Optimizing the regularization for image reconstruction of cerebral diffuse optical tomography

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Abstract. Functional near-infrared spectroscopy (fNIRS) is an optical method for noninvasively determining brain activation by estimating changes in the absorption of near-infrared light. Diffuse optical tomography (DOT) extends fNIRS by applying overlapping "high density" measurements, and thus providing a three-dimensional imaging with an improved spatial resolution. Reconstructing brain activation images with DOT requires solving an underdetermined inverse problem with far more unknowns in the volume than in the surface measurements. All methods of solving this type of inverse problem rely on regularization and the choice of corresponding regularization or convergence criteria. While several regularization methods are available, it is unclear how well suited they are for cerebral functional DOT in a semi-infinite geometry. Furthermore, the regularization parameter is often chosen without an independent evaluation, and it may be tempting to choose the solution that matches a hypothesis and rejects the other. In this simulation study, we start out by demonstrating how the quality of cerebral DOT reconstructions is altered with the choice of the regularization parameter for different methods. To independently select the regularization parameter, we propose a cross-validation procedure which achieves a reconstruction quality close to the optimum. Additionally, we compare the outcome of seven different image reconstruction methods for cerebral functional DOT. The methods selected include reconstruction procedures that are already widely used for cerebral DOT [minimum \( \ell_2 \)-norm estimate (\( \ell_2 \)MNE) and truncated singular value decomposition], recently proposed sparse reconstruction algorithms [minimum \( \ell_1 \)- and a smooth minimum \( \ell_0 \)-norm estimate (\( \ell_1 \)MNE, \( \ell_0 \)MNE, respectively)] and a depth- and noise-weighted minimum norm (wMNE). Furthermore, we expand the range of algorithms for DOT by adapting two EEG-source localization algorithms [sparse basis field expansions and linearly constrained minimum variance (LCMV) beamforming]. Independent of the applied noise level, we find that the LCMV beamformer is best for single spot activations with perfect location and focality of the results, whereas the minimum \( \ell_1 \)-norm estimate succeeds with multiple targets. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: 10.1117/1.OE.53.9.106006]

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1 Introduction

Diffuse optical tomography (DOT) is a modality of near-infrared spectroscopy (NIRS) that provides three-dimensional (3-D) images of absorption changes in a semi-infinite volume. Recently, it has been applied in breast cancer imaging or optical mammography as well as in small animal imaging. The 3-D DOT has been proposed by various groups for imaging brain function.

Used as a brain-imaging tool, DOT measures the changes in near-infrared light absorption in the cortex. It allows the operator to determine what functional changes are evoked in cerebral oxygenated (HbO₂) and deoxygenated hemoglobin (HbR) concentration in the cerebral blood flow during local brain activation. Due to the wavelength-dependent light attenuation, DOT usually employs two different wavelengths, each of them more sensitive to one of the main chromophores HbO₂ and HbR.

Compared to fNIRS, DOT uses more light sources and detectors in a high-dense optical fiber grid, and allows many overlapping optical data channels with different source-detector distances to be recorded. Light, which is detected far away from the source, passes through the deeper tissue layers, allowing the separation of superficial layers from cerebral layers in a 3-D manner.

Recovering the absorption coefficient \( \mu_a \) inside the head from boundary measurements is a nonlinear problem, but it can be linearized if scattering \( (\mu_s) \) in the head is stable over time and the change in \( \mu_a \) is small (perturbation approach). For image recovery, light propagation in the examined tissue needs to be modeled first. In tissue, where scattering dominates absorption and the propagation of light is close to isotropic, the diffusion equation can be applied for modeling. After discretization of the scanned volume (e.g., as a finite-element (FE) mesh), wavelength-specific optical properties are assigned to the elements (mesh nodes), and light propagation is modeled with respect to the positions of the optical fibers on the surface. Solving the forward problem results in a weight matrix \( J \) that

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contains sensitivity values for all nodes in the reconstruction volume for all given light source and detector pairs.

Reconstruction of DOT images requires inverting the forward mapping \( J \). This is an under-determined and ill-posed problem, since countless distributions of \( \mu_a \) within the volume can explain the same surface measurement. Moreover, near-infrared light can pass skin and bone, but is highly attenuated with increasing depth, causing \( J \) to be ill-conditioned (or even singular), and the solution to the corresponding linear system to be prone to numerical instabilities. With a penetration depth of 3 to 4 cm, light can reach the cortex, but there is a vast sensitivity loss in the depth. This leads to a sparse matrix with very low sensitivity values in the largest fraction of the volume. Furthermore, small changes in optical properties at this depth have to be recovered from boundary measurements with nearby nodes that have a high sensitivity to superficial signals and are, therefore, sensitive to noise. Due to the ill-posed nature of the DOT inverse problem, a unique solution can only be obtained if the constraints are imposed on the distribution of the absorption coefficients. Moreover, since \( J \) is ill-conditioned, a solution has to be found that optimally suppresses noise while still explaining the data. Many studies using DOT either add an additional regularization term to the model or eliminate the singular values smaller than a defined threshold from \( J \). Both methods overcome the problem of very small singular values of \( J \) causing amplification of noise upon inversion. However, the choice of a regularization parameter (either the number of singular values maintained or the relative weight of the regularization term in the cost function) is often made ad hoc and lacks objective criteria. For researchers, it may be challenging to find an appropriate regularization parameter, since the measured data vary highly between the experiments, depending on the setup, imaging device, tissue properties, and noise level.

Besides the problem of regularization, the distributed source localization methods such as minimum \( \ell_2 \)-norm estimate (\( \ell_2 \)-MNE) and truncated singular value decomposition (tSVD) tend to yield blurry images rather than focused results. Therefore, a variety of sparse image reconstruction methods, such as \( \ell_p \)-norm-based algorithms with \( 0 \leq p \leq 1 \), have been introduced in optical imaging.

Other approaches to reconstruct the brain activation are provided by developments in electrophysiological dipole mapping. The inverse problem of electroencephalography (EEG) localizes the position of the active cerebral current source from the measured surface fields, and is comparable with the inverse problem of image reconstruction in DOT.

The aim of this work is twofold. First, we show how the reconstruction quality in cerebral DOT depends on the amount of regularization chosen when distributed source localization methods (e.g., minimum norm estimates and tSVD) are used. We demonstrate the need for an independent parameter selection based on the features of the measurement data. To this end, we propose cross-validation (CV) for parameter selection. This yields high quality results and allows for an automatic data-driven determination.

