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Abstract. Red blood cell (RBC) anomalies are significant symptoms for identification of health disorders and several blood diseases, which involve the modification of the parameters and biophysical characteristics of such cells. The aim of this study is to measure the three-dimensional phase information of healthy RBCs and their parameters, such as cell diameter, thickness, and hemoglobin (Hb) content, using Talbot-projected fringes. The Talbot image of linear grating is projected onto an RBC slide. The deformed grating lines due to the shape and refractive index of RBCs are recorded by a CCD camera through a 20× microscope objective. Hilbert transform is used to extract the phase image from the deformed projected grating lines. Experimentally calculated values of diameter (8.2 μm), thickness (2.7 μm), and Hb content (28.7 pg/cell) are well within the limits available in the literature. The proposed system is robust and user-friendly and performs the imaging of RBCs with high axial and lateral resolution (2.19 μm).

Keywords: Talbot effect; self-imaging; red blood cell imaging; Hilbert transform.

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1 Introduction

In recent decades, several optical quantitative phase imaging techniques have been developed for biological cells, including human red blood cell (RBC) imaging. These techniques are spatial phase-shifting (e.g., Ref. 1), Fourier phase microscopy (e.g., Refs. 2 and 3), Hilbert phase microscopy (e.g., Ref. 4), digital holographic microscopy (e.g., Ref. 5), diffraction phase microscopy (e.g., Ref. 6), etc. In these methods, coherent, monochromatic light sources such as lasers are used to measure the properties of biological cells. Because different properties of the biological cells, for example, phase, refractive index, and dry mass, are wavelength-dependent, some different interferometric or microscopic techniques, such as spectroscopic phase microscopy (e.g., Ref. 9), spectroscopic diffraction phase microscopy (e.g., Ref. 10), quantitative dispersion microscopy (e.g., Ref. 11), quantitative phase spectroscopy (e.g., Ref. 12), and dynamic spectroscopic phase microscopy (e.g., Ref. 13), etc., have been developed. In these techniques, multiple wavelength lasers, color filter wheels, and a broadband source with acousto-optic tunable filters are used to filter the multiple wavelengths and to determine the wavelength-dependent properties of biological cells. However, all of these techniques are costly, require complicated setups to align, need more optical components, and involve many mechanical moving parts. Partially coherent light (temporally low-coherent) sources such as a white light source, superluminescent diode, and light-emitting device are also used for biological cell imaging. Although these (spectrally broad band) sources reduce the unwanted speckle noise, they also require a dispersion compensation mechanism for the dispersion correction. Furthermore, it is not a good choice to use a spectrally broad light source if the object or medium has an inhomogeneous spectral response.

The fringe projection is a noncontact technique that can be performed either with coherent or incoherent light, by illuminating the object with a fringe pattern generated by a binary or sinusoidal grating. The advantages of using a binary fringe pattern are—(1) simple: the coding and decoding algorithms are very simple, (2) fast: because the processing algorithm is very simple, it can reach very fast processing speeds, and (3) robust: since only two levels are used, it is very robust to the noise. The projection of a light pattern with a regular structure is a noncontact technique and easy to implement for measuring the three-dimensional (3-D) profile of a biological cell, which is decoded from the deformed fringe pattern recorded on the object. The digital fringe projection technique based on the Lau effect, Moiré method, Talbot effect has been used for surface profiling and contouring of reflecting objects. If the Talbot image of grating is projected on the object, the surface information is depth encoded in a deformed fringe pattern by a carrier frequency corresponding to the grating frequency. This depth encoded shape information is obtained by the phase extraction and image processing techniques. The Talbot-projected fringe technique has been used for profiling an object from the macroscopic (0.5 mm) to microscopic (11 μm) scales. Rodriguez-Vera et al. demonstrated the 3-D contouring of diffuse objects for shape measurement using Talbot fringe projection. Microscopic shape and deformation measurement, calibration of microtopographic measurement system, and vibration analysis at microscale, etc. have also been investigated by the Talbot fringe projection method.

