Principle and design of ternary optical accumulator implementing $M-k-B$ addition

Yunfu Shen
Benpeng Jiang
Yi Jin
Ouyang Shan
Junjie Peng
Principle and design of ternary optical accumulator implementing M-k-B addition

Yunfu Shen,* Benpeng Jiang, Yi Jin, Ouyang Shan, and Junjie Peng
Shanghai University, School of Computer Engineering and Science, Shanghai 200444, China

Abstract. In this paper, we focus on the M-k-B addition of the form $M + B_1 + B_2 + \ldots + B_k$ based on an optical approach, where $M$ is a modified signed-digit number and $B_i$'s are the binary numbers. We present three transforms C, P, and R and an algorithm of carry-free parallel addition of $M$ and $B$. Based on these transforms, the accumulation computing $M + B$ is proposed which indicates that it requires only $2k$ steps to complete the addition in parallel. Then, the optical structures for C, P, and R transforms as well as the adder realizing $M + B$ are designed. Moreover, a photoelectric implementation of the ternary optical adder to realize M-k-B structure using the reconfiguration method is presented. Additionally, an optical experiment for 2-bit M-2-B ternary adder is carried out to demonstrate the feasibility of M-k-B adder. The work indicates that the parallel carry-free addition in form $M_0 + B_1 + B_2 + \ldots + B_k$ is easily completed.

Keywords: ternary optical computer; modified signed-digit; reconfiguration; transform; M-k-B addition.

1 Introduction

Addition is a basic arithmetic operation. Mathematicians and computer scientists have long been looking for solving the problem of time delay and low efficiency caused by the carry propagation in addition. A lot of work has been done in addition algorithms and the corresponding circuit structures since 1960s. But the efficiency of these adders is still one of the most urgent problems to be coped with. Moreover, data stream application has become more and more popular, but the processing capacity is limited by ordinary technologies. Hence, some unconventional technologies based on optical approach have been studied and now optical computing is one of the most prospective technologies. Avizienis presented the redundant representation method, with which there is no problem of carry propagation in addition and the efficiency is improved significantly. Bocker et al. applied the modified signed-digit representation (MSD) to optical computing, which is easier to be implemented in hardware and leads to the applications in optical computer. Later new achievements were continuously reported. Ghosh et al. proposed an optical model based on the modified ternary number system, in which logic operations are expressed by the one-step addition/subtraction using ternary optical adder. Alam et al. proposed a one-step addition for trinary signed-digit numbers. Li et al. adopted a method called mixed binary complement value to express information and implement carry-free optical adder. They used an optical negabinary algorithm to compute addition in two steps for any length. Zhang implemented a one-step optical negabinary and modified signed-digit adder. Salim et al. proposed a one-step trinary signed-digit arithmetic using an efficient encoding scheme. Cherri et al. studied one-step addition/subtraction using negabinary MSD representations. Optical operation based on MSD of radix 2 was an active research field. Cherri proposed symmetrically recoded modified signed-digit two-step optical addition and subtraction. Huang et al. proposed a one-step MSD parallel addition and subtraction, in which the whole of three adjacent digits is divided into 10 groups and each group is judged. Qian et al. proposed a two-step MSD addition and subtraction algorithm based on binary logic arithmetic using electron-trapping device, and presented one-step digit-set-restricted modified signed-digit adder. Jin et al. proposed a principle of ternary optical computer (TOC), the decrease-radix design principle, and the reconfiguration principle and structure, which laid a solid foundation to the system design of the application-oriented TOC. Now the TOC is configured at least one optical processor. Ternary information is obtained by the conversion of three optical states (vertically polarized light, horizontal polarized light, and no-light) of liquid crystal controlled by electricity. The operation speed of the system is determined by the response time of liquid crystal. Physicists have invented a much faster way to switch a liquid crystals. Borshch et al. presented an electro-optic effect in a nematic liquid crystal with a response time of about 30 ns to both the field-on and field-off switchings. According to the work, the operation speed of an optical processor can achieve GHz scale.