Second, we benchmark the outcome of seven image reconstruction methods which are:

- widely applied standard reconstruction methods such as tSVD, \( \ell_2 \)-MNE, and a depth- and noise-weighted variant;
- recently proposed sparse methods (minimum \( \ell_1 \)- and a smooth minimum \( \ell_0 \)-norm estimate);

- and finally, two EEG source localization algorithms adapted to DOT. More precisely, we apply the linearly constrained minimum variance (LCMV) beamformer and a method for source localization using spatial flexibility (S-FLEX). S-FLEX has proven to be a good compromise between focality and smoothness, and allows the recovery of multiple activation foci from EEG data.

Our simulation mimics a cerebral DOT experiment. It provides a very realistic framework using an atlas-based five-layered head model in combination with real-world noise data, which are added to the simulated signals to take fiber distance-dependent noise levels. Rather than using transilluminated cylindrical (or breast tissue mimicking) geometries with one reconstructed sample point (e.g., to detect areas with different optical properties, such as tumors), we performed this study on a semi-infinite medium with a highly attenuated light sensitivity in deeper layers. Additionally, an enormous amount of data is being processed, as is typical for high-density cerebral DOT since it is used to record thousands of sample points in hundreds of optical data channels.

2 Methods

2.1 Head Atlas and Meshing

To achieve a simulation setting which is close to a real measurement, we used the Montreal ICBM 2009a atlas, an unbiased nonlinear average of 152 anatomical MR images with 1 mm³ voxel size and corresponding tissue probability maps for cerebrospinal fluid, gray matter, and white matter. In order to obtain a five-compartment model including scalp and skull, we additionally segmented the ICBM2009a images using mathematical morphological operations. Based on this segmented brain atlas [see Fig. 1(c)], we used a masking and meshing software (Nirview) to create a 3-D tetrahedral mesh [Fig. 1(e)]. This mesh was used to calculate the photon transport, and thus provides the framework to simulate the cortical activation and to test the outcome of different reconstruction methods.

2.2 Forward Simulation and Spatial Constraints

Optical fiber positions on the boundary of the FE mesh were chosen according to the setting of a previous real-world cerebral DOT experiment conducted under resting conditions [Fig. 1(b)]. Due to the use of registration landmarks from the EEG 10–20 reference system and known source-detector distances, the coordinates for each fiber were known. To model light propagation, we used the Nirfast software toolbox a MATLAB-based publicly available light modeling and reconstruction software. Nirfast applies the diffusion equation approximation, which is appropriate when scattering events dominate over absorption and the medium can be assumed to be an isotropic fluence field.

One challenge in DOT is the sensitivity of the measurement to signals coming from noncortical regions. The HbO₂ specific wavelength is often contaminated with hemodynamic fluctuations from superficial veins in the scalp. On the other hand, the decrease in absorption from the HbR sensitive wavelength is highly correlated to the BOLD response in functional magnetic resonance imaging. For this simulation study, we use light model and data from the HbR sensitive wavelength of 760 nm. Optical properties \( \mu_a \) and \( \mu'_s \) were assigned to each node of the FE mesh according to Strangman et al.
The result of the simulated light propagation is a sensitivity/Jacobian matrix $J$ with dimensions $M \times N$, where $M$ is the number of measurements (optical data channels) and $N$ is the number of nodes in the reconstruction volume. $J$ describes the logarithmic relationship between changes in measured boundary data ($\Delta y$) that are caused by small changes of $\mu_a$ within the tissue for each channel-node combination, where

$$\Delta y = J \Delta \mu_a.$$  \hfill (1)

Since the reconstruction volume was not entirely covered with the optode set, and since DOT has only a limited penetration depth of 3 to 4 cm, we constrained $J$ in order to reduce the result space and thus reduce the “degree of ill-posedness.” One criterion for the exclusion of nodes was their affiliation to the noncortical tissue. Nodes belonging to scalp, skull, or cerebrospinal fluid were discarded. To exclude “weak” channels with very low sensitivity (e.g., due to large source-detector separation), we calculated the vector norm for all rows of $J$. Rows having a norm lower than 1% of the maximum value were discarded. The same procedure was performed for the mesh nodes, excluding nodes from the result space that had hardly been reached by any measuring channel. This step reduced the result space from 256 to 232 channels, and from 150,000 to 10,000 nodes. In the following, we refer to this reduced Jacobian as $\tilde{J}$ with the dimension of $\tilde{M} \times \tilde{N}$ active, and the simulated DOT measurement $y$ defined by the $\tilde{M} \times \text{samples/hrf}$ matrix

$$y = \tilde{J} \ast \text{hrf},$$  \hfill (3)

of the sensitivity over all measurement pairs for all used nodes within the head volume.

### 2.3 Signal Generation and Noise Model

As an input signal, we modeled a hemodynamic response function (hrf) for absorption changes at 760 nm peaking 5 s after stimulus onset thereby mimicking a 400 s experiment with a stimulus duration of 20 s and an interstimulus interval of 20 s. This was necessary for testing the LCMV beamformer reconstruction method, which requires time-series data. Moreover, it allowed us to superimpose the artificial data with realistic noise of the same dimensionality obtained from the abovementioned resting-state recording.

Detector readings were generated as follows. A sparse matrix $A_{\text{sim}}$ with the dimension of $\tilde{N} \times \tilde{N}_{\text{active}}$ was created, where $\tilde{N}_e$ is the number of “activated” nodes. Each column of $A_{\text{sim}}$ labels one node by setting $A_{\text{sim}}(l) = 1$ at a specific location $l$, while all other nodes are set to “0.” The locations for these “activated” nodes were randomly chosen, but due to restrictions of the reduced Jacobian $J$, all nodes were cortical. The specific sensitivity pattern $p$ in the activated node/nodes is defined by

$$p = J \ast A_{\text{sim}}.$$  \hfill (2)

Fig. 1 (a) Segmented head atlas (ICBM 2009a, a nonlinear average of 152 MR images). From outer to inner layers: scalp, skull, cerebrospinal fluid, gray matter, white matter. (b) sketch of the optical fiber setup as used in the forward model (first nearest neighbor distance: 13 mm, (c) finite-element (FE) mesh of the left hemisphere with optical properties ($\mu_a$), (d) example of the total sensitivity of determined from the unconstrained Jacobian $J$. A cross section of the sensitivity volume is superimposed on the corresponding layer of the head model, (e) total sensitivity of the spatially constrained Jacobian $\tilde{J}$: sensitivities for skull, scalp and CSF were set to zero.

