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Shanghai Jiao Tong University Department of Electronic Engineering 800 Dongchuan Road, Minhang Shanghai 200240, China **Abstract.** An optical indicator is designed to detect the moving targets in complex-valued synthetic aperture radar (SAR) images and estimate their azimuth velocity components. The indicator consists of two subsystems, and each of them is composed of one phase-only filter and two cylindrical lenses. The subsystems refocus the SAR image by changing the parameters of the phase-only filters to get two refocused images in which the background is defocused to the same extent while the moving targets are defocused differently. The indicator involved detects moving targets by comparing the sharpness of two defocused SAR images piece-bypiece, and then estimates the azimuth velocity of each detected target from its sharpness difference curve. The effectiveness of the optical architecture is investigated, and the proposal is confirmed by theoretical analysis and experiments with simulated and field data. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: 10.1117/1.OE.52.8.083103]

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1 Introduction

Ground moving target indication plays an important role in the synthetic aperture radar (SAR) image processing community. For a moving point scatterer, the image is displaced in an azimuth dimension and then defocused in the range dimension due to its range velocity component. In addition, it is smeared in the azimuth dimension due to its azimuth velocity component. In the range Doppler domain of the returns from a moving target, the range velocity component leads to a nonzero Doppler centroid and the azimuth velocity component leads to a biased Doppler modulation rate with respect to that of the background. Researchers have exploited the affected phase information to identify the moving targets in a complex-valued SAR image. ¹⁻⁵

For a moving target with a nonzero range velocity component, it is possible for it to be detected by computing the Doppler centroid in the returns via pulse-by-pulse, and the corresponding algorithms, which are relatively mature. For a target moving in the azimuth direction only, many methods have been proposed, such as shear-average based autofocusing, information extraction from the antenna beam pattern, and image stack technology. Most of them are based on using phase estimation or Doppler filterbank techniques. However, the traditional digital algorithms mainly concentrate on operations such as Fourier transformation and phase estimation. These algorithms are so complex that they are usually computationally expensive to implement. Furthermore, they are not robust enough to deal with clutters or interference.

As an optical cylindrical lens acts as a natural Fourier transform operator, it is used in many early SAR processors. In this paper, we will present an optical moving target indicator (MTI) to detect moving targets with nonzero azimuth velocities in a complex-valued SAR image, and show how to estimate their azimuth velocities.

Using our approach, two refocused SAR images are generated using two refocusing filters. In one refocused SAR image, a moving target will be in better focus, while in the other, it will be defocused. By comparing the sharpness of the two refocused SAR images, it is possible to identify the moving target.

Our optical MTI architecture uses two groups of refocusing subsystems. Each of the subsystems consists of two cylindrical lenses and one phase-only matching filter. The majority of this paper is a brief analytical description of the detection and azimuth velocity estimation methods that we used. The proposed architecture has been verified by both computer simulations and field data experiments. The results show that the optical processor is effective and practicable.

The paper is organized as follows. The principles for moving target detection and azimuth velocity estimation in the spatial domain of a given SAR image are reviewed. We then propose and discuss an optical processor using the detection and estimation principles. Both simulated and field data are used to verify the proposed scheme. Finally, we state our conclusion of the proposed concept.

2 Principles

2.1 Moving Target Detection in Space Domain

A strip-map mode SAR is considered in the following analysis. For a stationary point scatterer, its azimuth phase history has the form: 10

$$\phi_s(x) = -\pi K_a x^2,\tag{1}$$

where x is the azimuth coordinate, and $K_a = 2/(\lambda R_0)$ with λ being the carrier wavelength and R_0 being the slant range to the stationary scatterer. If a scatterer is moving in azimuth direction with a constant velocity V_a , then the azimuth signal becomes

$$s_a(x) = \exp[-j\pi K_a (1 - \varepsilon_a)^2 x^2], \qquad |x - x_0| \le l_s,$$
 (2)

where x_0 is the azimuth position of the moving scatterer when the radar bore-sight is directed to the scatterer, l_s is the synthetic aperture length, and $\varepsilon_a = V_a/V_p$ with V_p being the platform velocity.

