Nonlinear optics in all-dielectric nanoantennas and metasurfaces: a review

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Abstract. Free from phase-matching constraints, plasmonic metasurfaces have contributed significantly to the control of optical nonlinearity and enhancement of nonlinear generation efficiency by engineering subwavelength meta-atoms. However, high dissipative losses and inevitable thermal heating limit their applicability in nonlinear nanophotonics. All-dielectric metasurfaces, supporting both electric and magnetic Mie-type resonances in their nanostructures, have appeared as a promising alternative to nonlinear plasmonics. High-index dielectric nanostructures, allowing additional magnetic resonances, can induce magnetic nonlinear effects, which, along with electric nonlinearities, increase the nonlinear conversion efficiency. In addition, low dissipative losses and high damage thresholds provide an extra degree of freedom for operating at high pump intensities, resulting in a considerable enhancement of the nonlinear processes. We discuss the current state of the art in the intensely developing area of all-dielectric nonlinear nanostructures and metasurfaces, including the role of Mie modes, Fano resonances, and anapole moments for harmonic generation, wave mixing, and ultrafast optical switching. Furthermore, we review the recent progress in the nonlinear phase and wavefront control using all-dielectric metasurfaces. We discuss techniques to realize all-dielectric metasurfaces for multifunctional applications and generation of second-order nonlinear processes from complementary metal–oxide–semiconductor-compatible materials.

Keywords: nonlinear optics; dielectric metasurfaces; Mie modes; Fano resonances; anapole modes; harmonic generation.

Received Dec. 21, 2018; accepted for publication Mar. 5, 2019; published online Apr. 3, 2019.

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[DOI: 10.1117/1.AP.1.2.024002]

1 Introduction

Nonlinear effects in electricity and magnetism have been recognized since Maxwell’s time. However, much progress has been made in the field of nonlinear optics since the discovery of the laser, which made high-intensity optical fields easily feasible. The field started to grow with the first experimental work of Franken et al. on optical second-harmonic generation (SHG) in 1961 and the theoretical work of Bloembergen et al. on optical wave mixing in 1962. Over the following decades, the field of nonlinear optics witnessed enormous growth, leading to the observation of new physical phenomena and giving rise to novel concepts and applications including high-harmonics generation and frequency mixing that can act as new light sources or as amplification schemes, light modulators for controlling the phase or amplitude of a light beam, optical switches, optical logic, optical limiters, and numerous ways of processing the information content of data images, which created revolutionary change in photonics technology in the 20th century. Almost all those achievements were made on conventional bulk crystals where cumbersome phase-matching conditions limit the efficiency of the nonlinear processes.

The current research trend in nonlinear optics has moved toward miniaturized optical materials in truly compact setups. In recent years, significant advancements in nanofabrication techniques have considerably broadened the experimental and theoretical framework in which nonlinear optical processes are explored. Major work over the past decade has been done in design and fabrication to simultaneously address the efficiency and phase matching in nonlinear generation within the subwavelength regime. Metamaterials and their two-dimensional counterparts, metasurfaces, are of great promise for efficient nonlinear generation of new waves. Metasurfaces can exhibit strong nonlinear optical responses compared to three-dimensional (3-D) structures because of...
the relaxation or complete overcoming of the phase-matching requirement.