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where the $\tilde{N}_{\text{active}} \times \text{samples}\_{\text{hrf}}$ matrix $\text{hrf}$ contains the activations of the simulated brain activity at the active nodes.

We applied a realistic noise model for the purpose of testing different reconstruction algorithms under natural conditions. Most studies added white noise to the data to simulate the real measurements. In real life measurements, however, the noise is usually temporally and spatially correlated and is not normally distributed. We typically observe a higher increased noise level for larger source-detector separations than that for short distances. Second, the noise often has a high fraction of hemodynamic oscillations, which may interfere with the hemodynamic response and are sometimes hard to remove. Rather than applying a random noise term, we utilized data from a 10-min DOT experiment conducted under resting conditions as the noise model $\mathbf{N}$. For recording these resting-state data, we used a compact tomography imager that provides up to 32 sources $\times$ 32 detectors ($\text{NIRScoutX Tomography Imager, NIRx Medizintechnik, Berlin, Germany}$). This allowed us to achieve realistic simulation data with characteristic features of the real measurements. The setup for that resting-state experiment was the same as that of the simulation setup, so that fiber distances and orientations were preserved.

We selected the rows of the noise matrix $\mathbf{N}$ according to the choice of channels for $\tilde{J}$, so that identical channels were used. Additionally, we took a subset of sampling/time points (columns) from $\mathbf{N}$, so that $y$ and $\mathbf{N}$ had the same dimensions.

Finally, $\mathbf{N}$ and $y$ were normalized by their respective Frobenius norms in order to calibrate the artificial measurement and noise matrix. Given $y$, $\mathbf{N}$ and $s$, where $s$ is the signal level with a value between 0 and 1, the noisy simulated measurement $y_N$ was constructed as

$$y_N = ys + \mathbf{N}(1 - s).$$

According to the real measurements, we low pass-filtered (first-order Butterworth) the generated data with a cut-off frequency of 0.4 Hz to remove the cardiac signals. In Fig. 2(a), we see detector readings from the resting measurement for large, medium, and short source-detector separations, and the dependence of the noise level on the fiber distances. Figure 2(b) depicts examples of the generated signal for two different measurement channels, each with a signal strength of 50% $(s = 0.5)$. Because of different locations and source-detector separations, the signal in the upper measurement is less dominated by noise compared to the second example in the lower graph.

### 2.4 Image Reconstruction Methods

Since the number of measurements is much smaller than the number of reconstruction nodes, the linear system of Eq. (1) is heavily underdetermined, and a unique solution for $\Delta \mu_a$ can only be obtained under constraints on the absorption

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![Figure 2](https://example.com/figure2.png)

**Fig. 2** (a) Simulated DOT measurement with additive realistic noise recorded in resting condition using a compact tomography imager ($\text{NIRScoutX, NIRx, Medizintechnik, Germany}$). The noise level strongly depends on the source-detector separation, (b) two different measurement channels and generated signals with no noise (blue line) and with 50% noise (green line) added. The lower channel is noise dominated, since the signal generated is 100-fold smaller compared to the upper example. Due to different location and source-detector separations, noise has a different impact on the generated signal and may hamper the correct reconstruction.
coefficient distribution. In order to find a solution which is neuro-physiologically plausible, these constraints should always encode valid prior assumptions on the properties of $\Delta \mu_a$. Various such assumptions have been proposed in the literature on an EEG/MEG inverse problem, which has a similar mathematical structure. In the following paragraphs, we introduce the approaches tested. As in previous parts of the paper, we omit the dependence of $\Delta \mu_a$ and $\Delta y$ on time. Thus, unless stated otherwise, a separate reconstruction is performed for each time point (i.e., difference measurement).

### 2.4.1 Minimum $\ell_2$-norm estimate

A common way of constraining the brain source activity $\Delta \mu_a$ is to penalize its norm, thereby encoding a preference for the “least-active” (or, “least-complex”) brain state that gives rise to the measurement. In the simplest case, the complexity is measured using the $\ell_2$ norm. The minimum $\ell_2$ norm estimate ($\ell_2$ MNE) of the DOT inverse problem can be written as

$$\Delta \tilde{\mu}_a = \arg \min_{\Delta \mu_a} \| \tilde{J} \Delta \mu_a - \Delta y_N \|_2^2 + \lambda \| \Delta \mu_a \|_2^2, \tag{5}$$

where $\lambda$ adjusts the degree of regularization. The solution is obtained as

$$\Delta \tilde{\mu}_a = H_y^{(\lambda)} \Delta y_N, \tag{6}$$

where

$$H_y^{(\lambda)} = J^T (J J^T + \lambda I)^{-1} \tag{7}$$

is a precomputable pseudoinverse matrix and $I$ is the $M \times M$ identity matrix.

### 2.4.2 Minimum $\ell_1$-norm estimate

In the EEG/MEG literature, it is often noted that linear inverses (i.e., those employing $\ell_2$-norm penalties) lead to blurred images of source activity, and are unable to simultaneously separate the multiple active brain sites. As a remedy, estimation of the brain activation maps using $\ell_1$-norm penalties is often suggested. Using $\ell_1$-norm penalties leads to sparse solutions, i.e., activity maps, which are zero almost everywhere. Here, we consider a depth-weighted variant of the method proposed by Matsuura and Okabe. The minimum $\ell_1$-norm solution is given by

$$\Delta \tilde{\mu}_a = \arg \min_{\Delta \mu_a} \| \tilde{J} \Delta \mu_a - \Delta y_N \|_2^2 + \lambda \| W \Delta \mu_a \|_1. \tag{8}$$

The weight matrix $W$ is chosen to be the same as in Eq. (13). The minimum of Eq. (8) is obtained using an iterative optimization algorithm.

