Time-reversed ultrasonically encoded optical focusing into tissue-mimicking media with thickness up to 70 mean free paths

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Abstract. In turbid media such as biological tissue, multiple scattering hinders direct light focusing at depths beyond one transport mean free path. As a solution to this problem, time-reversed ultrasonically encoded (TRUE) optical focusing is proposed based on ultrasonic encoding of diffused laser light and optical time reversal. In TRUE focusing, a laser beam of long coherence length illuminates a turbid medium, where the incident light undergoes multiple scattering and part of it gets ultrasonically encoded within the ultrasonic focal zone. A conjugated wavefront of the ultrasonically encoded light is then generated by a phase conjugate mirror outside the medium, which traces back the trajectories of the ultrasonically encoded diffused light and converges light to the ultrasonic focal zone. Here, we report the latest experimental improvement in TRUE optical focusing that increases its penetration in tissue-mimicking media from a thickness of 3.75 to 7.00 mm. We also demonstrate that the TRUE focus depends on the focal diameter of the ultrasonic transducer.

Keywords: ultrasonic modulation; optical phase conjugation; time reversal; multiple scattering; light manipulation, holographic recording.

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1 Introduction

In biomedical optical imaging, a variety of technologies, such as confocal microscopy, multiphoton microscopy, and optical coherence tomography, are being pushed to improve the imaging resolution and penetration depth in tissue. However, multiple scattering is an insurmountable barrier for direct focusing into biological tissue at depths beyond one transport mean free path, which limits the penetration depth of these technologies to ~1 mm in the skin. To overcome this optical diffusion limit, the incident wavefront can be shaped to maximize the possibility of delivering light to a desired region. One such approach that focuses light inside, or through, a turbid medium is to adaptively shape the wavefront of the incident light through a feedback loop. The feedback mechanism, however, requires the presence of a guide star—a luminous point. In addition, the iterative feedback algorithm is computationally intensive and takes several minutes to complete the wavefront optimization, which is much longer than the millisecond time scale required for biological tissues. These limitations prevent the technology from being practical for biomedical imaging. Nevertheless, iterative shaping with a feedback loop is not the only way to shape the incident wavefront. By generating a phase conjugated copy, i.e., a wavefront whose shape is identical down to the wavelength scale, optical phase conjugation (OPC) can suppress the turbidity effects of scattering media and can focus through biological tissues.

Recently, time-reversed ultrasonically encoded (TRUE) optical focusing has been proposed. By phase conjugating a wavefront that emanates from a virtual source (i.e., a guide star) inside a turbid medium, light is focused back to the spot coinciding with the virtual source. In this technique, a focused ultrasound wave noninvasively modulates diffused coherent light, providing a virtual source in the turbid medium. Outside of the medium, a phase conjugate copy of the modulated diffused light wavefront is generated through a holographic method, and is focused back to the virtual source location inside the scattering medium. Here, the TRUE focal region is determined by the focused ultrasound wave, whose scattering is negligible compared to light in tissue. Therefore, TRUE optical focusing can noninvasively and dynamically focus light to an arbitrary location within a turbid medium.

In this article, we report the latest experimental improvement in TRUE optical focusing that increases its penetration from a thickness of 3.75 to 7.00 mm in tissue-mimicking media. We also demonstrate that the TRUE focus depends on the focal diameter of the ultrasonic transducer.

2 Methods

2.1 Experimental Setup

TRUE focusing consists of two consecutive procedures, i.e., holographic recording and reading. In the recording procedure, light diffuses inside a scattering medium, where part of the light is encoded by a focused ultrasonic wave. The encoded light from this virtual source, noted as S, interferes with a reference
Fig. 1 Schematic of the experimental setup for TRUE optical focusing. EOM, electro-optic modulator; PBS1-3, polarizing beam splitter; S1-3, shutter; HWP1-3, half-wave plate; M1-3, mirror; AOM1-2, acousto-optic modulator; L1-3, lens; PD1-2, photodiode; BE1,2, beam expander; R, reference beam; R*, conjugate reference beam; WT, water tank filled with deionized water; UT, ultrasonic transducer; S*, collected diffused signal light through the sample; S', time-reversed signal light; PRC, photorefractive crystal [a 10×10×5 mm³ Bi₁₂SiO₂₀ (BSO) crystal was used in the study]; HVAC, high voltage ac electrical field; XYZ, system coordinates (x = sample scanning axis, y = acoustic axis, and z = axis of incident signal beam propagation).