Free from phase-matching limitations and featuring a unique control over nonlinear fields, plasmonic metasurfaces have been employed to the fullest extent for the generation of high-harmonics, frequency mixing, and other nonlinear effects.\textsuperscript{10,11,16–22} In the case of nonlinear plasmonics, the efficiency of the nonlinear optical processes is determined not only by the quality of the phase matching between the interacting optical beams but also by the degree of confinement and overlap between the optical near-field and the nonlinear optical structures with subwavelength features.\textsuperscript{11,18,23–25} Plasmonic materials are most commonly made of metals at the nanoscale. Metal nanostructures (nanoantennas) are variously shaped objects, with a size as small as few tens of nanometers, typically made of noble metals, such as gold and silver. Nanostructures supporting surface plasmon polariton resonances that provide both electric field enhancement and spatial confinement enable the generation of pronounced nonlinear optical effects at relatively low excitation powers even though the interaction volume may be very small. Plasmonic metasurfaces allow a large degree of control of the optical nonlinearity by engineering subwavelength meta-atoms, thereby enhancing the nonlinear generation efficiency, which has been observed during the past decade.\textsuperscript{16–18,26–24} However, second-order nonlinear processes, such as SHG, cannot be achieved from a metasurface having centrosymmetric modes at both fundamental and generated frequencies. Second-order processes from metal nanostructures originate from two contributions, the bulk and the surface. In noble metal, the local-bulk source is absent because of the material’s centrosymmetry, and only the nonlocal-bulk contribution needs to be considered.\textsuperscript{32} On the contrary, the local-surface contribution is allowed due to the symmetry breaking at the interface with the embedding medium.\textsuperscript{36,37} The magnitudes of the nonlocal-bulk and -surface contributions depend on the shape of the nanoparticle and on the optical properties of the metal at the fundamental and second-harmonic frequencies.\textsuperscript{3–41} Metasurfaces enabling SHG have been constructed by choosing specific geometries of the meta-atoms, such as L-shaped\textsuperscript{42–47} and G-shaped antennas,\textsuperscript{48–52} split-ring resonators,\textsuperscript{27,53–58} asymmetric dimmers,\textsuperscript{59,60} dielectric-loaded plasmonic 3-D structures,\textsuperscript{61} and multiresonant antennas,\textsuperscript{32–40} where the inversion symmetry is absent. Plasmonic metasurfaces have been employed for other second-order processes like sum-frequency generation (SFG)\textsuperscript{66,67} and difference-frequency generation (DFG),\textsuperscript{58–70} In contrast, third-order nonlinear effects, such as the Kerr effect,\textsuperscript{71–73} third-harmonic generation (THG),\textsuperscript{29,31,74–77} and four-wave mixing (FWM),\textsuperscript{23,25,78–83} are free from symmetry considerations for linear polarized light. In addition, high-harmonic generation\textsuperscript{84} and supercontinuum white-light generation\textsuperscript{85} have also been realized using plasmonic nanostructures.

Metasurface can locally control the phase, amplitude, or the polarization state of light waves that propagate through or reflect from them. The concept of phase tailoring plasmonic metasurfaces at a nonlinear regime enables both the coherent generation and the manipulation, such as beam steering and lensing of light beams. Nonlinear phase control has been demonstrated for SHG, THG, and FWM in metallic thin films.\textsuperscript{24,25,85} Recently, a plasmonic metasurface hologram has been realized at the THG frequency.\textsuperscript{31} In addition, nonlinear holography has been demonstrated to be operated at both fundamental and second-harmonic frequencies using a Pancharatnam–Berry (PB) phase change, which operates in both the linear and the nonlinear optical regimes simultaneously.\textsuperscript{27}

So far, we have seen that surface plasmon polaritons are capable of enhancing and spatially confining optical fields beyond the diffraction limit. Plasmonic effects in metallic nanostructures have been extensively used to enhance and control nonlinear optical processes at the nanoscale, such as harmonic generation, wave mixing, supercontinuum generation, nonlinear imaging, and holography. However, several disadvantages limit their applicability in nonlinear nanophotonic applications, including high dissipative losses and inevitable thermal heating, leading to low optical damage thresholds. Thus, the use of all-dielectric metasurfaces supporting magnetic resonances, and the ability to withstand much higher pump field intensities, would be a promising route to obtaining higher nonlinear conversion efficiencies.\textsuperscript{86} Furthermore, it has been discovered that highly efficient and flexible light manipulation can be achieved at the nanoscale by tuning the electric and magnetic responses of all-dielectric nanostructures.\textsuperscript{16,87–89} The electric field confinement in dielectric nanoresonators is not limited to the surface only; the additional volume resonance can be added to make the overall enhancement larger.

In this review, we highlight recent progress in the field of nonlinear optical processes with all-dielectric nanosystems, from nonlinear frequency generation and phase control to applications. The review is organized as follows. In Sec. 2, we discuss the existence of different resonant modes inside a dielectric nanostructure. In Secs. 3 and 4, we review the nonlinear effects based on third- and second-order optical nonlinearities. Section 5 aims to give insight regarding nonlinear switching. Finally, in Sec. 6, we provide an outlook on future directions in this field.

There are many publications available on nonlinear optical effects in artificial materials including epsilon-near-zero materials, perovskites, two-dimensional materials, and multiple quantum wells. A detailed overview of these topics is well beyond the scope of this review. For a detailed and complete survey, we refer readers to a well-known review paper on these topics.\textsuperscript{16}