### 2.4.3 Smoothed minimum $\ell_0$-norm estimate

The method described in Ref. has been applied to the cylindrical geometry for DOT in Ref. It aims at a direct minimization of the $\ell_0$-norm

$$\Delta \tilde{\mu}_a = \arg \min_{\Delta \mu_a} \| \tilde{J} \Delta \mu_a - \Delta y_N \|_2^2 + \lambda \| \Delta \mu_a \|_0. \tag{9}$$

Thus, it searches for the solution with the smallest number of active voxels. Since this leads to a combinatorial optimization problem, a smooth approximation of the (discontinuous) $\ell_0$-norm of a vector is considered, which leads to optimizing a sequence of certain continuous cost functions. The function, which approximates $\ell_0$-norm, includes an additional parameter $\sigma$, which determines the quality of the approximation in terms of balancing smoothness and sparsity of the result.

#### 2.4.4 Truncated singular value decomposition

The MNE solution Eq. (1) is defined for any positive regularization constant $\lambda$. The limit

$$\tilde{J}^+ = \lim_{\lambda \to 0} \tilde{J}^T (\tilde{J} \tilde{J}^T + \lambda I)^{-1} \tag{10}$$

called the Moore–Penrose (MP) pseudoinverse of $\tilde{J}$. The MP solution $\tilde{J}^+ \Delta y_N$ is the source activity with the smallest $\ell_2$-norm that exactly fulfills Eq. (1), whereas solutions $H_y \Delta y_N$ for $\lambda > 0$ no longer perfectly explain the data. The computation of $\tilde{J}^+$ can be performed using the singular value decomposition (SVD)

$$\tilde{J} = U \Sigma V^T \tag{11}$$

of $\tilde{J}$, where $\Sigma = \text{diag}(\sigma_1, \ldots, \sigma_M)$ is a $\tilde{M} \times \tilde{M}$ diagonal matrix, $\sigma_1 \geq \cdots \geq \sigma_M$ are the singular values, $U$ is an orthogonal $\tilde{M} \times \tilde{M}$ matrix with $U^T U = U U^T = I$, and $V$ is an $\tilde{N} \times \tilde{M}$ matrix with $V^T V = I$.

The MP pseudoinverse of $\tilde{J}$ Eq. (11) can be equivalently written as

$$\tilde{J}^+ = V \Sigma^{-1} U^T. \tag{12}$$

Similarly, for $\lambda > 0$, the SVD can be used to compute $H_y = V (\Sigma + \lambda I)^{-1} U^T$, and thus to solve Eq. (11). The formulation of $J^+$ in terms of $U$, $\Sigma$, and $V$ offers an alternative to regularizing the source activity using an $\ell_2$-norm penalty. Given that $\Sigma^{-1} = \text{diag}(1/\sigma_1, \ldots, 1/\sigma_M)$, it is possible to compute a reduced-rank pseudoinverse

$$\tilde{J}_m^+ = V_m \Sigma_m^{-1} U_m^T \tag{13}$$

using truncated matrices $V_m$, $\Sigma_m^{-1}$, and $U_m$, where the $\tilde{N} \times \tilde{m}$ matrix $V_m$ and the $\tilde{M} \times \tilde{m}$ matrix $U_m$ are obtained by selecting the first $\tilde{m}$ rows of $V$ and $U$, respectively, and where $\Sigma_m^{-1} = \text{diag}(1/\sigma_1, \ldots, 1/\sigma_m)$ is $\tilde{m} \times \tilde{m}$.

Performing image reconstruction using $\tilde{J}_m^+$ corresponds to constraining the source estimate $\tilde{J}_m^+ \Delta y_N$ to lie within the $m$-dimensional subspace of the brain, in which brain activity contributes most strongly to the sensors.

#### 2.4.5 Weighted minimum norm estimate

Reconstructing activations only in those parts of the brain having a high impact on the measurements (as in TSV) is reasonable, since doing so ensures that weak signal components (which might simply be noise) are not overinterpreted. However, one often wants to ensure that activations from different parts of the brain are equally likely to be detected. To this end, weighted minimum-norm estimates (wMNE) are employed. The idea here is to adjust the $\ell_2$-norm penalty in Eq. (9) to compensate for the different gains activation foci have at the detector level depending on their depth. Formally, this is achieved by introducing a $\tilde{N} \times \tilde{N}$ weight matrix $W$ in the penalty term:
\[ \Delta \mu_a = \arg \min_{\Delta \mu_a} ||J \Delta \mu_a - \Delta y_N||^2_2 + \lambda ||W \Delta \mu_a||^2_2. \]  

(14)

The solution of Eq. (14) is given by

\[ \Delta \mu_a = \tilde{J}^T (\tilde{J} \tilde{J}^T + \lambda W W^T)^{-1} \Delta y_N. \]  

(15)

Here, we use a diagonal matrix \( W = \text{diag}(w_1, \ldots, w_q) \) and the entries \( w_i = S_{ai} \) of which are the diagonals of \( S = \tilde{J}^T (\tilde{J} \tilde{J}^T)^{-1} \tilde{J} \).

### 2.4.6 Sparse basis field expansions

The selection of active voxels by sparse inverses tends to be unstable and highly noise dependent.

Moreover, the \( \ell_1 \)-norm penalty prevents multiple voxels with correlated activity to be jointly selected, which may lead to scattered solutions. To cope with these shortcomings, it has been suggested to replace sparsity in voxel domain by sparsity in a space of appropriately defined spatial basis functions. The basis function dictionary of the proposed S-FLEX (sparse basis field expansion) approach consists of Gaussian blobs of different widths centered at each voxel. Sparsifying the expansion coefficients corresponding to these blobs amounts to integrating the assumption that “plausible” activation maps are composed of a small number of blob-like activities, i.e., have a simple structure.

Denoting the \( N \times KN \) matrix of Gaussian basis functions by \( G \) and the vector of corresponding expansion coefficients by \( c \), where \( K \) is the number of blob widths, S-FLEX decomposes the estimated brain source activity into

\[ \Delta \mu_a = W^{-1} G \tilde{c}, \]  

(16)

where \( W \) is the weight matrix defined in the section above.

S-FLEX minimizes the squared deviation from the data under an additional \( \ell_1 \)-norm constraint ensuring the sparsity of \( c \):

\[ \tilde{c} = \arg \min \{ ||J W^{-1} G c - \Delta y_N||^2_2 + \lambda ||c||_1 \}. \]  

(17)

The minimum of Eq. (17) is inserted into Eq. (16) to yield the estimated brain activation \( \Delta \mu_a \). Note that for \( G = I \), the S-FLEX solution coincides with the weighted minimum \( \ell_1 \)-norm solution Eq. (8).