Jin et al. proposed the principles and construction of MSD adder. Peng et al. proposed a structure and implementing method for optical MSD adder from the view of application. But the MSD adder is essentially three-step. The authors proposed a one-step ternary optical MSD adder with restricted input symbols 0, 1 and proved its feasibility by experiment. But its output is an MSD number, which means that the output cannot be used to the next addition of the same type directly. Therefore, a converter must be used to transform the MSD number into binary number for the next addition. Therefore, such adder is not suitable to the binary addition of the form $B_0 + B_1 + B_2 + \ldots + B_k$, respectively.

*Address all correspondence to: Yunfu Shen, E-mail: yfshen@mail.shu.edu.cn

Optical Engineering 095108-1 September 2014 • Vol. 53(9)
In this paper, we focus on a more general MSD addition in
the following form:
\[ M + B_1 + B_2 + \ldots + B_k; \tag{1} \]
where \( M \) is an MSD number, \( B_1, B_2, \ldots, B_k \) are the binary
numbers. This kind of MSD addition will be called M-k-B addition in this paper. In Sec. 2, three key C, P, and R transforms are introduced, and an algorithm of carry-free ternary addition M-1-B and the processes of M-k-B are presented. In Sec. 3, the optical structures of three transforms as well as M-1-B adder are designed. In Sec. 4, an optical adder realizing M-1-B is presented based on reconfiguration. In Sec. 5, an experiment for M-2-B adder is described. Finally, in Sec. 6 we summarize our work.

2 Accumulation Principle of Carry-Free Ternary M-k-B Addition and Three Related Transforms

In this paper, MSD representation\(^3\) which we talk about here is a special ternary signed-digit number of radix 2.

Let \( m \) and \( b \) be 1-bit numbers, where \( m \in \{1, 0, 1\} \), \( b \in \{0,1\} \) and \( \bar{1} \) represents \(-1\). For convenience, \( i \) is also represented by \( u \).

We define three new transforms in Table 1: C transform for carry bit, P transform for primary bit, and R transform for revise bit.

Now the process of M-1-B addition of \( n \) bits is described as follows:

Denote the MSD number \( m_n m_{n-1} \ldots m_1 \) by \( M \) and the binary number \( b_n b_{n-1} \ldots b_1 \) by \( B \). The addition of \( M \) and \( B \) is carried out in two steps:

Step 1. Apply C transform to the input \( M \) and \( B \) bit by bit and denote the result by \( c \). Append one 0 at the end of \( c \) and still denote it by \( c \). Meanwhile, apply P transform to the input \( M \) and \( B \) bit by bit and denote the result by \( p \). Add one 0 at the head of \( p \) and denote it by \( p \) too.

Step 2. Apply R transform to new \( c \) and \( p \) bit by bit, and denote the result by \( s \).

We have the following theorem:

**Theorem.** The \((n + 1)\)-bit MSD number \( s \) obtained using the above two steps is the sum of \( M \) and \( B \).

**Proof.** Write \( M = M'' m_2 m_1, B = B'' b_2 b_1, M' = M'' m_2, B' = B'' b_1 \), where \( M'' = m_n \ldots m_1 \) and \( B'' = b_n \ldots b_1 \). Then, \( M = M m_2 = M' \times 2 + m_1, B = B b_1 = B' \times 2 + b_1 \) and \( M + B = (M' + B') \times 2 + (m_1 + b_1) \).

We check the results \( s \) and \( s' \) in computing \( M + B \) and \( M' + B' \) applying the three transforms respectively as follows shown in Table 2.

<table>
<thead>
<tr>
<th>C transform</th>
<th>P transform</th>
<th>R transform</th>
</tr>
</thead>
<tbody>
<tr>
<td>( m )</td>
<td>( u ) 0 1</td>
<td>( b ) 0 1</td>
</tr>
<tr>
<td>( b )</td>
<td>0 0 1</td>
<td>0 0 u</td>
</tr>
<tr>
<td>( u )</td>
<td>1 1 1</td>
<td>1 0 0</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Processes of M + B</th>
<th>Processes of M' + B'</th>
</tr>
</thead>
<tbody>
<tr>
<td>Augend M ( M'' m_2 m_1 )</td>
<td>Augend M' ( M'' m_2 )</td>
</tr>
<tr>
<td>Addend B ( B'' b_2 b_1 )</td>
<td>Addend B' ( B'' b_1 )</td>
</tr>
<tr>
<td>C transform c = ( X c_0 )</td>
<td>C transform c' = ( X 0 )</td>
</tr>
<tr>
<td>P transform p = ( Y p_2 p_1 )</td>
<td>P transform p' = ( Y p_2 )</td>
</tr>
<tr>
<td>R transform s = ( Z w p_1 )</td>
<td>R transform s' = ( Z p_2 )</td>
</tr>
</tbody>
</table>

Here, \( X = C(M', B'), Y = P(M'', B''), Z = R(X, Y) \) where \( X, Y \), and \( Z \) are the strings obtained by applying the corresponding transforms to input data bit by bit.