Taking the Fourier transform of $s_a(x)$ according to the stationary phase theory and ignoring the amplitude constant and the phase constant, one obtains

$$S_a(u) = \exp\left[j\frac{u^2}{4\pi(1-\varepsilon_a)^2K_a}\right] \exp(-jux_0), \qquad |u| \le \frac{2\pi}{l_a},$$
(3)

where l_a is the antenna length. Usually $|\varepsilon| \ll 1$, so the following approximation can be made:

$$\frac{1}{(1-\varepsilon_a)^2} \approx 1 + 2\varepsilon_a. \tag{4}$$

In the traditional range Doppler algorithm, 11 if $S_a(u)$ is filtered by

$$H(u) = \exp\left(-j\frac{u^2}{4\pi K_a}\right),\tag{5}$$

then the focused version of $S_a(u)$ is

$$S_f(u) = \exp\left(j\frac{\varepsilon_a u^2}{2\pi K_a}\right) \exp(-jux_0), \qquad |u| \le \frac{2\pi}{l_a}. \tag{6}$$

Taking the inverse Fourier transform of the above in Eq. (6), the focused signal can be shown to be

$$s_f(x) = s_0(x) \star s_r(x),\tag{7}$$

where

$$s_0(x) = \frac{\sin\left[\pi \frac{2}{l_a}(x - x_0)\right]}{\pi(x - x_0)},\tag{8}$$

$$s_r(x) = \mathsf{F}_{u \to x}^{-1} \left[\exp\left(j \frac{\varepsilon_a u^2}{2\pi K_a}\right) \right], \qquad |u| \le \frac{2\pi}{l_a}, \tag{9}$$

and the symbol \star means the convolution operation. In Eq. (9), F⁻¹ denotes the inverse Fourier transform. According to the stationary phase theory, and neglecting the constant coefficient, $s_r(x)$ takes the form

$$s_r(x) = \exp\left(j\pi \frac{K_a x^2}{2\varepsilon_a}\right). \tag{10}$$

Equation (10) indicates that a residual quadratic phase term appears in the refocused signal. This residual term affects the focusing effectiveness.

The effect of the residual quadratic phase is shown in Fig. 1. In Fig. 1(a), the solid line represents the time frequency distribution of a stationary target, the dotted line and the dashed line represent that of two moving targets

with the negative and positive azimuth velocity component, respectively.

It can be seen that the Doppler chirp rate of a moving target varies with its azimuth velocity component. In the traditional range Doppler imaging algorithm, the azimuth matched filter is optimally designed for the stationary background, so when it is used to compress the azimuth signal history of a moving target, a residual quadratic Doppler phase appears as shown in Fig. 1(b). In this figure, after being compressed in azimuth, it can be seen that the quadratic Doppler phase term of a stationary target is ideally removed after azimuth compression, which means that the stationary target can be focused optimally.

For the two moving targets, as the residual quadratic Doppler phase terms exist, the compressed signal of the target with $\varepsilon_a > 0$ and that of the target with $\varepsilon_a < 0$ have the pulse width of Δt_1 and Δt_2 , respectively.

As the bandwidth of $s_r(x)$ is $4\pi/l_a$, its azimuth width in space domain satisfies

$$2\pi \frac{K_a}{2|\varepsilon_a|} \qquad \Delta x = \frac{4\pi}{l_a},\tag{11}$$

and thus

$$\Delta x = |\varepsilon_a| \mu_x \cdot \rho_a,\tag{12}$$

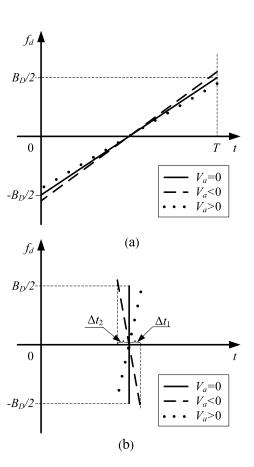


Fig. 1 Results of azimuth compression in Doppler domain. (a) Time–frequency representation of a stationary target and two moving targets. (b) Residual quadratic Doppler phase term after azimuth compression.