For a time series, S-FLEX jointly estimates the brain activations at all available time points under the assumption that a common set of spatial basis functions is active throughout the recording. To this end, coefficients corresponding to the same basis function but different time instants are grouped together and are jointly sparsified using a so-called \( \ell_{1,2} \)-norm penalty.

Note that without this technique, the sparsity pattern would jump from each reconstructed sample to the next, entirely obfuscating the temporal structure of the activations at the voxel level. We also use the technique of the minimum \( \ell_1 \)-norm approach. However, the minimum \( \ell_2 \)-norm approach, for which this problem also occurs, can not be extended to time-series data as easily.

### 2.4.7 Linearly constrained minimum variance beamformer

In contrast to the previously discussed techniques, beamforming is not only concerned with estimating activity across the entire brain at once, but a rather does the estimation separately for each node. To this end, the activity from each voxel \( q \) is extracted by means of a designated linear spatial filter \( v_q \), which is optimized for the given data \( \Delta y_N \). The estimated brain activity is obtained as \( \Delta \mu_q = [v_1, \ldots, v_q]^T \Delta y_N \).

The idea of the LCMV beamformer is to construct filters which let signals from a specific location pass with unit gain while suppressing all noise components. The optimal filter for location \( q \) is obtained as the solution to the optimization problem

\[ v_q = \arg \min_{v_q} v_q^T C v_q \quad \text{such that} \quad v_q^T J_q = 1, \]  

(18)

where \( C \) is the covariance matrix of the data \( \Delta y_N \) taken across time, and \( J_q \) is the gain vector for the \( q \)-th voxel (the \( q \)-th column of \( J \)). The solution is obtained as

\[ v_q = [J_q^T C^{-1} J_q]^{-1} J_q^T C^{-1}. \]  

(19)

The linear constraint \( v_q^T J_q = 1 \) ensures that brain activity from voxel \( q \) (i.e., the signal of interest) is not damped, whereas the minimization of \( v_q^T C v_q \) amounts to minimizing the overall (signal + noise) power of the projected data \( v_q^T \Delta y_N \). In total, Eq. (18) maximizes the signal-to-noise ratio. However, this only holds if the source activity at different voxels is uncorrelated. If there is correlated activity, the estimation of (in particular, of the power of) the sources may be biased.

### 2.5 Reconstruction Quality Criterion: Earth Mover’s Distance

Each of the image reconstruction procedures resulted in a matrix with the dimension \( N \times \text{samples} \). To estimate the quality of the result, we calculated a general linear model in a sense of a linear regression for all reconstructed time courses \( x_1, \ldots, x_N \) with hrf as the regressor. Thus, for each voxel of the reconstruction volume, a \( t \)-value was derived. All negative \( t \)-values and those with a \( t \)-value smaller than 20% of the maximum \( t \)-value were eliminated.

As a measure of overall reconstruction quality, we applied the Earth Mover’s Distance (EMD) to the reconstruction results (\( t \)-values) of all methods. The EMD calculates the minimal amount of energy that must be spent to transform one distribution into the other. Given the known locations (\( xyz \)-coordinates) of the mesh nodes in a 3-D space, the EMD uses the Euclidean distance between all nodes as a ground metric to calculate the minimum costs of transforming the normalized histogram of \( t \)-values into the normalized histogram of the simulated activations. Figure 3 shows an impression of a good reconstruction result with a low EMD [Figs. 3(b) and 3(c)] and a poor result [Fig. 3(d)] based on one simulated activation [Fig. 3(a)]. The advantage of the EMD is its ability to compare the overall distribution of the 3-D volumes. Unfortunately, so far there is nothing looking at the EMD value gives no hint as to whether the result is blurry and/or dislocated. To gain additional information about the reconstruction quality in terms of the malpositioning of the activation, we additionally calculated the Euclidean distance between the simulated target and the maximum value of the result for the cases where only one spot was activated.
2.6 Automatic Determination of the Regularization Parameter Using Cross-Validation

Distributed inverses, such as \( \ell_1 \) MNE, \( \ell_0 \) MNE, tSVD, wMNE, and S-FLEX, directly estimate the source activity \( \Delta \mu_a \). This means that for an \( M \times T \) sensor time series, \( N \times T \) parameters have to be estimated, where \( N \gg M \). Under these circumstances, regularization is necessary (as outlined above), and the choice of the regularization parameter crucially affects whether the fitted model is too complex (overfitting the data), too simple (not explaining the relevant aspects of the data), or “just right.”

Beamformers, on the other hand, are characterized by a low number of parameters. Therefore, the estimation is typically very stable. The LCMV beamformer in Eq. (19), for example, solves \( N \) optimization problems (one for each voxel), each of which is concerned with the estimation of only a single \( M \)-dimensional filter \( \tilde{\mathbf{g}}_a \) based on the covariance matrix of a \( M \times T \) dataset \( \Delta \mu_a \), where \( T \) is the number of samples, and typically \( T \gg M \).

The parameter \( \lambda \) of regularized models drives the estimated brain activity \( \Delta \mu_a \) away from the solution that explains the best measurement to a solution with “simpler” structure. As such, \( \lambda \) critically affects the shape of the chosen solution and the reconstruction accuracy. Therefore, choosing the “right” amount of regularization is very important. This choice should not be based on visual inspection or other subjective measures in order not to bias the later neurophysiological interpretation of the results. Rather, an automatic selection criterion is required.

One way of assessing the quality of a regularized model is to measure how well it explains the unseen data which have not been used for estimating the model parameters. This can be done using CV. In \( k \)-fold CV, the data are split into \( k \) chunks. The model is fitted on \( k-1 \) chunks and evaluated on the remaining “test” chunk. This procedure is repeated for each choice of the regularization parameter and for each choice of the test chunk. The parameter that best explains the test data on average is selected and used for training a final model based on the entire data available.