The lowest two bits of \( s \) are \( w p_1 = w \times 2 + p_1 \), where \( w = R(c_1, p_2) \). We need to show that \( s = s' \times 2 + (m_1 + b_1) \). That is, we need to prove that \( s = Z \times 2^2 + w \times 2 + p_1 = Z \times 2^2 + p_2 \times 2 + (m_1 + b_1) \). It is easy to see that we only need to prove \( w \times 2 + p_1 = p_2 \times 2 + (m_1 + b_1) \). Denote \( m_1 + b_1 \) by \( \bar{1} \).

Case 1: \( m_1 = u, b_1 = 0 \). Then, \( val = w = u, c_1 = C(m_1, b_1) = 0, p_1 = P(m_1, b_1) = u \) and \( w = p_2 \). So \( w \times 2 + p_1 = p_2 \times 2 + val \).

Case 2: \( m_1 = u, b_1 = 1 \) or \( m_1 = 0, b_1 = 0 \). Then, \( val = 0, c_1 = 0, p_1 = 0 \) and \( w = p_2 \). So \( w \times 2 + p_1 \) \( p_2 \times 2 + val \).

Case 3: \( m_1 = 0, b_1 = 1 \) or \( m_1 = 1, b_1 = 0 \). Then, \( val = 1, c_1 = 0, p_1 = u \) and \( w = 1 + p_2 \). So \( w \times 2 + p_1 \) \( p_2 \times 2 + (2 + p_1) = p_2 \times 2 + 1 = p_2 + 2 + val \).

Case 4: \( m_1 = 1, b_1 = 1 \). Then, \( val = 2 = (10)_2, c_1 = 1, p_1 = 0 \) and \( w = 1 + p_2 \). So \( w \times 2 + p_1 \) \( p_2 \times 2 + (2 + p_1) = p_2 \times 2 + 2 = p_2 + 2 + val \).

According to the above four cases, we find that the equation \( w \times 2 + p_1 = p_2 \times 2 + (m_1 + b_1) \) holds. Hence, \( s = s' \times 2 + (m_1 + b_1) \) is correct. We now apply C, P, and R transforms to \( M', B'' \) continuously in the same way as above. Then, we deal with \( M'' \) and \( B'' \) etc. Finally, we reach the highest bit and we have \( s = (m_n + b_n) \times 2^{n-1} + (m_2 + b_2) \times 2 + (m_1 + b_1) \). Hence, we finish the proof of the theorem.

From the above computing processes, only two steps are required to perform \( n \)-bit M-1-B addition using C, P, and R transforms in parallel. Now, we present the process of \( n \)-bit M-k-B addition of the form \( M + B_1 + B_2 + \ldots + B_k \) as follows.

Denote \( M_0 = M \). We first compute \( M_0 + B_1 \) and denote the sum by \( M_1 \). Next, we compute \( M_1 + B_2 \) and denote the sum by \( M_2 \), and so on. Finally, compute \( M_{k-1} + B_k \) and denote the sum by \( M_k \). Then, the result \( M_k \) is the sum of \( M + B_1 + B_2 + \ldots + B_k \), which is an MSD number of length \( n + k \). The whole addition is completed in \( 2k \) steps.

3 Design of 1-Bit M-1-B Adder

A one-to-one relationship can be established between the MSD symbol set \( \{0,1\} \) and the three optical states in some form. In the following, the symbols 1, 0 and \( \bar{1} \) stand for the states of vertically polarized light, horizontal
polarized light, and no-light (darkness or absence of light), respectively. But in the design of C, P, and R transforms, the state of each bit of M and B can be regarded not only as an input optical signal but also as an electric signal converted from a bright signal in order to control a liquid crystal. We use constant nonrotating liquid crystals.