In this paper, the microscopic 3-D imaging of RBCs is demonstrated using the Talbot-projected fringes in transmission mode. The phase information is extracted by Hilbert transform (HT). HT is simple to implement, and phase information can be extracted from deformed fringe patterns with a phase measurement accuracy of 2/25. It requires less computational time, as

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2 Theory

The imaging of a periodic object without any imaging device is known as the Talbot effect. For plane wave illumination of a grating, behind periodic objects, at a distance $Z_T = ka^2/l(k = 2, 4, 6, 8, \ldots)$, Fresnel diffraction gives well-defined images of periodic objects, known as Fourier images or Talbot images/self-images, whereas the intermediate intensity distribution appearing between the Fourier image planes is a Fresnel image. If these Talbot fringes (self-image) are projected on an RBC slide, these fringes are deformed according to the surface profile and refractive index of RBC. These deformed Talbot-projected fringes or codified optical signals are recorded by the CCD camera and used to decode or extract the phase information of RBCs.

The diffraction intensity distribution of the grating G1 at the Talbot plane, after passing through the object (RBCs) is given as:

$$I(x) = A(x) + B \cos \left( \frac{2\pi mx}{a} + \phi(x) \right),$$

where $A(x)$ is the background intensity distribution, $B$ is a constant, $m$ is the grating order, $a$ is the period of grating, and $\phi$ is the phase delay due to the presence of transparent phase object (RBCs).

The object phase is extracted using HT. HT is a linear operator that takes a function and produces a function with a shift of $\pi/2$ in the same spatial domain. The imaginary part of the analytical signal can be practically generated by passing the original signal through a “Hilbert transform.” A real function and its Hilbert-transformed function are related to each other in such a way that they together create an analytical signal, which can be written with an amplitude and phase, and the derivative of the phase can be identified as the instantaneous frequency.

The background intensity must be eliminated prior to the application of HT for retrieving the phase. To isolate the sinusoidal term and to eliminate the background intensity, Eq. (1) is highpass filtered in the spatial domain. The filtered image can be written as:

$$I'(x) = B \cos \left( \frac{2\pi mx}{a} + \phi(x) \right).$$

Now the HT of the filtered image is performed to get the complex analytical signal associated with the real function $I'(x)$. The complex analytical signal $Z(x)$ is given by:

$$Z(x) = \frac{1}{2} \left\{ I'(x) + i\text{HT}[I'(x)] \right\},$$

where HT is the Hilbert transform.

The phase associated with $Z(x)$ can be extracted as:

$$\Delta \phi = \arctan \left\{ \frac{\text{HT}[I'(x)]}{I'(x)} \right\}.$$

The complex analytical signal $Z(x)$ exhibits rapid phase modulation with spatial frequency $1/a$; thus, $\Delta \phi$ is strongly wrapped. Finally, the phase $\phi(x)$ associated with the presence of the object is extracted as:

$$\phi(x) = \Delta \phi - q(x), \quad \text{where} \quad q(x) = \frac{2\pi m}{a}$$

The wrapped phase, $\Delta \phi$, is unwrapped using the Goldstein phase unwrapping algorithm.

3 Experimental Setup

Figure 1 shows the schematic diagram of the experimental setup. A light beam from a He–Ne laser of wavelength 632.8 nm is expanded using a 40x microscope objective (NA = 0.65) by Melles Griot (model No. 160/017 40/0.65) and filtered by a pinhole of 5-µm diameter. A collimating lens of diameter 50 mm and focal length 250 mm is employed to illuminate the grating G1 (300 lines/mm) by a collimated beam. The RBC slide is placed at Talbot distance ($Z_T$) from the grating G1 (1.62 cm), so the Talbot-projected fringes (self-image of grating) lie on the RBC slide surface.

To increase the lateral resolution for RBC imaging, a microscope objective (20x, NA = 0.40) is placed such that the RBC slide with Talbot-projected fringe image should be at the focus of the microscope objective. A CCD camera is placed at a distance of 3.24 cm from the microscope objective to capture the maximum field of view.

For preparing a blood slide for RBC imaging (RBC slide), the blood samples were collected from the Indian Institute of Technology (IIT) Delhi, Hospital Pathology Lab, and approved by the responsible ethics committee of IIT Delhi, Delhi. The blood is diluted by mixing 1 ml of blood with 10 ml of saline solution (NaCl) in a test tube. One drop of this diluted blood is placed at one end of a slide and is dispersed using another slide over the slide’s length. The aim is to get a region, called a monolayer, in which the cells are spaced far enough apart to be differentiated.