In the distributed inverse source reconstruction, data folds are created by dividing the measurement channels into \( k \) sets, and the performance criterion to be estimated is the squared loss at the “test” channels, i.e., \( \| \tilde{J}^{\text{test}} \mu_a - \Delta \mu_a^{\text{test}} \|_2^2 \), where \( \tilde{J}^{\text{test}} \) and \( \Delta \mu_a^{\text{test}} \) are the parts of \( \tilde{J} \) and \( \Delta \mu_a \) belonging to the test channels. For inverse methods estimating the brain activations as linear combinations of the data using some pseudoinverse \( \tilde{J}^p \) (such as MNE, wMNE, and tSVD), an approximation to leave-one-out CV (i.e., \( k \)-fold CV with \( k = M \)) can be carried out in the closed form. The so-called generalized CV score \( g(\lambda) \) is given by

\[
g(\lambda) = \frac{\| \tilde{J}^p \mu_a - \Delta \mu_a \|_2^2}{\text{trace}(I - \tilde{J}^p \tilde{J}^p)^{-1}},
\]

where \( \tilde{J}^p \) is the pseudoinverse constructed using the regularization parameter \( \lambda \). The value of \( g(\lambda) \) is calculated for every \( \lambda \) to be tested, and the parameter with the minimal score is used for reconstruction.

One goal of this work is to show how the reconstruction quality alters when different regularization values are used for reconstruction. Methods that directly estimate \( \Delta \mu_a \) are highly dependent on the choice of this parameter. To visualize this relationship, we first generated one target, then added 50% noise to the artificial measurement matrix, and finally reconstructed this specific activation using a wide range of values for \( \lambda \). For every instance of this reconstruction result, the EMD was calculated. This procedure was repeated \( 50 \) times for \( \ell_2 \) MNE and wMNE. To test the same for tSVD, we proceed in the same manner except that we increased the number of singular values used for reconstruction, starting with the 10 highest and ending with using all \( (m = 231) \).

3 Results

In the following section, first we show that the effectiveness of the proposed methods depend on the regularization parameter \( \lambda \) chosen (or in case of tSVD the number of singular values \( m \)). Second, we present simulation results that were achieved using the seven methods described above. We benchmark

![Fig. 3 Example for image reconstruction using ISVD and with different numbers of singular values used for inversion of \( J \). (a) Simulated target activation, (b) result using 30 used singular values for reconstruction (EMD = 12.6, best possible result), (c) result using (cross-validated) 60 singular values (EMD = 15.1), (d) result from reconstruction with 160 singular values (EMD = 57.3).](image-url)
their performances in a realistic DOT simulation for one and two activated spots.

3.1 Reconstruction Quality Highly Depends on the Choice of the Regularization Parameter: an Almost Optimum Choice Can Be Made without a User Bias

To visualize the impact of the chosen value for regularization, Fig. 3 depicts an example of reconstruction for tSVD, where the activation was recovered using different numbers of singular values for the inversion of \( \mathbf{J} \). Figure 3(b) shows the best possible reconstruction result with the lowest EMD for this simulation [Fig. 3(a)]. The result that was achieved with the cross-validated number of singular values is shown in Fig. 3(c). Both parameters resolve the activation reasonably well with a correct location and little blur. The result obtained with 160 used singular values [Fig. 3(d)] leads to overfitting, which is evident from the high number of phantom activations.

Figure 4 depicts multiple graphs, each representing one of the distributed reconstruction methods used. The red solid line shows the mean EMD for 50 different simulations and a wide range of values for \( \lambda \) (increasing number of singular values \( m \) for tSVD, respectively). The red transparent area represents the standard error of the mean and the blue area represents the standard deviation. In all quality plots, we clearly see how EMD changes with different regularization parameters. We find a high EMD when very small or very high regularization values are chosen, rendering data that are either over or under fitted. Between them, we find a global minimum, which is indicated by the red dot representing the best possible EMD. Assuming that the location of this minimum would be known prior to reconstruction, this \( \lambda \) (\( m \), respectively) would be the first choice for parameter selection. However, in real-world experiments, the true location and extent of this activation is unknown and such a plot is not available. To overcome this challenge, this optimum is approximated by the CV as described in the section above. The blue dots in each subplot indicate the mean value for \( \lambda \) (\( m \), respectively), estimated using the CV and the respective mean EMD. In all three methods, the cross-validated value leads to results that are comparable in quality to the best possible result. The slight mismatch between the best possible and cross-validated results may be caused by the limited amount of data available.

Please note that since \( l_1 \text{MNE}, l_0 \text{MNE}, \text{and S-FLEX cannot be solved in the closed form and rely on numerical optimization, the calculation time for such a large number of variations was unreasonably high. Therefore, the results for these methods are not shown here. In practice, we choose the regularization strengths for these methods indirectly by selecting } \lambda \text{ such that the data are explained to the same extent as it was explained by wMNE using a cross-validated } \lambda \text{. The LCMV beamformer is also omitted here, since it does not depend on the choice of a regularization parameter in the same way as do the other methods, as mentioned above.}

With respect to the reconstruction quality concerning different amplitudes of the simulated target, we calculated additional simulation, testing two more aspects. First, we reconstructed a target on a fixed location with two different amplitudes and a fixed regularization parameter (optimized for one of the simulations). Then, we reconstructed a target in a fixed location with different amplitudes and a variable regularization parameter. Figure 4 depicts the relation between regularization and reconstruction quality of three distributed reconstruction methods (noisy data, one activated spot). (a) Result for \( l_2 \text{ MNE}. \) In each simulation run, the activation was reconstructed using 100 different regularization parameters. The red line depicts the average EMD for 50 simulation runs. The geometric mean of the best possible regularization value (red dot) and the same for the automatically detected (cross-validated) (blue dot) and their respective mean EMD. (b) Reconstruction quality for tSVD using an increasing number of singular values for reconstruction, (c) result for wMNE.
parameter. In both cases, the difference in amplitude heights in the most “active” voxels reflected the simulated difference. The reconstruction quality was almost identical.

3.2 Linearly Constrained Minimum Variance Beamforming Resolves Single Activation Spots Best

The second focus of this work is on benchmarking source reconstruction methods, among which are frequently used methods such as the recently proposed sparse algorithms and EEG-source localization methods. These methods are introduced below in the context of cerebral DOT with its semi-infinite geometry. Figure 5 gives an impression of the simulation and the reconstruction result for a single spot activation in a single case with the seven reviewed methods. For visualization, we show the transverse cross sections covering the area of the simulated activation.