### 2 Multipolar Resonances in All-Dielectric Systems

In this section, we discuss the different modes that are available in all-dielectric nanostructures and their dependence on geometry, which is responsible for nonlinear field enhancement. The optical response of spherically symmetric scatterers, irrespective of their size and constituting medium, can be analytically predicted by expanding the electromagnetic fields in the multipolar basis. This is commonly known as the Lorenz–Mie theory.\textsuperscript{30} For lossless and nonmagnetic materials, their scattering properties can be fully determined when two parameters are specified: the permittivity ε and a size parameter s, which is defined as the proportional ratio between the nanoparticle radius R and the wavelength of light λ, s = 2πR/λ.\textsuperscript{32} In the case of subwavelength spherical plasmonic scatterers (s < 1), only electric-type resonances can usually be excited and the magnetic response is negligible as the field inside the sphere vanishes; whereas high-refractive-index dielectric scatterers exhibit both magnetic and electric type resonances, known as Mie resonances.\textsuperscript{28,90} The resonant magnetic dipole moments originate from the coupling of incident light to circular displacement current of the electric field, due to the field penetration and phase retardation inside
the particle. The magnetic resonance appears when the wavelength inside the particle becomes comparable to its spatial dimension: \(2R \approx \frac{\lambda}{n} \), where \(n\) is the refractive index of nanoparticle material, \(R\) is the nanoparticle radius, and \(\lambda\) is the light’s wavelength. Mie-type resonant behavior is not just specific to spherical scatterers. Nonspherical scatterers, such as nanocubes,\(^{92}\) spheroids,\(^{93,94}\) disks and cylinders,\(^{95}\) rings,\(^{96}\) and many other geometries\(^{97}\) have also been shown to support electric and magnetic Mie resonances. This gives the freedom to design various all-dielectric nanostructures with a desirable range of input wavelengths, to achieve resonant conditions. Figure 1(a) shows a schematic representation of charge–current distributions of the four major resonant modes in high-index dielectric particles (magnetic dipole, electric dipole, magnetic quadrupole, and electric quadrupole).\(^{98}\) A positive charge (such as a proton) and a negative charge (such as an electron) form an electric dipole, but they are not assumed to be in motion relative to each other, whereas a magnetic dipole, generally a tiny magnet of microscopic to subatomic dimensions, is equivalent to a flow of electric charge around a loop.\(^{100}\) Electrons circulating around atomic nuclei, electrons spinning on their axes, and rotating positively charged atomic nuclei—all are magnetic dipoles. An elementary electric quadrupole can be represented as two dipoles oriented antiparallel. Both the monopole moment (total charge) and dipole moment for this configuration are zero, but there exists a nonzero quadrupole moment. Likewise, a magnetic quadrupole can be realized by employing two pairs of identical current loops, such that the dipole moments of both the loops in each pair are antiparallel while the pairs are perpendicular to each other. Such a configuration cancels

Fig. 1 Mie resonances in dielectric nanostructures. (a) Schematic illustration of the charge–current distributions that give rise to the electric dipole \((p)\), magnetic dipole \((m)\), electric quadrupole \(\left(Q^e\right)\), and magnetic quadrupole \(\left(Q^m\right)\) (Ref. 98). (b) The simulated multipolar decomposition of the scattering cross section of an individual silicon nanodisk with height \(h = 660\) nm and diameter \(d = 660\) nm in air (Ref. 99). (c) SEM image of one of the fabricated silicon disk arrays (Ref. 99). (d)–(f) Dark-field optical microscope images (top left), SEM images (top right), and dark-field scattering spectra (bottom) of spherical silicon (Si) nanoparticles with approximate diameters of (d) 100 nm, (e) 140 nm, and (f) 180 nm (Ref. 87). Figure reprinted with permission: (a) Ref. 98, © 2014 by the American Physical Society (APS); (b) and (c) Ref. 99, © 2016 by the Nature Publishing Group (NPG); (d)–(f) Ref. 87, © 2012 by NPG.
the dipole moment and gives a quadrupole moment. Figure 1(b) illustrates the spectral position of the corresponding modes for a silicon nanodisk with a height of 660 nm and a diameter of 660 nm in air [see the scanning electron microscopy (SEM) image in Fig. 1(c)]. The resonant behavior of subwavelength high-refractive-index structures in the visible and near-IR region was first experimentally demonstrated while studying the optical response of silicon nanowires. Later, it was demonstrated that silicon nanospheres with sizes ranging from 100 to 300 nm support strong magnetic and electric dipole resonances in the visible and near-IR spectral range, as shown in Figs. 1(d)–1(f).

Mie resonators featuring both electric and magnetic responses are seen as a promising platform capable of leading to a practical realization of the Kerker conditions (suppression of the back-scattered field under given conditions) with nonmagnetic materials. An experimental verification of this effect in high-refractive-index particles was carried out in the microwave range and subsequently observed in the visible range with silicon and gallium arsenide (GaAs) nanoparticles, where the Kerker effect was due to the interference between the fields radiated by the induced electric and magnetic dipoles. It has been shown that a generalization of this effect to higher-order multipoles is also possible.

