artifacts and quantification errors (not shown here) are comparable for both sets in the presence of noise.
To verify that these results hold also if noisy data is used for reconstruction, different amounts of relative noise are added to the simulated measurement data before reconstruction. Relative noise up to 0.5% is applied, since for noise levels of 1% and higher, the artifact errors for both sets of wavelengths are above 90%, i.e., the inhomogeneities are completely buried by noise.

To come to a compact presentation of the results, the benchmark values $\Delta x$, $\Delta a$, and $\Delta g$ are averaged over all 64 combinations of different spectra. The results are shown in Fig. 9. Clearly, the advantage of reduced cross talk is still valid for noisy data (left plot), while artifacts and quantification errors (not shown) are comparable in the presence of noise.

Recapitulating the findings, we conclude that the introduced new criterion for wavelength optimization leads clearly to the intended minimization of cross talk, while artifacts and quantification errors are comparable to sets of wavelengths optimized without that criterion.

6 Conclusion

The introduced method for the optimization of laser wavelengths for CW DOT systems considers, in contrast to existing methods, the uncertainties in the absorption spectra of the chromophores. The absorption spectra are essential for reconstruction, if absorption and scattering should be distinguishable in CW DOT. For each of the chromophores, four absorption spectra were compared, revealing significant deviations.

Considering these deviations led to optimal sets of wavelengths different from those determined ignoring the uncertainties in the absorption spectra. It was demonstrated with simulated data that reconstructions based on the new sets of wavelength are significantly more robust with respect to cross talk, if the assumed absorption spectra deviate from reality.

Recently, Eames et al. published a method, also based on the criteria of Corlu et al., to optimize sets with a much larger number of wavelengths than considered here. It is straightforward to include the criterion introduced here in this method. Last, it should be noted that although this discussion is focused on CW data, it is straightforward to apply the introduced method to TD of FD measurements.

Acknowledgments

The authors would like to express their gratitude to Albert Cerussi (University of Irvine, California), Alper Corlu (University of Pennsylvania, Philadelphia), and Dirk Grosenick (Physikalisch-Technische Bundesanstalt, Berlin, Germany) for providing chromophore absorption spectra.

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Journal of Biomedical Optics 034041-9 May/June 2009 • Vol. 14(3)
Brendel and Nielsen: Selection of optimal wavelengths for spectral reconstruction in diffuse optical tomography