When a prepared RBC slide is inserted at the Talbot plane, the Talbot-projected fringes get distorted. These distorted Talbot-projected fringes, having the phase, refractive index, and thickness information of RBCs, are recorded by a CCD camera (Make—Lumenera Corporation, Model—Infinity3-1M). The pixel size on the CCD sensor is 6.45 µm × 6.45 µm. The total number of pixels is 1392 × 1040, and the sensor chip dimension is $2/3”$. 

4 Results

HT is used for the evaluation of the phase map from the captured image.
Initially, the experiment is carried out using a USAF resolution test chart and polystyrene beads to know the resolution of the setup. A small portion of the USAF chart is captured by a CCD camera using Talbot-projected fringes and a self-imaging effect to know the lateral resolution of the setup. No other imaging optics are used for recording the image. Figure 2(a) shows the recorded image of the USAF resolution test chart with Talbot-projected fringes. The phase image of the USAF resolution test chart is reconstructed using HT. From the reconstructed wrapped phase image of the test chart, the sixth element of the seventh group can be easily seen in Fig. 2(b). This element corresponds to 228.1 line pairs/mm (i.e., the width of one line is 2.19 μm in the USAF resolution test target). From the line profile of the unwrapped phase image shown in Fig. 2(c), drawn along line AB marked in the Fig. 2(b), the observed value of one pixel is ~0.4 μm, which is used for the determination of the lateral dimension of object RBCs under study.

To study the accuracy of the system in retrieving the phase map and profiles, measurements are performed on polystyrene microbeads of a known diameter of 10 μm. The polystyrene beads are diluted in an index matching oil medium and placed on the glass slide to prepare the polystyrene beads sample slide. Figure 3(a) shows the recorded image of polystyrene beads, and Fig. 3(b) shows the reconstructed 3-D unwrapped phase corresponding to Fig. 3(a).

From the 3-D unwrapped phase map shown in Fig. 3(b), the phase of selected polystyrene bead is 3.8 rad. The size of the polystyrene bead is calculated by 
\[ \phi(x) = \frac{2\pi}{\lambda}(n_p - n_m)d, \]
where \( \phi(x) \) is the phase in radian, \( d \) is the size of the polystyrene bead, \( n_p \) is the refractive index of the polystyrene bead (1.59), and \( n_m \) is the refractive index of the index matching oil medium (1.55).

The calculated size of the polystyrene bead is 9.57 μm. The size of the polystyrene bead, according to the specification by the supplier (10 μm) is closely related to the calculated value.

Figure 4(a) shows the 3-D thickness map of a polystyrene bead, and Fig. 4(b) shows the thickness profile along line AB as shown in Fig. 4(a).

To check the consistency of the results, the same procedure was repeated with various polystyrene beads of the same size. Figure 5 shows the unwrapped phase map and the calculated thickness profile of selected polystyrene beads. The calculated size of different polystyrene beads as shown in Fig. 5 is 10.9, 9.4, 10.3, 10.1, and 9.7 μm. The experimentally calculated size of polystyrene beads shows a standard deviation (SD) of 0.32 μm from the mean value of 9.96 μm. The results are quite consistent with the size of these beads given by the supplier. The percentage error between the experimentally calculated size of polystyrene beads (average size 9.96 μm with SD 0.32) and the supplier specification (10 μm) is 0.4%.

A preliminary experiment is conducted on RBCs to ascertain the phase map and the viability of this technique for biological
Fig. 5 3-D unwrapped phase map and the calculated thickness profile corresponding to selected beads.

Fig. 6 (a) Recorded image, (b) 2-D wrapped phase of RBC, and (c) 3-D unwrapped phase of RBC.

