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Abstract. Dynamic analyses of vibrational motion in cell membranes provide a lot of information on the complex dynamic motilities of a red blood cell (RBC). Here, we present the correlation properties of membrane fluctuation in discocyte and spherocyte RBCs by using quantitative phase microscopy (QPM). Since QPM can provide nanometer sensitivity in thickness measurement within a millisecond time scale, we were able to observe the membrane flicking of an RBC in nanometer resolution up to the bandwidth of 50 Hz. The correlation properties of the vibrational motion were analyzed with the detrended fluctuation analysis (DFA) method. Fractal scaling exponent α in the DFA method was calculated for the vibrational motion of a cell surface at various surface points for normal discocyte and abnormal spherocyte RBCs. Measured α values for normal RBCs are distributed between 0.7 and 1.0, whereas those for abnormal spherocyte RBCs are within a range from 0.85 to 1.2. We have also verified that the vibrational motion of background fluid outside of a cell has an α value close to 0.5, which is a typical property of an uncorrelated white noise. © 2011 Society of Photo-Optical Instrumentation Engineers (SPIE). [DOI: 10.1117/1.3601460]

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1 Introduction

Red blood cells (RBCs) exhibit dynamic and spontaneous vibratory motion in their cell surfaces, which is referred to as flickering. Frequency-domain or statistical analysis of flickering can be effectively used to determine the mechanical characteristics of a plasma membrane that consists of the lipid bilayer and the cytoskeletal protein (spectrin) network. RBC membrane fluctuations were first observed by Browicz in the late 19th century using light microscopy,¹ and the quantitative analysis of RBC membrane fluctuations were first reported by Brochard and Lennon in 1975.² The maximum height of the fluctuations was estimated to be in the order of $0.4 \mu\text{m}$, which is about 5% of the average diameter ($7.5 \mu\text{m}$) of a normal RBC. Numerous studies have been made to explore the physiological properties of RBC membrane flickering because it provides important biological functions.^{3–11} These studies showed that flickering is driven by thermal energy delivery⁶ and the metabolic energy associated with adenosine 5'-triphosphate (ATP).⁹ Recently, Park et al. showed the effect of ATP on membrane fluctuations and the biconcave shape in RBCs under normal and ATP-depletion condition.¹² Their results revealed that the depletion of ATP not only reduced membrane fluctuations, but also altered the biconcave shapes of RBCs. These mechanical characteristics determine the morphology and deformability of RBCs under normal and pathological conditions.

New noncontact interferometric techniques, called quantitative phase microscopy (QPM) based on interferometric techniques, such as Fourier phase microscopy,¹³ Hilbert phase microscopy,¹⁴ diffraction phase microscopy,¹⁵ and digital holographic microscopy¹⁶ have recently been proposed to provide the quantitative information about cell morphology. Several attempts have been made to analyze the characteristics of RBC using QPM.^{10,17–23} We previously proposed a QPM system with autofocusing and edge detection techniques for the accurate analysis of the volume of a living cell.²⁴ This QPM with spatially modulated interferometry can provide the ability to retrieve the optical path length distribution on a whole cell surface from a single interferogram image. Our QPM system makes it possible to measure the morphologic and dynamic characteristics of transparent samples with subnanometer path length sensitivity within a millisecond time scale.

In this paper, we have used our previously described QPM system²⁴ to study thickness fluctuations of an RBC. The measured temporal function of thickness fluctuations were analyzed with the detrended fluctuation analysis (DFA) method^{25,26} to study the connection between the correlation properties of the membrane flicking of an RBC and the morphological shape of an RBC: discocyte and spherocyte. DFA is a powerful method used to study the existence of long-range correlations in a temporal function. DFA has been recently used to analyze the dynamics of RBC flickering in young and old cells with phase contrast microscopy (PCM)²⁷ and differential interference contrast microscopy.²⁸ The previous studies have revealed that old cells showed relatively higher fractal scaling exponents than young