For metallic nanoantennas, the electric dipole modes usually dominate the Mie scattering. In contrast to plasmonics, strong localization of electric and magnetic fields at the nanoscale due to Mie resonances inside dielectric nanoparticles enhances nonlinear effects. It has been acknowledged that the intrinsic microscopic nonlinear electric polarizability of resonant nanoparticles may induce magnetic nonlinear effects. The presence of both electric and magnetic nonlinearities enhances the interference effects, which in turn increase the efficiency and control the polarization of the nonlinear processes, as well.

Another important resonance mode that can be achieved in dielectric nanostructures possessing more complex design is the Fano resonance. The Fano resonance is considered as an asymmetric lineshape of resonances, which arises from an interference of discrete (resonance) states with broadband (continuum) states. To observe Fano resonance from all-dielectric nanoparticles/metasurfaces, one of the important concepts is to include interaction between resonant (bright) and nonresonant

![Figure 2](https://www.spiedigitallibrary.org/journals/Advanced-Photonics/024002--4-Mar-Apr-2019-Vol.1(2)/terms-of-use)

**Fig. 2** Fano resonances and AMs in dielectric nanostructures. (a) Schematic illustration of the interference between the bright- and the dark-mode resonators, (b) corresponding SEM image of a single-unit cell of the fabricated metasurface, and (c) corresponding experimental transmittance (T), reflectance (R), and absorption (A) spectra, showing a Fano-type resonance (Ref. 114). (d) Schematic illustration of an anapole excitation: the toroidal dipole moment is associated with the circulating magnetic field M accompanied by electric poloidal current distribution. As the symmetries of the radiation patterns of the electric P and toroidal T dipole modes are similar, they can destructively interfere, leading to total scattering cancelation in the far-field with nonzero near-field excitation (Ref. 115). (e) Calculated spherical electric dipole (black), Cartesian electric (red) and toroidal (green) dipole moments contribution to the scattering by a dielectric spherical particle of refractive index n = 4 and wavelength 550 nm, as a function of the diameter. The anapole excitation is associated with the vanishing of the spherical electric dipole when the Cartesian electric and toroidal dipoles cancel each other (Ref. 115). Figure reprinted with permission: (a)–(c) Ref. 114, © 2014 by NPG; (d) and (e) Ref. 115, © 2015 by NPG.
(dark) scattering modes [Figs. 2(a) and 2(b)],\textsuperscript{114} which can be recognized as a nonsymmetrical dip in the scattering spectrum [Fig. 2(c)].\textsuperscript{114} Boosting the near field of the resonant nanoparticle at the Fano frequency is considered an important approach to increase nonlinear light–matter interaction. In addition to a strong local field enhancement, the Fano resonance allows controlling the radiative damping of the resonant modes. Besides the electric type of the Fano resonance, all-dielectric nanostructures exhibit a similar magnetic one, related to the optically induced magnetic dipole mode of the individual high-index nanoparticles. This is an additional degree of freedom to manipulate the magnetic resonances of dielectric nanostructures to enhance the nonlinear interaction.

High-index dielectric nanoparticles also support other unusual electromagnetic scattering modes such as anapole modes (AMs).\textsuperscript{115–117} Anapoles are characterized by a specific configuration of excited fields inside a system. When the toroidal and electric dipole modes spectrally overlap, they produce almost equivalent radiation patterns in the far field but with opposite phases, generating a pronounced dip in the spectrum [Fig. 1(e)].\textsuperscript{115} with nonvanishing near-field.\textsuperscript{116,117} The lack of scattering and radiation loss in a dipole channel can further enhance the local fields, boosting nonlinear effects. The recent development of all-dielectric nonlinear nanostructures that can show comparable electric and magnetic multipolar contributions has led to advances in the emerging field of multipolar nonlinear nanophotonics.

### 3 Third-Order Nonlinear All-Dielectric Nanostructures and Metasurfaces

A wide range of theoretical and experimental studies of nonlinear plasmonics have already laid the foundation of modern nonlinear optics with nanostructures. However, all-dielectric arrangements can support even stronger nonlinear optical responses as well as novel functionalities enabled by signified magnetic dipole and higher-order Mie-type resonances, compared to their plasmonic counterparts. In this section, we present an overview of the state-of-the-art progress in the area of nonlinear interactions of high-index dielectric nanostructures and metasurfaces, supporting additional magnetic resonances. In addition, dielectric nanostructures are able to withstand much higher pump fields, making them a promising way to obtain higher nonlinear conversion efficiencies.\textsuperscript{89,90,120} The electric field enhancement in dielectric nanostructures is typically smaller than in the plasmonic ones; however, additional volume resonance can be added to make the overall enhancement larger, as the field confinement in dielectric nanostructures is not restricted to the surface only, as in their metallic counterparts.