where $\mu_x = \lambda R_0/\rho_a^2$ with $\rho_a = l_a/2$ being the theoretical azimuth resolution which is the effective space width of $s_0(x)$. The image of a moving scatterer will be smeared to the azimuth length

$$\rho_{\text{smear}} \approx (1 + |\varepsilon_a|\mu_x)\rho_a. \tag{13}$$

If the SAR image is refocused in azimuth with a pair of new refocusing filters described by

$$H_1(u) = \exp\left(-j\frac{\varepsilon_a' u^2}{2\pi K_a}\right),\tag{14}$$

and

$$H_2(u) = \exp\left(j\frac{\varepsilon_a' u^2}{2\pi K_a}\right),\tag{15}$$

where $\varepsilon_a' = V_a'/V_p$ with V_a' is a probing azimuth velocity, then two refocused SAR images will be obtained. In the two refocused SAR images, the background is smeared to the same extent, while for a moving target, the two refocused Doppler spectra will be

$$S_{f1}(u) = \exp\left[j\frac{u^2}{2\pi K_a}(\varepsilon_a - \varepsilon_a')\right] \exp(-jux_0),\tag{16}$$

and

$$S_{f2}(u) = \exp[j\frac{u^2}{2\pi K_a}(\varepsilon_a + \varepsilon_a')] \exp(-jux_0). \tag{17}$$

Equations (16) and (17) illustrate that the moving target will be smeared differently in the two refocused images. In one image it is focused better, while in another image it is defocused worse. For a quadratic phase error, in the smeared image the energy tends to be spread uniformly over the distance of the smear for an un-weighted aperture.² The moving target image will be in better focus when the refocused residual phase term is smaller, with the opposite also being true.

Different measurements can be used to describe the focusing quality, such as sharpness, entropy, and contrast. We adopt the sharpness function¹² defined by

$$D = \sum_{(m,n)\in P} |g(m,n)|^4,$$
(18)

where *P* is a patch sized by a resolution cell. The moving target can be indicated by comparing the sharpness between the two refocused SAR images:

$$D_c = |D_1 - D_2|, (19)$$

where D_1 and D_2 are the sharpness distribution image of the two SAR images refocused by $H_1(u)$ and $H_2(u)$, respectively. During the sharpness computation procedure, the patches are overlapping so that a moving target with a typical size will correspond to a set of bright pixels in the sharpness difference image. The bright pixels will be kept when a median filter is used to remove isolated bright pixels caused by noise.

2.2 Azimuth Velocity Component Measurement

In Eq. (16), the refocused image is smeared in

$$M(\varepsilon_a, \varepsilon_a') = 1 + |\varepsilon_a - \varepsilon_a'| \mu_x \tag{20}$$

azimuth resolution cells, and in Eq. (17), the refocused image is smeared in

$$M(\varepsilon_a, -\varepsilon_a') = 1 + |\varepsilon_a + \varepsilon_a'| \mu_x \tag{21}$$

azimuth resolution cells. For a moving scatterer having the intensity $|b|^2$, its sharpness difference of the two refocused SAR images can be formulated by

$$D_c(\varepsilon_a, \varepsilon_a') = \frac{|b|^4}{M(\varepsilon_a, \varepsilon_a')} - \frac{|b|^4}{M(\varepsilon_a, -\varepsilon_a')}.$$
 (22)

Equation (22) will be analyzed on the condition that $\varepsilon'_a > 0$. When $\varepsilon_a > 0$, in the case of $0 < \varepsilon'_a \le \varepsilon_a$,

$$\frac{dD_a}{d\varepsilon_a'} = \frac{|b|^4 \mu_x}{[1 + \mu_x(\varepsilon_a - \varepsilon_a')]^2} + \frac{|b|^4 \mu_x}{[1 + \mu_x(\varepsilon_a + \varepsilon_a')]^2} > 0. \quad (23)$$

And in the case of $\varepsilon_a' > \varepsilon_a$,

$$\frac{dD_a}{d\varepsilon_a'} = \frac{|b|^4 \mu_x}{[1 + \mu_x (\varepsilon_a + \varepsilon_a')]^2} - \frac{|b|^4 \mu_x}{[1 + \mu_x (\varepsilon_a' - \varepsilon_a)]^2} < 0.$$
 (24)