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cells. However, these conventional optical imaging techniques essentially provide qualitative information for a given sample since the relationship between the intensity and phase of the image field is generally nonlinear,^{29,30} especially when the amplitude of vibration becomes close to the wavelength of the laser used in measurements. Since the amplitude of membrane flickering in an RBC becomes as large as $0.4 \mu\text{m}$, it is very important to use a quantitative phase measurement technique which can measure the actual amplitude of a membrane vibration in an RBC. In this study, we have used QPM to measure the thickness fluctuations of RBCs. These thickness fluctuations represent RBC membrane flickering in a good approximation. In order to analyze the long-range correlation properties of the measured membrane vibration, we have used DFA. We have shown that the fractal scaling exponent α of the DFA method are quite different with each other for normal discocyte and abnormal spherocyte RBCs. It is demonstrated that the fractal scaling exponent α for the vibrational noise observed in the background fluid outside of a cell is very close to that of a typical white noise. We also present two-dimensional (2D) maps of fractal scaling exponent α over the whole cell surfaces, as well as background fluids for discocyte and spherocyte RBCs.

2 Materials and Methods

2.1 Sample Preparation

Cells were prepared with the same procedures as previously described in Ref. 24. Fresh blood was collected from a mouse, and $10 \mu\text{l}$ of it was diluted by 50-fold with a low K^+ solution (Mm: KCl 2, NaCl 145, HEPE-Na 10, MgCl_2 0.15, and 1 mg/ml BSA). This low K^+ solution works as a surrounding medium for the observation of an RBC in our QPM system. After being washed twice, normal discoid shape RBCs were adjusted to an appropriate experimental concentration, and then abnormal spherical shape RBCs were prepared by adding 1.3 mM Ca^{2+} and 1 mM of A23187 to the low- K^+ solution. This dehydrates RBCs and acts as a Ca^{2+} ionophore to transport ions across the lipid bilayer of RBC membrane.³¹ All experiments were carried out at 25°C .

2.2 Quantitative Phase Imaging

We have used the QPM system proposed by Professor Michael Feld's group at MIT (Ref. 14) to obtain a time series of quantitative phase images of RBC membrane fluctuations. The QPM system has provided a quantitative phase image with subnanometer optical path length sensitivity. Quantitative 2D phase information $\phi(x,y)$ can be easily converted into a 2D thickness profile $t(x,y)$ by using the equation: $\phi(x,y) = 2\pi/\lambda \cdot \Delta n \cdot t(x,y)$, where λ is the center wavelength of the light source, Δn is the difference in refractive index between the RBC and the surrounding medium. The basic configuration of the QPM is a combination between a Mach-Zehnder interferometer with a laser diode as an optical source and an optical microscope with a charge coupled device (CCD) as an image capturing device. The center wavelength of the laser diode is 633 nm, and the optical magnification of the imaging system is calibrated to be ~ 110 for the imaging system. After using appropriate high frequency filtering and the Hilbert transformation of a recorded interferogram captured by the CCD, we can obtain a quantita-

tive phase image $\phi(x,y)$. The 2D thickness profile $t(x,y)$ of a cell is calculated from $\phi(x,y)$, where the refractive index difference Δn between the RBCs and the surrounding medium of our low K^+ solution is estimated to be 0.06.¹⁹

2.3 Detrended Fluctuation Analysis

The following DFA algorithm has been previously described by Peng et al.²⁵ For a given data series of length N , we calculate a new integrated time series $y(k)$ defined with

$$y(k) = \sum_{i=1}^k [t(i) - t_{\text{ave}}], \quad (1)$$

where $t(i)$ is the i 'th value of the original thickness data, and t_{ave} is the average value of the original thickness data. Next, the integrated time series $y(k)$ is divided into nonoverlapping boxes of equal length n . In each box of length n , $y(k)$ is fit with a straight line using a least-square fitting method, which represents the local trend in that box. The y -coordinate of the least fit line in each box is denoted by $y_n(k)$. Then, the integrated time series $y(k)$ is detrended by subtracting the local trend $y_n(k)$ in each box of length n . For a given box size n , the root-mean-square (rms) fluctuation for this integrated and detrended time series is calculated by