Shcherbakov et al.\textsuperscript{121} demonstrated a strong nonlinear response from dielectric nanostructures made of silicon nanodisks. They exhibited enhanced THG, which was observed by the naked eye using both an isolated nanodisk and an array of nanodisks, which were optically pumped in the vicinity of the magnetic dipole resonance, as shown in Figs. 3(a) and 3(b).\textsuperscript{121} The nanodisks were fabricated using a silicon-on-insulator wafer and exhibited both electric and magnetic dipole resonances, for which the silicon metasurface generated up to 4-nW THG power for a pump power of 30 mW (peak pump intensity 5.5 GW cm\textsuperscript{−2}). The resulting conversion efficiency of 0.9 × 10\textsuperscript{−7} [Fig. 3(b)]\textsuperscript{121} was fundamentally limited by free carriers generated via two-photon absorption in the bulk Si substrate, which leads to free-carrier absorption of the pump beam.

THG from a Fano nonlinear metasurface consisting of resonant Si nanodisks and nanoslits, supporting resonant dark (magnetic dipole) and bright (electric dipole) modes, respectively, was demonstrated by Yang et al.\textsuperscript{122} The nanostructures were fabricated by electron beam lithography followed by reactive-ion etching after depositing a 120-nm-thick poly-Si layer on a quartz substrate. The measured conversion efficiency was 1.2 × 10\textsuperscript{−6} with an average pump power of 50 mW at a peak pump intensity of 3.2 GW cm\textsuperscript{−2} [Fig. 3(c)].\textsuperscript{122} The enhanced nonlinearity arose from high-quality factor Fano resonance that in turn strongly enhanced the local electric field within the Si, thus resulting in a large effective third-order nonlinearity. Fano resonances can also be excited from nanodisks only by using different lattice arrangements. A square array of symmetric clusters of four Si nanodisks, forming quadrumers, exhibited multifold enhancement of the THG signal, excited by an oblique plane wave.\textsuperscript{123} The origin of the Fano resonance in Si nanodisk quadrumers is the destructive interference between the coupled magnetic-like modes formed by out-of-plane magnetic dipoles and circulating displacement current produced by in-plane electric dipoles in the far field. In addition, the Fano-assisted THG in Si nanodisk trimers has been demonstrated.\textsuperscript{124} Another example of enhanced THG in a Fano-resonant silicon metasurface due to the trapped mode supported by the high quality factor was demonstrated by Tong et al.\textsuperscript{125} The conversion efficiency was enhanced by about 300 times with respect to the bulk silicon slab, which depended on both the wavelength and the polarization angle of the pump light.

Germanium (Ge) is another excellent material for nonlinear metasurfaces, because of its high refractive index in the visible range and large third-order susceptibility. THG in thin Ge nanodisks under normally incident laser excitation can be boosted via a nonradiative AM. Grinblat et al.\textsuperscript{126} demonstrated strong THG by exciting a Ge nanodisk near the AM [Fig. 3(d)], and the measured TH intensity was about one order of magnitude larger than the corresponding signal for the excitation of the dipolar resonances, at which the field was poorly confined within the dielectric material. The observed conversion efficiency was \textapprox 10\textsuperscript{−4} upon 1 μW (15 GW cm\textsuperscript{−2}) pump power. Later the same group demonstrated THG using higher-order AMs\textsuperscript{128} and FWM using high-order modes (HOMs)\textsuperscript{129} that do not show anapole characteristics. In the case of FWM, when the two excitation wavelengths were chosen with two different HOMs and when the near-field intensity overlap between those modes was about 80% within the disk, the FWM signals were found to be >30% lower in intensity compared to the THG of the individual pump wavelengths [Fig. 3(e)].\textsuperscript{129} However, when the two different pump wavelengths covered a single HOM, the degenerated FWM signals were observed to decrease by only ~10% in intensity with respect to the THG process, indicating nearly equivalent efficiency [Fig. 3(f)].\textsuperscript{129}

Very recently, Wang et al.\textsuperscript{130} demonstrated a new concept for embedding any functionality into a nonlinear all-dielectric...
metasurface made of silicon, producing phase gradients over a full 0- to 2-π phase range based on the generalized Huygens’s principle that was extended to nonlinear optics. Efficient wavefront control of a third-harmonic field along with the generation of nonlinear beams at a designed angle and the generation of nonlinear focusing vortex beams were shown in that work (Fig. 4).130

So far, we have seen that the choice of the appropriate confined optical mode and mode overlap (in the case of wave mixing) are the two utmost important factors to get maximum conversion efficiency. These investigations reveal useful pathways for the further optimization of third-order optical processes in all-dielectric nanostructures.