The photoelectric structure for transforms C, P, and R are shown in Figs. 1–3.

In Figs. 1–3, LD, LD1, LD2... are the photoelectric converters converting the lighted signal to electric signal which is used to control liquid crystals. LC, LC1, LC2... are the liquid crystals. The black slim arrows stand for the control ports of the LCs. The diamonds stand for polarizing films which are transparent to horizontal polarized light and absorb vertical polarized light. The short and thick black films which are transparent to horizontal polarized light and absorb vertical polarized light. The short and thick black oblique lines represent holographes or beam splitting mirrors. “Source” represents a stable light source.

The principle of C transform is described as follows according to Fig. 1. We discuss three cases according to the states of m with two subcases each.

Case 1: m is u. The beam m penetrates horizontal polarized film H and LD converts bright signal into electric signal 1 to control LC1 and LC2, respectively. Meanwhile, V1 absorbs the horizontal polarized light m and LC1 thus displays a no-light state.

(1) b is 0, LC2 displays no-light, so the result c is a no-light state and c = 0.

(2) b is 1. After penetrating V2, the vertical polarized light passing through LC2 is rotated 90 deg and becomes a horizontal polarized light. Then, the horizontal polarized light is absorbed by V4 which means no light outputs. So c is still a no-light state. So c = 0.

Case 2: m is 0. LD outputs a low voltage, so LC1 and LC2 do not rotate polarized light and LC1 receives no light. Under this condition, LC1 displays a no-light state.

(1) b is 0. Then, LC2 displays a no-light state. Thus, the result c is a no-light state. So c = 0.

(2) b is 1. The vertical polarized light b passing through V2, LC2, and V4 is still a vertical polarized light. So c = 1.

Case 3: m is 1. The vertical polarized light m is absorbed by H and then LD generates a low voltage. Consequently, the lights passing through LC1 and LC2 are not rotated. The light m projects on V1 after two reflections by a beam splitting mirror and a holograph. Then, it passes through V1, LC1, and V3 in sequence. Thus, c displays a vertical polarized light. So c = 1.

(1) b is 0. Then, LC2 displays darkness. After merger of the two lights by a holograph and a half-reflection mirror, the result c is 1.

(2) b is 1. The vertical polarized light penetrates V2, LC2, and V4 successively. Now V2 displays vertical polarized light. After merger, the light is still vertical polarized. So the result c is still 1.

The cases discussed above show that the results agree with C transform in Table I(a).

The photoelectric structure of P transform is shown in Fig. 2. The principle of P transform is described as follows. We discuss two cases of b with two subcases each.

Case 1: b is 0. LD1 generates a low voltage. So LC1 does not rotate light. The light penetrating V is a vertical polarized light, which penetrates LC1 without changing its state and projects to LC2.

(1) m is 0. LC2 does not rotate light, so the vertical polarized light projecting to LC2 passes through LC2, but it is absorbed by H. So the result is no-light. Thus, p = 0.

(2) m is u or 1. LD2 converts the light signal to a high voltage 1, which enables LC2 to rotate a polarized light. The vertical polarized light projecting to LC2 is rotated 90 deg and penetrates H. So the output is a horizontal polarized light. So p = u.

Case 2: b is 1. The beam b is converted to a high voltage by LD2, which enables LC1 to rotate a polarized light by 90 deg. Here, the source light penetrating V is rotated 90 deg and becomes a horizontal polarized light by LC1 and then projects to LC2.

(1) m is 0. LC1 does not rotate a polarized light. So the horizontal polarized light projecting to LC2 passes...
through LC₂ and H. So the result is a horizontal polarized light and \( p \) is \( u \).

(2) \( m \) is \( u \) or 1. LD₂ converts the bright signal to a high voltage, which enables LC₂ to rotate a polarized light. The horizontal polarized light which projects to LC₂ is rotated 90 deg to a vertical polarized light by LC₂ and then it is absorbed by H. So the output is no-light and \( p \) is 0.

The cases discussed above show that the results agree with P transform in Table 1(b).

The photoelectric structure of R transform is shown in Fig. 3. The work procedure of R transform is described according to the four cases as follows:

Case 1: Both \( c \) and \( p \) are 0. LC₁ and LC₂ display no-light and \( r \) is 0.