The arrow in Fig. 5(a) indicates the node that was set “active.” Rows 1 to 7 in Fig. 5(b) show the reconstructed images

![Exemplary reconstruction images for a single spot activation. (a) Transversal slices of the reconstruction volume with the simulated activation in column 6. The other columns depict transverse cross sections adjacent to the central layer (z direction, slice depth: 1 mm). (b) Reconstruction result for a 0% noise level. Each row represents the result from one particular reconstruction method. The number in the right column indicates the Earth Mover’s Distance (EMD) for this specific example. (c) 50% noise added to the data.](https://www.spiedigitallibrary.org/journals/Journal-of-Biomedical-Optics)
for all tested methods in a noise-free simulation. Within each row, the EMD between the simulation and the result is pointed out in the last column. Figure 5(c) shows the same simulation but with 50% noise in the data.

For $\ell_2$MNE, tSVD, and wMNE, we find a relatively good localization of the peak activation with slight blurring in the noise-free simulation. This blurring increases when noise is added to the data. Compared to $\ell_2$MNE, wMNE shows an increased sparsity and a lower EMD. S-FLEX and $\ell_1$MNE show small positioning errors in the noisy case and a focal result. In both noise levels, we find the ideal results for LCMV, with no displacement and a high focality. All the three latter methods appear to be rather insensitive to the applied noise level. $\ell_0$MNE performs well in the noise-free case, but fails when noise is added to the data.

For an overall comparison of all methods, the average EMD of 100 simulations with one activated spot and four different noise levels (0%, 25%, 50%, and 75%) can be found in Fig. 6(a). The respective mean Euclidean distance between simulation and maximum value of the reconstruction result can be found in Fig. 6(b).

Similar to the single case, we find the best reconstruction at every noise level when LCMV is used. In almost all simulations, the beamformer achieves a correct positioning with minimal blurring even at the highest noise level. S-FLEX and $\ell_1$MNE perform well and recover sparse results; however, their results are dislocated by a few millimeters. Interestingly, S-FLEX and $\ell_1$MNE do not achieve their best EMD scores at the lowest noise levels [see Eq. (4)]. This may be due to the fact that, for efficiency reasons, the optimization for both methods is stopped after the data have been fitted with a goodness-of-fit of $gof = 0.95$, where $gof = 1 - \frac{\|\tilde{J}\Delta x_u - \Delta y_k\|_2}{\|\Delta y_k\|_2}$. The data may be insufficiently fitted for very low noise levels.

TSVD, $\ell_2$MNE, and wMNE show a clear dependence on the noise level: with higher noise, the EMD increases. This can be especially observed in tSVD. However, although reaching a high EMD, tSVD still shows only a small positioning error (Euclidean distance) between the peak value of the reconstruction and the simulation [Fig. 6(b)]; within the highest noise level, the average Euclidean distance between the result and simulation is 8.3 mm ($\ell_2$MNE: 15, wMNE: 11, LCMV: 0.2, S-FLEX: 10.1, and $\ell_1$MNE: 8.8 mm).

This implies that the main reason for a high EMD is a higher blur level rather than malpositioning; this blur could possibly be reduced by thresholding the result. The highest sensitivity to noise is found in $\ell_0$MNE: beginning with low noise levels, the EMD and the positioning error dramatically increase.

### 3.3 Minimum $\ell_1$-Norm Achieves Best Result When Two Spots Are Active

When investigating a relatively small area of the brain, there is often only one spot of activation within the probe. However, there are approaches where larger areas or even the whole head are scanned. When the medium is larger, the possibility of including two or more areas with simultaneously fluctuating rhythms caused by a synchronic hemodynamic answer rises. We, therefore, simulated two additional areas with perfectly correlated activity in the brain.

Recovering two (or more) activation foci in an algorithm is a challenge. TSVD, $\ell_2$MNE, and wMNE show no significant differences in their EMD, which is attributable to the generally increased level of blur. That makes it harder to distinguish
the quality using the EMD method. However, when looking at single cases with visualized reconstruction results (Fig. 7), we can see that all methods except the beamformer are capable of recovering both activations. Since $l_1$MNE can reconstruct the sparser activation patches more clearly than the other methods, its performance is better, although again some slight positioning errors do occur. At lower noise levels, S-FLEX yields results comparable to those of $l_1$MNE, but their quality decreases at the highest noise levels. $l_0$MNE can almost perfectly recover both targets in a noise-free dataset, but fails again when noise is added. Due to reduced blur, wMNE shows a slight but not significant advantage over $l_2$MNE, and with increased noise levels it also has a slight advantage over tSVD. Finally, it is obvious that the LCMV beamformer cannot resolve correlated activity at different brain sites, and, therefore, shows a greatly decreased performance. For a comparison see Fig. 8.

3.4 Test on Experimental Data

It is always of interest to see how algorithms work with real data. However, it is difficult to estimate or compare the reconstruction quality with no objective reference. To get an impression of how the different algorithms work with real data, we added reconstruction results for a choice of reconstruction methods (LCMV, $l_2$MNE, tSVD, and wMNE) for a finger tapping task (right hand tapping for 20 s followed by 20 s rest, 10-min duration). Activated

![Fig. 7 Exemplary reconstruction images for two activations. (a) Simulated activation: two nodes in different locations were defined as “active” (indicated by the arrow), (b) reconstruction results for noise-free data and from seven different reconstruction algorithms, (c) results for noisy data (50%). Columns represent transverse cross sections of the reconstruction volume (z-direction, slice depth: 1 mm).]
areas were identified using a general linear model. In Fig. 9, we show the lateral view on the left hemisphere with colored areas indicating voxels with a significant \((t\)-values \(\leq -4\)) hemodynamic answer in the Hb\(R\) time courses.

### 4 Discussion

We conducted this simulation study to illustrate how image reconstruction methods depend on the regularization parameters chosen, and to benchmark a wide range of reconstruction procedures for cerebral DOT in a semi-infinite medium. To our knowledge, such an extensive study had not yet been performed. The implementation aimed at mimicking a very realistic environment for DOT measurements. However, assumptions of the nature of the used medium had to be made. For instance, the choice of optical properties to model light propagation in the head was intermediate values, since their true values alter and a variety of values have been reported. Furthermore, Ref. reported a decreasing scattering coefficient when looking at larger optode distances (reflecting deeper tissue), which is in contrast to the values used which assume an increasing value for \(\mu_s^f\).