4 Second-Order Nonlinear All-Dielectric Nanostructures and Metasurfaces

In Sec. 3, we have shown that Si and Ge nanostructures and metasurfaces can be utilized to enhance the third-order nonlinearities. However, Si and Ge do not possess bulk-mediated second-order nonlinearities due to their centrosymmetric crystal structure. To overcome this limitation, nanostructures made...
out of III–V semiconductors that possess a high-dielectric index and relatively large second-order susceptibilities have been used. Resonantly enhanced SHG using GaAs-based dielectric metasurfaces, made of arrays of cylindrical resonators, has demonstrated SHG enhancement factors as large as $10^4$ compared to...
The SHG measurements were performed in reflection geometry because the SHG wavelengths were above the bandgap of GaAs so that the second-harmonic signal in the transmission direction would have been completely absorbed by the GaAs substrate. The strongest SHG effect was observed when pumped at the magnetic dipole resonance, at which the absolute nonlinear conversion efficiency reaches \( \sim 2 \times 10^{-5} \) with \( \sim 3.4 \text{ GW cm}^{-2} \text{ pump intensity} \), as shown in Fig. 5(a).\textsuperscript{132} Interestingly, the demonstrated conversion efficiency at the magnetic dipole resonance was about \( \sim 100 \) times higher than the conversion efficiency at the electric dipole resonance, which was caused by increased absorption of GaAs at the shorter wavelength of the electric dipole resonance.

Recently, the same group demonstrated a GaAs metasurface-based optical frequency mixer [Fig. 5(b)] that concurrently generates 11 new frequencies spanning the UV to near-IR.\textsuperscript{133} The even and odd higher-order nonlinearities of GaAs enabled the observation of SHG, THG, and fourth-harmonic generation (FHG), SFG, two-photon absorption-induced photoluminescence (TPA-PL), FWM, and six-wave mixing (SWM), as shown in Fig. 5(c).\textsuperscript{133} The resonantly enhanced frequency mixing was achieved by simultaneously exciting the lowest order magnetic and electric dipole Mie resonances of a GaAs nanocylinder. The simultaneous occurrence of these seven nonlinear processes is assisted by the combined effects of strong intrinsic material nonlinearities, enhanced electromagnetic fields, and relaxed phase-matching requirements. The results illustrate that metasurfaces can be a versatile system for achieving multiple nonlinear processes with equal contributions simultaneously.

**Fig. 5** Second-order nonlinear effects at GaAs metasurfaces. (a) SHG power dependence at low pump intensities, and the deviation from the quadratic relationship at higher pump intensities due to the damage of GaAs resonators. Left inset: SEM image of the fabricated GaAs resonator array. Right inset: SHG conversion efficiency as a function of pump power (Ref. 132). (b) Schematic illustration of an optical metamixer consisting of a square array of subwavelength GaAs dielectric resonators. Two femtosecond near-IR pulses pump the metamixer and a variety of new frequencies are simultaneously generated. Top inset: SEM image of the GaAs metamixer (scale bar 3 \( \mu \text{m} \)). Bottom inset: energy diagrams of the seven nonlinear optical processes that occur simultaneously at the metasurface: SHG, THG, FHG, SFG, TPA-PL, FWM, and SWM (Ref. 133). (c) Measured nonlinear spectrum exhibiting 11 generated peaks originating from seven different nonlinear processes when two optical beams at \( \lambda_2 \sim 1.24 \mu \text{m} \) and \( \lambda_1 \sim 1.57 \mu \text{m} \) are used to simultaneously pump the GaAs metasurface. Blue labels indicate harmonic-generation processes and photoluminescence arising from two-photon absorption that each requires only one pump beam. Red labels indicate frequency mixing that involves both pump beams (Ref. 133). Figure reprinted with permission: (a) Ref. 132, © 2016 by ACS; (b) and (c) Ref. 133, © 2018 by NPG.
By shaping the unidirectional SHG radiation pattern from aluminum gallium arsenide (AlGaAs) nanodisk antennas as well as its polarization state, generation of cylindrical vector beams of complex polarization has been experimentally demonstrated. In these experiments, nonlinear conversion efficiencies exceeding $10^{-4}$ have been achieved. In another work, SHG from monolithic AlGaAs optical nanoantennas of optimized geometry, excited by a magnetic dipole resonance at the wavelength of 1550 nm, has been measured, revealing a peak conversion efficiency exceeding $10^{-5}$ at 1.6 GW cm$^{-2}$ pump intensity.