$$F(n) = \sqrt{\frac{1}{N} \sum_{k=1}^N [y(k) - y_n(k)]^2}, \quad (2)$$

where N is the total length of the original data. This calculation is repeated over all box sizes to evaluate the relationship between $F(n)$ and the box size n . The slope of a graph between $\log F(n)$ and $\log n$ represents a scaling exponent α , which characterizes the correlation properties of the original time series signal $t(i)$. A power-law relation $F(n) \sim n^\alpha$ implies different correlation properties for different values of the fractal scaling exponent α . When $0 < \alpha < 0.5$, a time series signal is stationary or anticorrelated. A time series represents uncorrelated randomness or white noise if $\alpha \cong 0.5$. When $0.5 < \alpha$, a time series is considered to be correlated. A time series with $\alpha \cong 1$ corresponds to $1/f$ noise (pink noise). A time series of nonstationary or like random walk has $\alpha > 1$. When $\alpha \cong 1.5$, the time series represents a random walk (Brownian motion).

2.4 Statistical Analysis

Data were analyzed by ANOVA using STATVIEW 5.0.1 software (SAS Institute, Inc.) and summarized as the mean \pm SEM. Statistical significance was accepted for cases with $p < 0.05$.

3 Results and Discussions

3.1 DFA Computation of Time Series RBC Thickness Data Obtained by QPM

In order to analyze RBC membrane fluctuations, we have measured 2000 sequential thickness images of the normal discoid shape and the abnormal spherical shape RBCs. These cells were observed for 20 s with an imaging speed of 100 frames/s.

Figure 1(a) shows a typical 2D thickness image for a normal discocyte RBC. The color bar on the right side of the figure

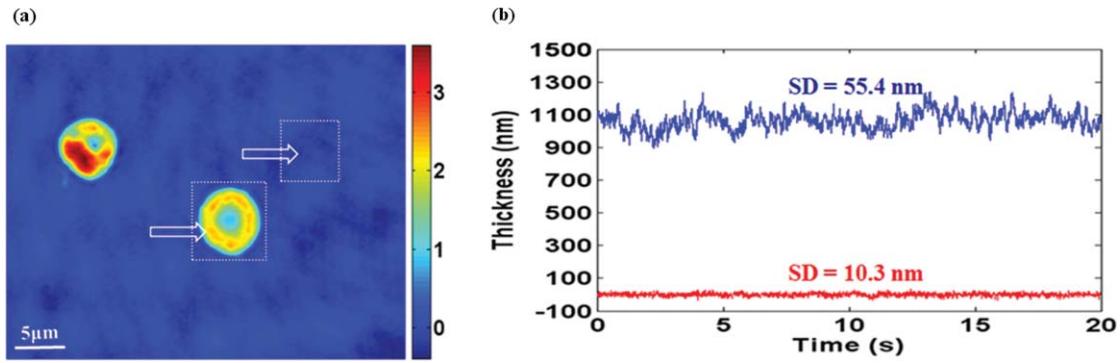


Fig. 1 (a) Thickness image of normal RBCs with QPM with a colorbar in micrometers. (b) Temporal thickness variations for a pixel inside a cell (upper plot) and a pixel outside a cell (lower plot); two corresponding pixels are indicated by two arrows in (a).

indicates the thickness of a cell in micrometers. Figure 1(b) shows temporal thickness variations at two different points indicated by two arrows in the measured thickness image of Fig. 1(a). The upper graph shows temporal fluctuations in thickness for a pixel on the membrane of the normal discocyte RBC, while the lower graph shows those for a pixel on the surrounding medium outside of the discocyte. The standard deviation (SD) of the amplitude of the membrane vibrations is 55.4 nm in the upper graph of Fig. 1(b), while the SD of the background medium is shown to be 10.3 nm in the lower graph. These results indicate that the RBC membrane undulation amplitude is significantly larger than the background noise. Since we have a very small refractive index difference of 0.06 between the cell and the surrounding medium, 10.3 nm error in thickness $t(x,y)$ corresponds to 0.62 nm ($\approx \lambda/1000$) measurement sensitivity in

optical path length difference, which is defined as the product of refractive index difference Δn and thickness $t(x,y)$.