The two cases show that (1) when $0 < \varepsilon_a' \le \varepsilon_a$, $D_c(\varepsilon_a, \varepsilon_a')$ is a monotonic increasing function that reaches its maximum value at the point where $\varepsilon_a' = \varepsilon_a$, and (2) when $\varepsilon_a' > \varepsilon_a$, $D_c(\varepsilon_a, \varepsilon_a')$ is a monotonic decreasing function that reaches its maximum value at the point where $\varepsilon_a' = \varepsilon_a$. In addition, it infinitely approaches zero with incremental increases of ε_a' .

The same analysis procedure can be repeated for the case of $\varepsilon_a < 0$. The analysis results show that (1) when $0 < \varepsilon_a' \le -\varepsilon_a$, $D_c(\varepsilon_a, \varepsilon_a')$ is a monotonic decreasing function that reaches its minimum value at the point where $\varepsilon_a' = -\varepsilon_a$, and (2) when $\varepsilon_a' > -\varepsilon_a$, $D_c(\varepsilon_a, \varepsilon_a')$ is a monotonic increasing function that reaches its minimum value at the point where $\varepsilon_a' = -\varepsilon_a$. In addition, the sharpness difference curve infinitely approaches zero with the increment of ε_a' .

Figure 2 presents two sharpness difference curves versus ε_a' for two moving targets with $\varepsilon_a > 0$ and $\varepsilon_a < 0$, respectively. From this diagram, we can see that the azimuth velocity of a moving target can be estimated from its sharpness

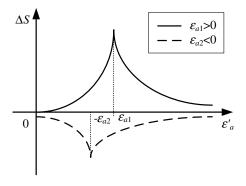


Fig. 2 Sharpness difference curves of two moving targets in opposite azimuth direction.

difference curve at the peak or valley point. The peak indicates that the target's azimuth velocity component is positive, while the valley indicates a negative value.

The discussion above provides us a chance to estimate the azimuth velocity of a detected moving target by varying ε'_a in a reasonable range.

3 Implementation

The optical MTI processor architecture is presented in Fig. 3. In this architecture, a given complex-valued SAR image named I(m,n) is separated into an amplitude part and a phase part in the computer, i.e.,

$$I(m,n) = |I(m,n)| \exp[j\varphi(m,n)], \tag{25}$$

where $\varphi(m,n)$ is the phase angle of I(m,n). Two spatial light modulators (SLM), M_0 and M_1 , are modulated by

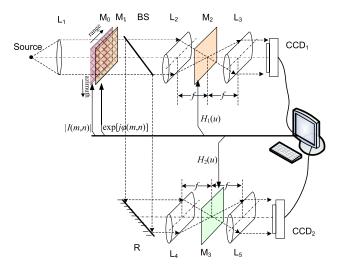


Fig. 3 An optical architecture to detect moving targets in a complex-valued SAR image.

|I(m,n)| and $\exp[j\varphi(m,n)]$, respectively. The modulated light is split up into two beams by a beam-splitter. One beam is transmitted to the cylindrical lens L_2 , the other part is reflected to the cylindrical lens L_4 . The lenses L_2 and L_4 transform the complex-valued SAR image into a range Doppler map. The phase-only SLM M_2 is modulated by the refocusing filter $H_1(u)$, and the filtered range Doppler map is transformed by the cylindrical lens L_3 resulting in a refocused SAR image. The computer samples the refocused image by using a charge-coupled diode (CCD) camera. The same operations are performed at L_4 , M_3 , and L_5 except that M_3 is modulated by the refocusing filter $H_2(u)$. After the two refocused SAR images are sampled and stored, their sharpness difference is computed and the moving targets are indicated.

Let us discuss the selection of ε_a' . For a moving target, either a too small or a too large ε_a' will lead to a small D_c . To detect moving targets with different azimuth velocities, ε_a' will vary. For example, it can be orderly selected from a set $V_a' = \{5, 10, 15, 20, 25, 30\}$ (m/s).