In an unconventional way, Bar-David and Levy recently reported the generation of second-harmonic signal from an amorphous silicon metasurface. The second-harmonic signal was generated mostly from the surface, following selection rules that rely on the asymmetry of the meta-atoms.

The superiority of the fabricated materials is utmost important to get efficient nonlinear phenomena. Fabrication of the dielectric metasurfaces of nonzero second-order bulk susceptibility requires special attention to maintaining their high quality, as they are made of III–V semiconductor nanostreams. In this context, widegap materials, such as ZnO, GaN, or LiNbO$_3$, allowing even lower losses at shorter wavelengths, can be an alternative as second-order materials to realize highly nonlinear all-dielectric metasurfaces.

The high-index dielectric metasurfaces provide strong nonlinear response, low dissipative losses, and high damage thresholds. These advantages make them a powerful platform for modern nonlinear nanophotonics. The presence of both the electric and the magnetic responses makes it possible to tune the scattering patterns and design switchable flat optical devices engaging these nonlinearities.

### 5 All-Dielectric Ultrafast Optical Switching

One of the biggest advantages of metasurfaces is their ability to spatially vary and tune the optical parameters of the surface. Such spatial variations enable new opportunities for the observed ultrafast optical switching, namely to construct ultrafast displays that can switch between two or more different images at the femtosecond timescale. Ultrafast optical switching that is based on the free-carrier nonlinearity in semiconductors suffers from long switching time (limited to tens of picoseconds) due to two-photon absorption and comparatively large free-carrier lifetime. In the past decade, plasmonic metasurfaces have provided important progress on optical ultrafast switching based on strong light localization within subwavelength mode volume, which in turn increased the third-order nonlinearity, resulting in a change of the complex refractive index of the material. However, optical loss and heating effects in plasmonic nanoantennas limit device performance. In this context, high-permittivity all-dielectric metasurfaces can be a promising alternative. In this section, we discuss the recent progress of ultrafast switching effects using all-dielectric metasurface. Makarov et al. presented an approach for efficient tuning of optical properties of a high-refractive-index subwavelength nanoparticle. The nanoparticles showed a magnetic Mie-type resonance that was shifted by femtosecond laser irradiation. The effect is based on an ultrafast photoionization of a dense ($>10^{20}$ cm$^{-3}$) electron–hole plasma within the nanoparticle, drastically changing its transient dielectric permittivity. The work experimentally demonstrated 20% switching of the reflection of a single silicon nanoparticle photoexcited by femtosecond laser pulses with a wavelength in the vicinity of the magnetic dipole resonance, enabling high-efficiency light manipulation on the subwavelength scale [Fig. 6(a)]. Later, the same group reported on the experimental observation of a ~2.5 ps operation regime of a nonlinear all-dielectric nanoantenna, which was an order of magnitude faster than their previous work. A corresponding theoretical study on silicon nanoparticle dimers for nonlinear optical tuning, enabled by photoexcitation of electron–hole plasma, was set forth in another work.

All-optical switching of femtosecond laser pulses passing through subwavelength silicon nanodisks at their magnetic dipole resonance was presented. Pump-probe measurements revealed that the switching of the nanodisks can be governed by bandwidth-limited 65-fs long two-photon absorption. The authors observed an improvement of the switching time by...
a factor of 80 with respect to the unstructured silicon film [Fig. 6(b)]. The undesirable free-carrier effects can be suppressed by proper spectral positioning of the magnetic resonance, making such a structure the fastest all-optical switch operating at the nanoscale.

All-dielectric metasurfaces, benefited from very low intrinsic losses and localized Mie-type modes, are promising for all-optical switching and modulation. Magnetic resonances in all-dielectric metasurfaces suppress the free-carrier effect, leading to greatly reduced all-optical switching time without suffering from a strong loss in modulation depth.

6 Summary and Outlook

We have reviewed the state of the art in the intensely developing area of all-dielectric nonlinear nanostructures and metasurfaces, as a promising alternative for nonlinear plasmonic metasurfaces. We have discussed the important role of the electric and magnetic dipoles and higher-order Mie modes, in harmonic generation, wave mixing, and ultrafast optical switching, including Fano resonances and anapole moments. Electric and magnetic resonances and their interference in high-index dielectric nanostructures strongly influence the enhancement of the nonlinear optical interactions. Although the electric field enhancement in dielectric nanostructures is smaller than in the plasmonic counterparts, the additional volume resonance, coming from the field confinement of the mode in the high-index resonators, can make the overall enhancement of the nonlinear process larger. High-index dielectric nanostructures and metasurfaces, supporting additional magnetic resonances, can induce magnetic nonlinear effects, which along with electric nonlinearities increase the nonlinear conversion efficiency.