Figure 2(a) shows the same flicking data at one point on the RBC membrane that is the same as the one shown in the upper plot of Fig. 1(b). Since 100 images were taken in 1 s, we have 2000 data points for the whole observation period of 20 s. We have used this data for time series data $t(i)$ defined in Eq. (1). Integrated time series $y(k)$ were calculated using Eq. (1) and are plotted with the line (1) in Fig. 2(b). The line (2) in Fig. 2(b) shows the representative example of local trend $y_n(k)$. The local trend $y_n(k)$ was fit in each box with a length of 200 data points using a least-square line fit. Finally, we obtained a double log graph between $\log F(n)$ and $\log n$ by repeating the calculation shown in Eq. (2). Figure 2(c) shows the plot of $\log F(n)$ with respect to $\log n$. The fractal scaling exponent α for

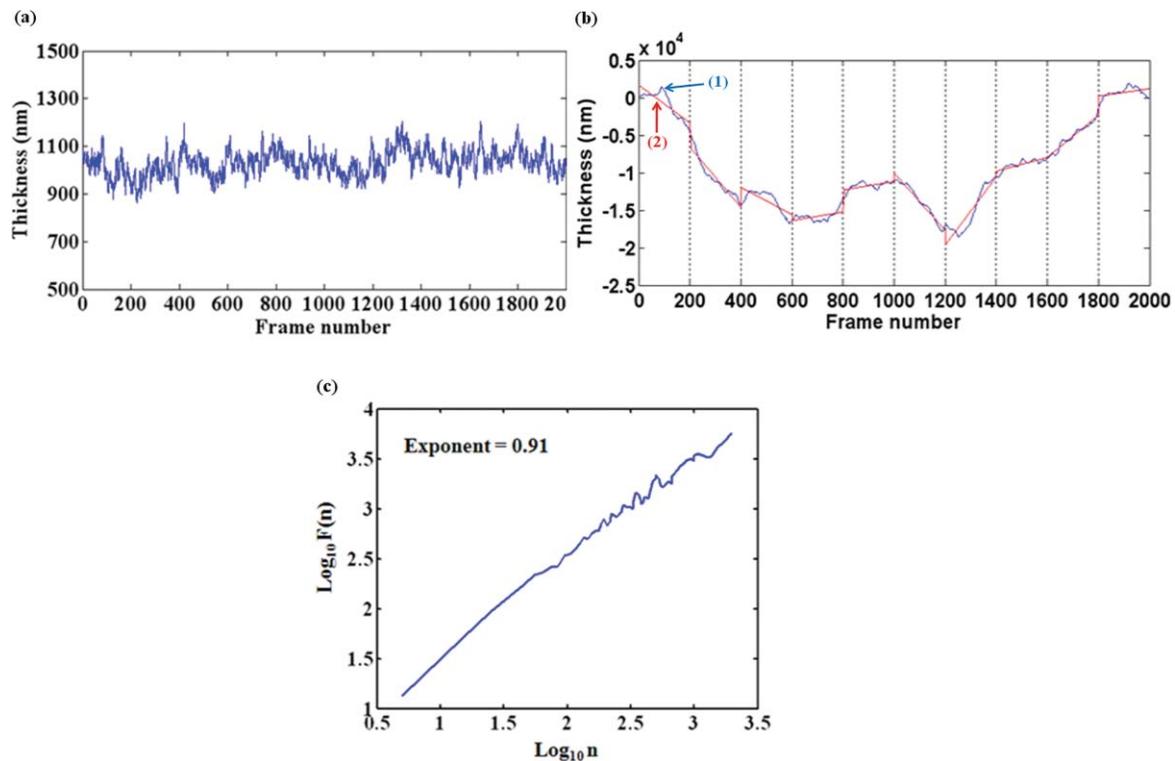


Fig. 2 (a) Typical thickness fluctuation data $B(i)$ for a pixel on the membrane of a normal RBC. (b) The integrated time series $y(k)$ depicted as line (1) and the local trend $y_n(k)$ depicted as line (2). (c) Log-log plot for $F(n)$ and n .