Case 2: \( c \) is 0 and \( p \) is \( u \). LD₁ outputs a low voltage and LD₂ outputs a high voltage. As LC₁ does not rotate polarized light, the horizontal light \( p \) passes through LC₁ and H. So \( v₁ \) displays no-light. After LC₂ rotates polarized light and \( c \) is in no-light state, the input of LC₂ is no-light, which means that \( v₂ \) has no light. After merger, \( r \) is a horizontal polarized light.

Case 3: \( c \) is 1 and \( p \) is 0. LD₁ outputs a high voltage and LD₂ outputs a low voltage. LC₁ rotates a polarized light by 90 deg. Now \( p \) is no-light. So both LC₁ and \( v₁ \) display no-light. Meanwhile, as LC₂ does not rotate a polarized light, the vertical polarized light \( c \) passes through LC₂ and V directly. So \( v₂ \) outputs a vertical polarized light. After merger of \( v₁ \) and \( v₂ \), \( r \) is a vertical polarized light.

Case 4: \( c \) is 1 and \( p \) is \( u \). Both LD₁ and LD₂ output high voltage 1 to control LC₁ and LC₂, respectively. The horizontal light projecting on LC₁ is rotated by 90 deg to a vertical polarized light which is absorbed by H. So \( v₁ \) displays no-light. Meanwhile, the light \( c \) projecting on LC₂ is rotated by 90 deg which is absorbed by V. So \( v₂ \) displays no-light and \( r \) is a no-light state.

The cases discussed above show that the results agree with C transform in Table 1(c).

By combining the above three transformers, the photoelectric structure of 1-bit M-1-B adder is shown in Fig. 4, where \( m_{i-1} \), \( m_i \) are in MSD form, \( b_{i-1}, b_i \) are in binary form, and the result \( s_i \) is an MSD number.

Using \( n + 1 \) M-1-B adders as in Fig. 4 and configuring them together properly we obtain a carry-free adder realizing M + B of \( n \) bits, which will be seen in Sec. 5.

4 Design of M-1-B Ternary Optical Adder Based on Reconfiguration Approach

In this section, an easy way to design a photoelectric adder realizing M + B of 1-bit is described based on reconfiguration.

Firstly, encode the input for the truth tables of C and P transforms.

The addend \( b \) is a binary number and the augend \( m \) is an MSD number. Their codes are shown in Tables 3 and 4. Here, the vertically polarized light, horizontal polarized light, and no-light states are denoted by V, H, and N, respectively.

Secondly, by reconfiguration approach, there are 18 simplest basic operation units (BOUs), and any of all \( 3^3 = 19683 \) ternary logic transforms can be realized with at most six BOUs by setting a reconfiguration code. For the

<table>
<thead>
<tr>
<th>State (( b ))</th>
<th>( b'' )</th>
<th>( b' )</th>
</tr>
</thead>
<tbody>
<tr>
<td>V (1)</td>
<td>0 1</td>
<td></td>
</tr>
<tr>
<td>N (0)</td>
<td>0 0</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>State (( m ))</th>
<th>( m'' )</th>
<th>( m' )</th>
</tr>
</thead>
<tbody>
<tr>
<td>V (1)</td>
<td>1 0</td>
<td></td>
</tr>
<tr>
<td>N (0)</td>
<td>0 0</td>
<td></td>
</tr>
<tr>
<td>H (( \bar{1} ))</td>
<td>0 1</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 4 Photoelectric structure of M-1-B adder of 1-bit.
principle of reconfiguration and the photoelectric structure of BOU, the reader can refer to Ref. 21. The transforms C, P, and R are ternary logic transforms. By the true value tables in Table 1, the transformers realizing the corresponding transforms can be easily designed based on reconfiguration by setting proper reconfiguration codes to BOUs. The optical structure realizing C transform needs two BOUs, that is, one vvBOU and other hhBOU. Similarly, P transformer consists of one vhBOU and other hhBOU. Here, vvBOU, vhBOU, hvBOU, and hhBOU are four kind BOUs of VV-type, VH-type, HV-type, and HH-type, respectively.