Fig. 7 Phase image: (a) 2-D unwrapped phase of selected portion and (b) 3-D unwrapped phase of RBC.
cells. Figure 6(a) shows the recorded image of the RBCs. The phase information is obtained by the application of HT using Eq. (4). Figure 6(b) shows the wrapped phase, and Fig. 6(c) shows the 3-D unwrapped phase map corresponding to Fig. 6(a). The obtained phase map is wrapped between 0 and $2\pi$. This $2\pi$ phase discontinuity is removed using the Goldstein phase unwrapping algorithm.\textsuperscript{34} Figures 7(a) and 7(b) show the two-dimensional (2-D) unwrapped phase map and 3-D

![Figure 8](image_url)

**Fig. 8** (a) 3-D unwrapped phase of single RBC and (b) 2-D unwrapped phase profile.

![Figure 9](image_url)

**Fig. 9** 3-D unwrapped phase map and obtained diameter of RBCs.
unwrapped phase map of selected RBCs from Fig. 6(b) (shown in circle), respectively.

Figure 8(a) shows the unwrapped phase map of a single RBC selected from Fig. 7(b), and Fig. 8(b) shows the phase profile with respect to position in μm (RBC diameter), obtained by drawing a line profile on phase map along line AB. The experimentally calculated value of the selected RBC diameter is ≈ 8.2 μm.

The experiment was repeated for several RBCs. The unwrapped phase map of RBCs as shown in Fig. 6(c) was used to calculate the diameter of various RBCs. Figure (9) shows the unwrapped phase map and diameter of RBCs obtained by drawing a line profile on the phase image of various selected RBCs. The calculated diameter of different RBCs as shown in Fig. 9 is 6.8, 7.3, 8.1, 8.3, and 7.8 μm.

The mean value of the experimentally calculated diameter is found to be 7.6 μm with SD 1.21 μm, which is in good agreement with the value available in the literature. 35,36 The phase information retrieved by the proposed method can be expeditiously translated into thickness information, which in turn can be utilized to measure other relevant morphological parameters, such as cell shape and volume. As we know, the refractive index of biological cells is a vital parameter for determining the thickness and hemoglobin (Hb) concentration in RBC. The thickness of the human RBC can be calculated using the following equation:

\[
t = \frac{\lambda}{2\pi(n_{\text{RBC}} - n_m)} \phi(x),
\]

where \( \lambda \) is the wavelength of laser light, \( \phi(x) \) is the optical phase, \( n_{\text{RBC}} \) is the refractive index of a healthy RBC, \( n_m \) is the refractive index of medium, and \( t \) is the geometrical thickness of RBC. The refractive index of saline water for He–Ne laser wavelengths (632.8 nm) is 1.331, and the value of the refractive index of a healthy RBC is 1.394, as reported in the literature. 37,38 The calculated value of the RBC thickness is ≈ 2.7 μm, which is in good agreement with the value available in the literature. 35,39 Figure 10(a) shows the 3-D thickness map of RBC, and Fig. 10(b) shows the thickness profile along line AB as shown in Fig. 10(a).

Hb content measures the amount of protein present in one RBC. For the measurement of the Hb content, the measured 2-D phase at the normal angle was used. The Hb content of an RBC is given as

\[
\text{Hb content} = \frac{\lambda}{2\pi\alpha} \sum \phi(x),
\]

where \( \alpha \) is the refractive index increment (assuming average \( \alpha = 0.2 \text{ ml/g} \)) 40–42 and \( \sum \phi(x) \) is the 2-D optical phase integrated over the entire cell area. The term \( \sum \phi(x) \) is calculated by multiplying the phase \( \phi(x) \) to the projected cell area (shape of the RBC is considered circular), so fewer errors are involved in assessing the phase value over a small area. 40 The calculated mean value of the Hb content is ~ 28.7 pg/cell. 40,41 Figure 11 shows the 2-D and 3-D Hb contents of one RBC.

Fig. 10 (a) 3-D thickness map of RBC and (b) thickness profile along line AB.

Fig. 11 Hemoglobin content of RBC: (a) 2-D and (b) 3-D.
In addition, the Hb concentration in an RBC can also be obtained from the Hb content divided by the cellular volume.

5 Conclusion

We have presented a simple and low-cost, quantitative phase measurement technique for 3-D microscopic imaging of RBCs using the Talbot-projected fringes of a linear grating. The present method will open possibilities for diagnosing diseases as well as studying the pathophysiology of human RBCs. In addition, the stability of the proposed system from environmental perturbation due to its common-path geometry as well as its compactness and portability give it a high potential for clinical applications.

Disclosures

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References

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