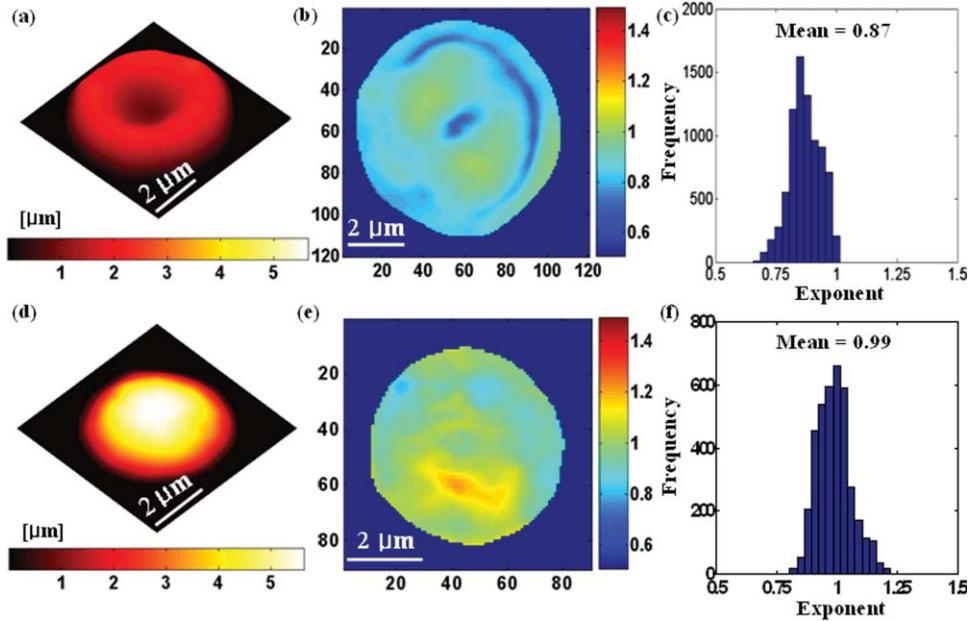


Fig. 3 Averaged thickness images [(a) and (d)] and their corresponding fractal scaling exponent maps [(b) and (e)] for a discocyte and a spherocyte RBCs. Histogram of fractal scaling exponent α for the discocyte RBC, (c) and the spherocyte RBC (f).

this vibrational motion is calculated to be 0.91 from this log-log plot. This suggests that the flicking motion of the membrane of a normal discocyte RBC has long-range correlation properties. These results were in good correspondence to the previous study of normal RBCs using PCM.²⁷

3.2 Spatial Correlation Properties of Membrane Fluctuations in Discocyte and Spherocyte RBCs

From a series of measured thickness images for an RBC, we obtained temporal thickness fluctuation data that were similar to the data shown in Fig. 2(a) for each pixel in the series of measured images. From the thickness fluctuation data, we have calculated the fractal scaling exponent α for each pixel with the procedures explained in Sec. 3.1. As a result, a 2D map of α

was constructed for an RBC from a series of thickness images obtained by QPM.