For a most realistic data generation, we added noise originating from a real-world experiment, including all the specific features such as hemodynamic fluctuations and fiber distance-dependent noise levels that can influence reconstruction quality. This allowed the generation of datasets to be recorded in psycho-physiological experiments, while at the same time allowing for a direct assessment of the reconstruction quality. In contrast to other studies, we evaluated all methods against a semi-infinite medium. This geometry can rely on back-reflected light only and there might be differences from the usually used cubes or cylinders where light is applied from all sides.
Since experimental setups and imaging devices vary between experiments and labs, parameters such as regularization values should be determined for every reconstruction in a data-dependent (and user independent) way. In this work, we demonstrated that CV is able to ascertain the degree of regularization required for a good balance between data and noise. It can be easily implemented within the reconstruction routine and leads to high-quality results by relying solely on the measurement and the Jacobian. CV is one of the most popular methods for model selection due to its high robustness and stability. Note, however, that CV assumes stationarity, independent, and identically distributed properties for the underlying data. In the setup of the present study, all assumptions are fulfilled: (1) even though different channels are left out, the reconstruction of the signal on the remaining channels follows the overall distribution without causing nonstationarity, and (2) due to the low spatial range of NIRS, it can be safely assumed that the data are spatially independent.

Linear methods, such as tSVD and \( \ell_2 \)MNE, are widely used in cerebral DOT and NIRS experiments or phantom studies, because they allow for fast or even real-time volumetric image reconstruction of time series. However, they often provide heavily blurred images in which the true activation may be indistinguishable. To overcome this drawback, sparse methods such as \( \ell_1 \)MNE or S-FLEX may be used. These methods prefer spatially focal results and they have proven able to distinguish multiple activation foci. They have provided good results regardless of the number of activated spots within a medium noise level. Besides the promising results for sparse methods, some other aspects may also hamper their applications. The most important is that they are nonlinear in the data. Thus, unlike the linear methods, they cannot be implemented as a multiplication of the data matrix with a precalculated pseudoinverse matrix, but rather require iterative optimization for each new data point or chunk. This makes these algorithms unsuitable for online use and even hard to apply to large data recordings, such as psycho-physiological experiments, at all.

An increased number of measuring channels and/or a higher reconstruction resolution will dramatically increase the reconstruction time.

In our setting, smooth source localization methods were superior to most of the sparse methods concerning the computational time. For a 400 s experiment (1360 sample points) with 225 data channels, a \( \ell_2 \)MNE and a wMNE need less than 10 s for reconstruction (including CV) and \( \ell_1 \)MNE 96 s. Within the class of sparse methods, LCMV succeeds (3 min) over \( \ell_0 \)MNE (86 min), \( \ell_1 \)MNE (182 min), and S-FLEX (190 min). All calculations were performed with MATLAB R2011b (7.13), 64-bit (glxna64) (The MathWorks, Inc., Natick, Massachusetts, USA) on an Intel Core i5-2500 (4x 3.3GHz), 32 GB RAM. As previously described, the complexity of the source localization problem, and thus the computational time, increases with a higher number of data channels. However, since for smooth (\( \ell_2 \)-norm penalized) methods, a data-independent pseudoinverse can be computed, the solution of these methods can be computed for a large number of samples in an almost negligible amount of time once that matrix is available. In contrast, sparse methods need to solve an optimization problem for each new sample/data segment, which leads to increased computational costs.

As a further sparse method, we tested \( \ell_0 \)MNE, which failed to properly reconstruct the noisy data. In contrast to S-FLEX or \( \ell_1 \)MNE, the proposed implementation of \( \ell_0 \)MNE lacks the potential to treat a time series in its entirety. Since the inverse solution is recalculated for every time point, the sparsity patterns vary likewise. The performance could probably be improved if the activation is localized for one entire time series (rather than one sample at a time) with the constraint that identical voxels must be chosen for the whole time course, as was the case in implementing for S-FLEX or \( \ell_1 \)MNE.

In addition to the distributed imaging approaches discussed above, we also introduced the LCMV beamformer, another reconstruction method used in the EEG field (although originally developed for radar arrays) which provides linear filters for transforming sensor measurements into source activations, and can be efficiently applied just like tSVD, \( \ell_2 \)MNE, and wMNE. Although LCMV provides a filter matrix the size of a pseudoinverse of \( \mathbf{J} \), it technically does not provide a solution to the general forward equation. This means that certain parts of the measured data may not be explained at all, while the variance in other components may be accounted for many times in different voxels. That reason for this behavior lies in the beamformer’s property of separately modeling the activation at each voxel. Consequently, it shows excellent results when only one brain area is active or when multiple brain sites show uncorrelated activation, but it is unable to deal with correlated source signals. Furthermore, in contrast to all other methods, LCMV filters must be computed from a large amount of data. This prohibits the localization of single measurement samples and hampers straightforward online application. Its broad utilization in functional brain imaging experiments with potentially multiple correlated sources of activation has to be considered carefully in regard to paradigm, imaging setup, and the presumed area(s) of activation.

Besides the implemented methods, a huge variety of other source localization algorithms exist. A few of them are mentioned here, such as the subspace preconditioned least-squares root \( \ell_1 \)-generalized Tikhonov regularization (GTR), GTR in combination with the L-curve criterion (GTR-MLCC), \( \ell_1/\ell_2 \)-norm estimate (group lasso), \( \ell_1 + \ell_2/\ell_2 \)-norm estimate (sparse group lasso), a total variation regularization and a time-frequency mixed-norm estimate that uses time-frequency analysis for regularization.

5 Conclusion

In this work, we performed a highly realistic simulation of a functional brain imaging study with the cerebral DOT in humans on a semi-infinite medium with multiple highly attenuating layers. A choice of volumetric image reconstruction approaches were benchmarked including two recent methods for EEG source localization. We showed that linear reconstruction methods provide fast and adequate results. However, their accuracy can be increased by implementing sparse algorithms, albeit at the expense of computational time and effort. Using the framework presented, a robust system for cerebral DOT can be established and the necessary model parameters selected with the CV approach. We consider it now ready for broad usage in clinical studies, diagnosis, and general neuroscience research. Future studies will simultaneously investigate whole head multidistance optical tomography as well as multimodal image reconstruction using EEG and DOT in order to obtain a more robust reconstruction for complex sources.
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