After a moving target is detected, it is isolated from the given SAR image and sent to the SLMs M_0 and M_1 . By varying ε'_a , a series of refocusing filter pairs are generated and displayed in M_2 and M_3 . As a result, a sharpness difference curve is drawn in the computer. The target's azimuth velocity can be estimated from this curve.

This scheme is feasible because the sharpness of clutter is erased from the sharpness difference image, and thus the moving target can be detected with greater ease. Furthermore, the optical architecture ensures high computational efficiency because complex Fourier transforms are implemented by lenses instead of digital computation.

4 Results

4.1 Computer Simulation

We can verify the proposed scheme by computer simulations combined with optical instruments. In one of the simulations, three point scatterers are used as the scene. The three

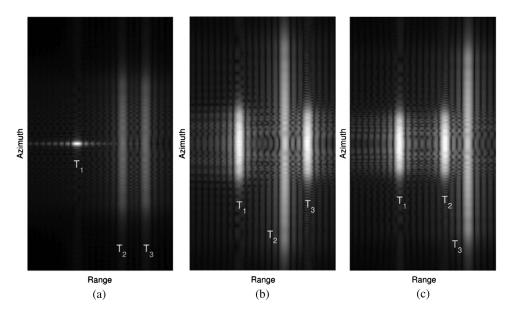


Fig. 4 Simulation results of three targets. (a) A simulated SAR image with three targets. (b) Defocused image by $H_1(u)$. (c) Defocused image by $H_2(u)$.

scatterers are set up such that one is stationary, and the other two have azimuth velocity components of -10 and 10 m/s. The radar waveform is a chirp pulse, its bandwidth is 400 MHz, the pulse width is 20 μ s, and the pulse repetition frequency is 2000 MHz. The radar carrier frequency is 10 GHz. While the radar platform is moving at the speed of 200 m/s, the returns are collected and processed, resulting in an SAR image embedded with three targets labeled by T_1 , T_2 , and T_3 shown in Fig. 4(a). From this figure, we can see that the stationary scatterer T_1 is optimally focused, while T_2 and T_3 are smeared in the azimuth direction because of their azimuth velocity components. The complex-valued SAR image is put in the SLMs M_0 and M_1 and is defocused by M_2 and M_3 . The SLMs M_2 and M_3 are modulated by $H_1(u)$ and $H_2(u)$ for $\varepsilon_a' = 0.025$ ($V_a' = 5$ m/s), and the defocused SAR images are shown in Fig. 4(b) and 4(c), respectively. From the two defocused images, we see that the scatterer T_1 is defocused to the same extent, while in Fig. 4(b), T_2 is smeared worse and T_3 is focused better,

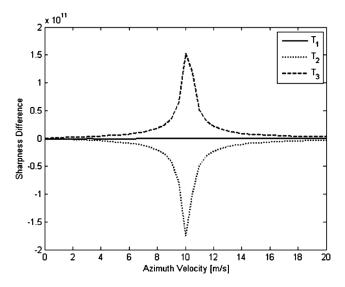


Fig. 5 Sharpness difference curves of the three simulated targets.

and in Fig. 4(c), T_2 is focused better and T_3 is smeared worse. So the moving targets T_2 and T_3 can be indicated by comparing the sharpness difference of the two defocused SAR images.

The azimuth velocity components of the three detected scatterers are estimated according to Eq. (22) by using the optical processor. The measured sharpness difference curves varying with V'_a are presented in Fig. 5. In the estimation process, V'_a ranges from 0 to 20 m/s with regular increments of 0.5 m/s. The sharpness difference curve of T_1 is flat because a stationary target tends to be defocused to the same extent in the SLMs M_2 and M_3 . The sharpness difference curve of T_2 reaches its valley value at $V'_a = 10$ m/s, and it indicates that the target's azimuth velocity is -10 m/s. The sharpness difference curve of T_3 reaches its peak value at $V_a' = 10$ m/s, and it indicates that the azimuth velocity of T_3 is 10 m/s. From Fig. 5 we see that the maximum sharpness difference values appear at the expected azimuth velocity points. The simulation results show that the proposed scheme is feasible and effective.