The synchronized wave is sent to a power amplifier (50 dB, ENI, synchronized for the whole period of recording and reading. The high frequency, amplitude, and burst duration (200 ms), which is transmitted through an electro-optic modulator (EOM, Conoptics M350-50) to switch the polarization between the horizontal and vertical states by varying the driving voltage of the EOM. In the recording stage, light is vertically polarized by the EOM, so that almost all of the light is transmitted through PBS1. Then, the light is split into a signal beam S (with vertical polarization) and a reference beam R (with horizontal polarization) by a variable beam splitter composed of a half-wave plate (HWP2) and a polarizing beam splitter (PBS2). The signal beam is sent through two acousto-optic modulators (AOM1 and AOM2, IntraAction AOM-802AF1) in series to tune its optical frequency to \( f_S = f_0 - f_a \), where \( f_0 \) is the laser frequency and \( f_a \) is the net frequency shift due to the two AOMs. The signal beam, after transmitting through PBS3, is incident on the front surface of a tissue-mimicking phantom.

The incident light is multiply scattered in the phantom, and within the focused ultrasonic beam it is encoded by an ultrasonic wave with frequency \( f_a \). Three different ultrasonic transducers are used in the experiment: Panametrics A381S for \( f_a = 3.5 \) MHz, Panametrics A302S for \( f_a = 1.0 \) MHz, and Sonic Concepts H-148 for \( f_a = 2.0 \) MHz. A function generator (Agilent 33250A) generates a sinusoidal wave with a specific frequency, amplitude, and burst duration (200 ms), which is synchronized for the whole period of recording and reading. The synchronized wave is sent to a power amplifier (50 dB, ENI, 240L), resulting in pressures of 0.70 MPa at the 3.5 MHz ultrasonic focus, 0.33 MPa at the 1.0 MHz focus, and 1.44 MPa at the 2.0 MHz focus. The corresponding mechanical indexes are 0.37, 0.33, and 1.02, respectively. To maximize the ultrasonic encoding efficiency, the ultrasonic focus is aligned to overlap the center of the diffused light profile within the medium. The light encoded by the ultrasonic wave has a frequency shift of \( f_a \).

The transmitted light exiting the backside of the sample consists of three spectral components: the “unencoded” photons at \( f_S = f_0 - f_a \), and the “encoded” photons \( S(f_a) + S(f_a) \) at \( f_a = f_0 \) and \( f_a = f_0 - 2f_a \), respectively. All three light components are collected and mixed with \( R \) within a 10×10×5 mm³ Bi₁₂SiO₂₀ (BSO) crystal, but only \( S(f_a) \) can form a stable interference fringe with \( R \), which is recorded in the crystal; the other frequency components form traveling interference fringes that are averaged out within the 190 ms recording time. To enhance the recording efficiency, a 2.1 kHz, 8 kV (peak-to-peak) high voltage square wave electrical field is applied across the crystal. The response time of the crystal is approximately inversely proportional to the illuminating light intensity.

In the subsequent reading stage, the EOM changes the laser beam to horizontal polarization. As a result, both the signal and reference beams are now turned off, and the beam reflected by PBS1 forms \( R^* \), which is incident on the crystal in the direction opposite that of \( R \). The polarization of \( R^* \) is tuned by HWP1 to accommodate the optical activity of the BSO crystal. The hologram recorded by \( S \) and \( R \) in the crystal thus can be read by \( R^* \) to generate a time-reversed copy of \( S(f_a) \), denoted as \( S^*(f_a) \). Due to its reversibility, \( S^*(f_a) \) accurately traces back the trajectories of \( S(f_a) \) to the focused ultrasonic region, hence achieving optical focusing inside the scattering medium.

In the ultrasonic focal zone, \( S^*(f_a) \) is again ultrasonically modulated, resulting in three components: \( S^*(f_a), S^*(f_a + f_a), \) and \( S^*(f_a + f_a) \) (with frequencies at \( f_0, f_0 + f_a, \) and \( f_0 + f_a \), respectively). All three components were transmitted through the rest of the sample, with polarization tuned by HWP3 for maximum reflection at PBS3. The time-reversed light is finally focused by lens L1 onto a photodiode PD1 with 13 mm² of active aperture (Thorlabs PDA36A). The collected TRUE signal is digitized by an oscilloscope (Tektronix TDS5034) and downloaded to a computer for further processing.

In our previous work,\(^4\) we demonstrated the focusing of light into the middle of a tissue-mimicking phantom sample with an optical thickness of 25 (i.e., thickness of 25 mean free paths), equivalent to a depth of 1.25 mm in soft tissue. In this paper, the system was updated by employing an EOM to switch light between writing and reading, in order to focus light deeper into the turbid media. Three tissue-mimicking phantoms, made from porcine gelatin, water, and intralipid, with different thicknesses but the same anisotropic factor, were used in the study.