Figures 3(a) and 3(d) are thickness images of discocyte and spherocyte RBCs, respectively. Figure 3(b) shows a 2D map of α for the normal discocyte RBC, while Fig. 3(e) is the 2D map of α for the abnormal spherocyte RBC. Statistical properties of the calculated α for discocyte and spherocyte RBCs can be clearly seen by two histograms of α displayed in Figs. 3(c) and 3(f). Calculated α values from the thickness data of the discocyte are distributed between 0.7 and 1.0, and their mean value is 0.87. These results reveal that there exists a long-range correlation in the membrane fluctuations of a normal discocyte RBC. As illustrated in Fig. 3(e), calculated α values from the thickness data of the spherocyte are within a range from 0.85 to 1.2. Its mean value is 0.99. These results indicate that detrended fluctuation analysis for the dynamical properties of membrane

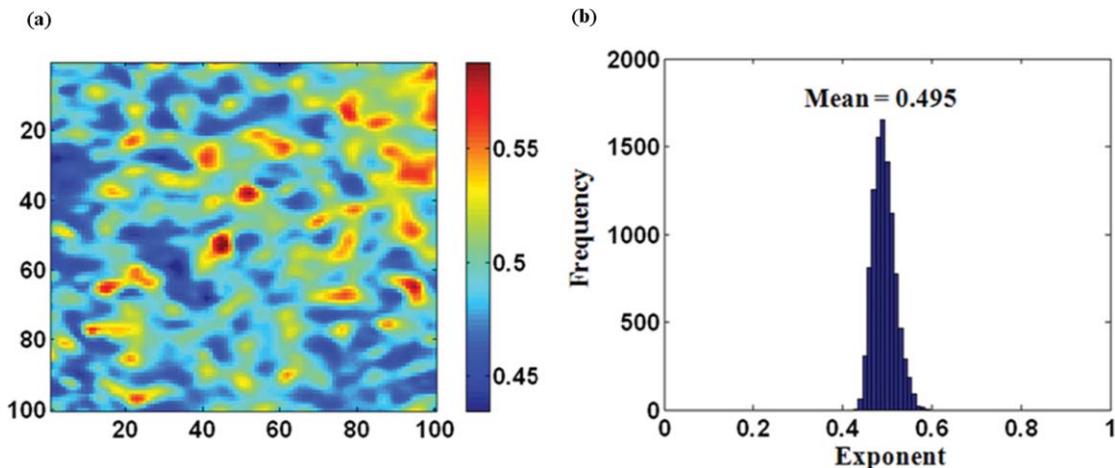


Fig. 4 (a) Fractal scaling exponent map of background fluid outside a cell indicated with a white dashed box in Fig. 1(a). (b) Histogram of fractal scaling exponent α for the background fluid.

flicking in the abnormal spherical shape RBC is more or like random walk.

We have also measured fractal scaling exponent α for the background medium in our system without a sample cell. Figure 4(a) shows a 2D map of fractal scaling exponent α for an area without a cell indicated by the white dashed square in Fig. 1(a). Figure 4(b) is the histogram of α for the pixels within the 2D map of Fig. 4(a). It shows that 96.5% of the measured α for the background fluid without a sample ranges from 0.46 to 0.54. The average value of the measured exponents for the background fluid is approximately 0.5, which demonstrates that the time series of background fluid fluctuation is an uncorrelated white noise.

We have repeated the above measurement of the fractal scaling exponent α for 10 different normal discocyte RBCs and 10 abnormal spherocyte RBCs, as well as for the background fluids of these RBC samples. Figure 5 shows the box plot representation of measured fractal scaling exponent distributions for discocytes, spherocytes, and background fluids. The mean and the SD of measured exponent values (mean \pm SD) for the discocytes and the spherocytes are 0.86 ± 0.03 and 0.99 ± 0.02 , respectively. And, those for the background fluids are 0.49 ± 0.03 . This finding suggests a significant difference in the long-range scaling behavior between healthy (discocyte) and diseased states (spherocyte). It is well known that a vibrational motion is unbounded or like random walk when the fractal scaling exponent α is larger than 1.²⁵ We have also calculated the percentage of pixels whose scaling exponent is larger than 1 ($\alpha > 1$) for these two different types of RBCs. 2.3% of pixels in discocytes have their scaling exponent larger than 1, while 46.2% of pixels in spherocytes have $\alpha > 1$. These results show that the fluctuation motion of the membrane of a spherocyte resembles an unbounded random walk more than that of a discocyte. Studies on membrane fluctuations in discocytes and spherocytes have been previously reported by using a QPM system. Popescu et al. showed an increase in membrane tension as a discocyte was changed to a spherocyte.¹⁸ Also, Park et al. recently reported significant increases in the shear and the bending moduli of the membrane associated with morphology changes in an RBC.³²