During our simulations, we find that the scheme provides high measurement precision because of the sharp and high sharpness difference curve for a large azimuth velocity, while for a small azimuth velocity, the measurement precision is poor because its sharpness difference curve is fairly flat and low.

4.2 Field Data

A set of field SAR data is used to verify the optical processor. Figure 6(a) shows an image of two vehicles moving along a runway at the speed of 5 m/s in the same direction. The targets are labeled by T_1 and T_2 , respectively. The radar waveform parameters are listed as follows. The carrier frequency is 9.6 GHz, the pulse width is 20 μ s, the bandwidth is 400 MHz, and the pulse repetition frequency is 1200 MHz. The platform moves at the speed of 218 m/s along the runway. From Fig. 6(a) we see that the images of the two vehicles are smeared in the azimuth direction.

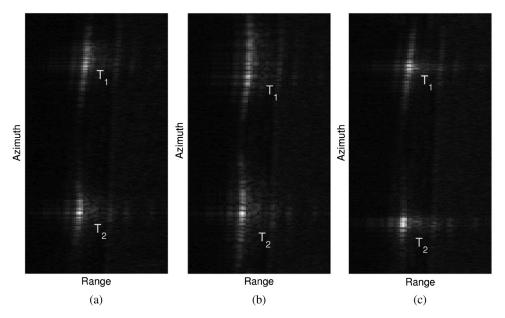
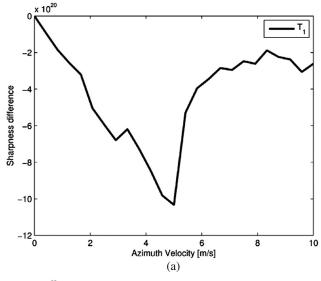


Fig. 6 Experimental results of field data. (a) A field SAR image patch. (b) Defocused image by $H_1(u)$. (c) Defocused image by $H_2(u)$.



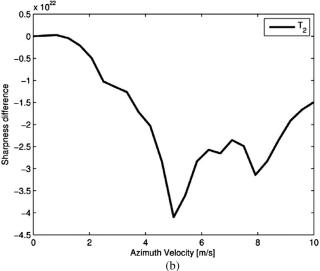


Fig. 7 Sharpness difference curves of the two targets in the field data. (a) Sharpness difference of T_1 . (b) Sharpness difference of T_2 .

In the target detection process, the SLMs M_2 and M_3 are modulated by $H_1(u)$ and $H_2(u)$ with $\varepsilon_a'=0.029$ ($V_a'=5$ m/s), respectively. After being filtered by M_2 and M_3 , two defocused SAR images are generated and shown in Fig. 6(b) and 6(c), respectively. It can be seen that the two vehicles are smeared even worse in Fig. 6(b) and focused better in Fig. 6(c). By computing the sharpness difference of the two defocused images, the moving vehicles can be indicated.

The azimuth velocity components of the two detected vehicles are measured according to Eq. (22) by using the proposed optical processor. The measured sharpness difference curves varying with V'_a are presented in Fig. 7. In the estimation process, V'_a ranges from 0 to 10 m/s with regular increments of 0.5 m/s. The two curves reach their valley values at $V'_a = 5$ m/s approximately. It indicates that the speed of the vehicles is about -5 m/s.

The curves in Fig. 7 show a nonmonotonic behavior due to the radar imaging process. Uncontrollable measurement conditions, such as the vibration of antenna, nonstraight trajectory of the platform, external interference, and digitalization, will cause phase errors in the echoes during the signal collection process. So there are some subtle differences between the two defocused images of the background, which is mixed in the detected moving target. As a result, the sharpness difference curve of a real moving target appears uneven. However, the trends of the two curves in Fig. 7 are similar to that in Fig. 2. This experimental result shows that the proposed scheme can deal with the field data practically.

5 Conclusion

In summary, we have presented an optical MTI to detect moving targets and estimate their azimuth velocities in SAR images. In principle, it is robust against clutter and interference. The experimental results using both simulated and field data show that the proposed optical architecture is feasible, effective, and practical.

Acknowledgments

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