Additionally, low dissipative losses and high damage thresholds of all-dielectric nanosystems provide an added degree of freedom in operating at high pump intensities, resulting in considerable enhancement of the nonlinear processes. In comparison to plasmonic nanostructures, this is a huge advantage as the loss and the thermal-heating effects are mostly undesired, and can easily lead, for metallic structures, to the destruction of the nanostructures.

Despite the tremendous progress in the enhancement of the nonlinear efficiency, much less advancement has been achieved in realizing functional nonlinear metasurface elements. Very few examples are available in the literature about nonlinear phase and wavefront control to show novel optical functionalities. The work by Wang et al. shows that a wavefront control of the third-harmonic field based on the generalized Huygens’ principle (which is extended to nonlinear optics) seems feasible. Using Huygens’ principle for nonlinear processes while keeping the nonlinear conversion efficiency high seems to be an important research angle for future improvements. Furthermore, the spatial control of the nonlinear phase of the THG signals depends sensitively on the precise geometry and refractive index of the nanostructures, resulting in challenging fabrication. Here, different concepts for the control of the nonlinear phase might bring further advantages. In this context, an elegant way to arbitrarily tailor the nonlinear phase would be based on the PB phase technique, which has been demonstrated for nonlinear effects at plasmonic metasurfaces. The PB phase manifests as an accumulated phase during the change of the polarization state of light, for example, if light with a particular polarization is scattered at a nanostructure. Because the PB phase depends solely on the elements’ orientation, it can be interpreted as being of geometrical nature and is often referred to as a geometrical phase. The concept was previously applied to encode phase information into planar flat surfaces with plasmonic nanostructures, giving rise to nonlinear optical holography, image generation, and beam profile manipulation. We note that the same symmetry selection rules for nonlinear processes as for plasmonic nanostructures are valid, resulting in symmetry-dependent nonlinear processes. By tailoring the rotation angle of each nanostructure, the angle will determine the local phase of the nonlinear material polarization. Hence, by using the control over the nonlinear PB phase, the local phase in the generation process can be controlled. This way, one can generate different nonlinear functional elements that rely on a space-dependent phase of the generated nonlinear signal. One important application of tailoring the nonlinear phase is nonlinear holography. In this context, two or more nonlinear processes can simultaneously be overlapped to create nonlinear holographic multiplexing with different frequencies.

Apart from the conventional selection of the second-order nonlinear materials, the fabrication of metasurfaces is rather complex, and another promising direction is to use complementary metal–oxide–semiconductor-compatible materials (such as Si, SiN, SiO2, and Ge) to realize second-order processes by breaking their local symmetry. Second-order nonlinear metasurfaces are required for important processes such as phase-only modulation, SFG, and DFG, besides SHG. Other than that, they might find important application in quantum nonlinear optics. The symmetry breaking might be possible by applying an external direct current (DC) field, similar to electric-field-induced SHG (EFISHG). In this process, the third-order nonlinear susceptibility is converted to a second-order susceptibility that can introduce a phase shift known as DC Kerr effect, an inherently phase-matched process. Recently, Timurdogan et al. demonstrated EFISHG along with the DC Kerr effect in integrated silicon ridge waveguides by breaking the crystalline symmetry of silicon through applying DC fields and inducing a second-order susceptibility proportional to the third-order susceptibility of silicon. The second-order originated from the large third-order of silicon combined with large electric fields generated within reverse-biased p−n junctions. To achieve an efficient EFISHG in silicon, the fundamental pump and signal modes were quasi-phase-matched with periodically patterned p−n junctions.

All-dielectric metasurfaces have a high potential for enabling the efficient generation of new frequencies by simultaneously using more than one nonlinear process. In such a way, one can construct holographic multiplexing elements based on frequency or polarization. Nonlinear all-dielectric nanosystems might also drive rapid progress in engineering nonlinear optical effects beyond the diffraction limit and have enormous potential to develop new concepts of miniaturized efficient nonlinear photonic metadevices in the near future.

Acknowledgments

This project received funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation program (Grant Agreement No. 724306) and the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) (No. 231447078-TRR142). The authors have no relevant financial interests in the manuscript and no other potential conflicts of interest.
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Sain, Meier, and Zentgraf: Nonlinear optics in all-dielectric nanoantennas and metasurfaces: a review

Mar/Apr 2019 • Vol. 1(2)


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