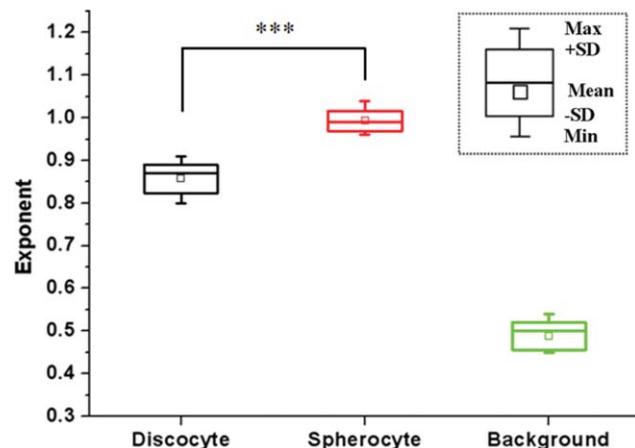


Fig. 5 Box plots for the distributions of the measured fractal scaling exponents of 10 normal discocyte RBCs, 10 abnormal spherocyte RBCs, and 10 background fluids (***) $p < 0.0001$, discocytes versus spherocytes).

In this paper, we have demonstrated a relationship between the temporal correlation properties of membrane fluctuation in an RBC and its morphological shape (discoid and spherical shapes). Variances in p -value between discocytes and spherocytes displayed in Fig. 5 clearly verify differences between these two morphological shapes of an RBC ($p < 0.0001$).

Our findings are of great importance for the relationship between correlation properties of membrane fluctuations and metabolic driving force depending on ATP. We suggest a scenario that the increase of membrane rigidity in the absence of ATP forces to have a larger fractal scaling exponent α in spherocytes, which means correlation property with a random walk or a Brownian motion. We believe that these results of higher stiffness and a larger fractal scaling exponent are results of low deformability and ATP deletion in spherocytes due to A23187 induced calcium accumulation. Based on these findings, we could assume that the transition from discocytes to spherocytes causes the change of the mechanical characteristics and the correlation properties of RBC membrane fluctuations. In this regard, our study has verified that QPM can be effectively used with the detrended fluctuation analysis for a time series motion of absolute thickness undulations in an RBC by showing the significant difference in fractal scaling exponent between discocytes and spherocytes.

4 Conclusions

We have used QPM for DFA as a tool to differentiate a discocyte RBC from a spherocyte RBC by monitoring the correlation properties of membrane fluctuations in a noninvasive manner. We have measured the absolute thickness variations for an RBC with interferometric QPM and analyzed its temporal correlation properties with DFA from the time series of thickness fluctuation data for each pixel in QPM images. Fractal scaling exponents for discocyte and spherocyte RBCs were calculated and analyzed over their whole cell surfaces. We have also validated the usage of DFA for the analysis of temporal membrane fluctuation in an RBC with our QPM system by measuring the fractal scaling exponents of the background fluid without a sample. Based on our preliminary results on the possibility of differentiating normal and abnormal RBCs with DFA for temporal thickness fluctuation data measured with our QPM technique, we believe that QPM, with the help of DFA, can be effectively applied to study the complex dynamic properties of the membrane vibration of an individual cell under various physiological conditions.

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