### 3 Results

#### 3.1 Time-Reversed Ultrasonically Encoded Signal and a Comparison To Ballistic Light

Compared with wavefront correction techniques that require seconds or even minutes, a PRC has a much faster response, which monotonically decreases as a function of optical illumination intensity\(^5\) for the formation of a stable hologram. The
response time was on the order of 100 ms in our experiment, limited by the weak intensity of the modulated light. During the measurements, the recording time was set to 190 ms, which effectively averaged out influences from ambient sources, e.g., air disturbance. In the reading procedure, the hologram written on the BSO crystal was almost instantly erased by intense illumination, and simultaneously a phase conjugate copy was generated from the diffraction on the crystal. An example of the obtained TRUE signal waveform is shown in Fig. 2, and the amplitude of the peak immediately after both shutters S1 and S2 are turned on at time 0 is recorded as a TRUE signal. The noise mainly came from shot noise and the spatial noise of randomly distributed charge carriers, both of which can be reduced by coherent averaging.

Compared with the negative exponential decay of ballistic light, the TRUE signal originating from modulated diffused light had a much slower decay rate, as shown in Fig. 3. Hence, the TRUE signal was more resistant to multiple scattering, and more efficient in delivering energy to a target in biological tissue. After transmitting through a turbid layer with an optical thickness of $\mu_s L$, the output ballistic light intensity $I_f$ equals $I_0 \exp(-\mu_s L)$, where $I_0$ is the input laser intensity, the extinction coefficient $\mu_s = \mu_s + \mu_a = 10 + 0.01 \approx 10 \text{ mm}^{-1}$ is a sum of the scattering and absorption coefficients $\mu_s$ and $\mu_a$, and $L$ is the thickness of the turbid layer. In contrast, the fluence rate of the diffuse light is characterized by $\exp(-\mu_{\text{eff}} L)$, where the effective attenuation coefficient $\mu_{\text{eff}} = \sqrt{3} \mu_s (\mu_a + \mu'_s)$, the reduced scattering coefficient $\mu'_s = \mu_s (1 - g)$, $g$ is the scattering anisotropic factor of a scattering medium, and $\rho$ is the distance between the observation point and the source point. The fluence rate at the middle plane of a diffuse layer, in which the ultrasonic focus modulates the diffuse light, is proportional to $\exp(-\mu_{\text{eff}} L / 2)$. The modulated light is multiply scattered, and the diffused of modulated light can again be described by the diffusion theory, which leads to another decay factor $\exp(-\mu_{\text{eff}} L / 2)$. Finally, the fluence rate of the transmitted modulated light is proportional to $\exp(-\mu_{\text{eff}} L)$. In the time-reversal phase of TRUE optical focusing, the optical absorption from the medium surface to the virtual source and the following random scattering from the virtual source to the opposite surface further attenuate the TRUE signal. The experimentally measured TRUE signal has a decay rate of 0.32 mm$^{-1}$, which is greater than $\mu_{\text{eff}} = 0.20 \text{ mm}^{-1}$.

### 3.2 Focusing Into an Optical Thickness of 37.5

The first phantom [Figs. 4(a) and 4(b)] was 7.5-mm thick, with a scattering coefficient $\mu_s = 5 \text{ mm}^{-1}$ at 532 nm, giving an optical thickness of 37.5. Again, the scattering anisotropy is $g = 0.9$. Two absorption inclusions (Obj 1 and 2) measuring $1.5 \times 6.0 \times 0.8 \text{ mm}$ along their XYZ-axes, were embedded in the middle. These inclusions were made of the same material as the background, except that they were dyed with India ink to provide an optical absorption contrast ($\mu_a = 1.17 \text{ mm}^{-1}$). Two ultrasound transducers were used: one with a 3.5 MHz central frequency (Panametrics A381S, focal length $F = 38 \text{ mm}$, aperture size $D = 19 \text{ mm}$, and focal width $w = 0.87 \text{ mm}$), and the other one with a 1.0 MHz (Panametrics A302S, focal length $F = 41 \text{ mm}$, aperture size $D = 25 \text{ mm}$, and focal width $w = 2.49 \text{ mm}$). There exists a relation, $w = c F f_d D$, where $c$ is the speed of sound in soft tissue. During the experiment, the phantom was scanned along the $x$ axis with respect to stationary light and ultrasound beams. At each position, both the TRUE signal (collected by PD1) and the traditional ultrasound-modulated optical tomography (UOT) signal (collected by PD2) were recorded, from which one-dimensional (1D) TRUE and UOT images were shown as a function of the phantom position [Figs. 4(c) and 4(d)]. In this study, the laser output was 1.20 W, and the ultrasonic pressures were 0.70 MPa at the 3.5 MHz ultrasonic focus, and 0.33 MPa at the 1.0 MHz ultrasonic focus.

As shown in Fig. 4(c), both the TRUE and UOT images can distinguish the two objects from the background, and the TRUE image concords with the UOT image. The resolutions of the TRUE and UOT images—defined as the full widths at half maximum (FWHMs) of the approximated Gaussian profiles of the 3.5 MHz transducer—were 0.63 and 0.88 mm, respectively. Because of the square law, the ratio between the resolutions of the UOT and TRUE images with the same transducer is $\sqrt{2}$. The square relation shows that light can be focused back into a scattering medium with an optical thickness of 37.5, i.e., an equivalent thickness of 3.75 mm in tissue. Figure 4(d) shows the comparison of the normalized TRUE images obtained with a 3.5 MHz transducer (represented by black crosses and solid...
3.3 Focusing Into an Optical Thickness of 50

To focus into a thicker scattering sample, in addition to increasing the laser output to 1.80 W, a more efficient ultrasonic encoding was applied by using a 2.0 MHz HIFU transducer (Sonic H-148, focal length \( F = 63 \) mm, aperture size \( D = 64 \) mm, and focal width \( w = 0.70 \) mm). Optimized pressure at the ultrasonic focus was 1.44 MPa. Figure 5 shows the results acquired from a 5-mm thick phantom, whose scattering coefficient \( \mu_s = 10 \) mm\(^{-1} \) and optical thickness was 50, equivalent to a 5 mm thick tissue. Three inclusions—Obj 1 and 2 (absorbing), and Obj 3 (scattering)—were embedded in the middle plane of the phantom as shown in Fig. 5(a).

In Fig. 5(b), the blue dots (experimental data) and solid line (Gaussian fit) represent the TRUE image with the 2.0 MHz transducer. As we can see, the experimental data and the Gaussian fit agree quite well \((R^2 = 0.90)\), giving an imaging spatial resolution (FWHM) of 0.50 mm, which equals the value of the 2.0 MHz transducer focal width \((0.70 \) mm). The imaging results verified that light was focused into the tissue-mimicking phantom at a depth of 2.5 mm, and the focus was determined by the focal region of the 2.0 MHz transducer.

3.4 Focusing Into a Phantom With an Optical Thickness of 70

Based on the current setup, the maximum obtained TRUE focusing optical thickness was 70, i.e., an equivalent 7 mm tissue thickness, and the results are shown in Fig. 6. The agreement between experimental data and the fitted curve, despite the relatively low signal-to-noise ratio (SNR) as indicated by an \( R^2 \) of...
paraxial regime. Therefore, the fidelity of OPC is restricted by (PCM), a phase-reversed copy can be achieved only within an effective response area and angle of a phase conjugate mirror required for accurate OPC. In practice, however, considering the thermal vibration and physiological motions, first is inhomogeneity, such as direction-oriented muscle fibers, cartilages, and blood vessels, which may reduce the ultrasonic tagging efficiency and dampen TRUE focusing. Second is the stability of tissue microstructure, which is essential for time reversal. However, the physiological motion and thermal vibration of scatterers, which can be reinforced by acoustic and optical energy deposition, gradually distorts the optical train and finally breaks the reversibility for time reversal. In experiments, we found that TRUE signals actually decreased beyond certain values of ultrasonic pressure and laser output. Hence, an efficient way to focus into thick biological tissue is using a large area of photorefractive material with fast response, to accomplish writing and reading within tissue speckle de-correlation time, which is on a millisecond scale because of the inherent thermal vibration and physiological motions.

For therapeutic purposes and high SNR probes, an intense fluence rate within the ultrasonic focus is demanded. But, for the dynamic holographic material we used, the energy gain of time reversed focal light was smaller than unity, since the hologram was erased in the reading procedure. However, its intensity gain was enhanced with an intense reading beam at the expense of a shortened time in reading. In some materials, holograms can be fixed by heating or an external electric field, and there is no restriction on intensity gain and energy gain in playing back fixed holograms. Numerous photons can be focused into the turbid media to interact with and even burn particles, cells, and clusters within the focus. Besides hologram fixing, nondestructive read-out of holograms can also be realized by the two-photon storage technique for fast response.

5 Conclusions

In this study, by using an EOM to switch light between recording and reading, as well as using lower frequency ultrasound waves, we increased the TRUE focusing thickness stepwise from 2.5 to 3.75 and 7.0 transport mean free paths, which are equal to the mean free path divided by \((1 - g)\). We also demonstrated that the focal region, determined by focused ultrasonic wave, was scalable with the focused ultrasonic region. In summary, the utilization of TRUE focusing allows us to dynamically deliver diffused light to an arbitrary spot inside a turbid medium to manipulate light-matter interaction and see into the turbid medium.

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References