Now, a photoelectric implementation of 1-bit adder computing M + B is shown in Fig. 5 where duplex settings of vvBOU and hvBOU in C transformer and vhBOU and hhBOU in transformer P are configured for two different functions. In Fig. 5, The dotted lines with arrow stand for the direction of current, the thick lines with arrow stand for the light transmission direction, LD1–LD4 are four photoelectric convertors, LC1–LC4 are four LCs, V1 and V2 are vertical polarized films, and H1 and H2 are horizontal polarized films. The labels Rvh, Rhh, Rvv, and Rhv denote the generating type of polarized lights, which generate the electric structures in Fig. 6 and produce a four-bit sum in R transformer. The carry-free addition realizing n-bit M-k-B can be completed in k level with 2k steps in parallel. In level i, a (n + i − 1)-bit M-1-B adder is configured. Without loss of generality, we just present a hardware experiment to verify the 2-bit addition m2m1 + b2b1 + b1′b1′ of the form M-2-B in this section. For general case, the implementation idea is the same.

For simplicity, we draw a diagram of Fig. 5 and show it in Fig. 6. Thus, the structure of M-2-B of 2 bit is shown in Fig. 7, where Levels 1 and 2 represent 2-bit and 3-bit adders, respectively. Therefore, we design a 2-bit adder computing M + B1 by using three photoelectric structures in Fig. 6. The sum M1 is a three-bit MSD number m1m2m1. Then, we design a 3-bit adder to implement M1 + B2 using four photoelectric structures in Fig. 6 and produce a four-bit sum M2.

Obviously, M1 + B2 is implemented in the same way as M + B1, but the result M2 = M + B1 can be sent directly to the next stage in the form of light signal.

In the experiment, two small-scale FPGAs are adopted to build reconfiguration circuit. Each FPGA controls three-layer liquid-crystal displays (LCDs) to construct two reconfigurable optical processors. Two DICE-SEM II digital simulation comprehensive boxes are used to complete the experiment. The ACEX1K PLD (Programmable Logic Device) of the one box is used to implement the reconfiguration circuit of transformers C and P. The ACEX1K PLD of the other box is used to implement the circuit of R transformer.

EDS819 TN (Twisted-Nematic) static stroke segment LCD is used and is shown in Fig. 8. Its light source is uniformly distributed and of high light intensity. It has three
parts labeled 1, 2, and 3. Both parts 2 and 3 have seven stroke
segments labeled A-G, respectively. In this experiment, we
do not use segments 2G, 3G, and part 1. Parts 2 and 3 are
divided into four regions VV, HV, HV, and HH as shown in
Fig. 9. The four regions can be used some or all of segments.
For example, in one LCD, the stroke segments (2F, 2E), (2A,
2D), and (2B, 2C) in part 2 are selected to represent two 3-bit
signals from high to low bit of three C transforms. Similarly,
the stroke segments (3F, 3E), (3A, 3D), and (3B, 3C) in
region VH and HH are selected to represent 3-bit signals
for three P transforms. Hence, one piece LCD is enough
to represent the results of three C and P transforms. But
four regions of one LCD are just used to represent 3-bit sig-
als for three R transforms.

In practical adder realizing M-k-B, the liquid crystals,
polaroids, light source, and sensitive arrays should be inte-
grated as a whole. But our experiment system of M-2-B
adder is only to verify the correctness of the principle men-
tioned before. Therefore, we just use common EDS819 TN

static stroke segment LCDs. Using such low-speed LCD
does not affect the replacement of liquid crystal with high
speed in practical system. Every polarizer matches with
LCD and no couplers are used. In order to easily adjust
the equipments, the components are not bonded. The lights
sources we talk about here are stable. That is, they are the
white plane illuminant scattering by LED, and the transmit-
tance does not reflect the situation of the practical system.

Take 1u + 10 + 11 as an example to illustrate the whole
experiment.

First, we design a 2-bit adder to calculate 1u + 10. The
addend 10 is encoded as 0100 and the augend 1u is encoded
as 1001 according to Tables 3 and 4. They will be the input
of BOUs.

In Fig. 10, the segments (2F, 2A, and 2B) in the region
VV are used to represent the values of vvBOUs and the seg-
ments (2E, 2D, and 2C) in the region HV are used to re-
present the three values of hvBOUs in three C transforms
from high bit to low bit in Level 1, but we set 2B and 2C
to no light. Therefore, (2F, 2E), (2A, 2D), and (2B, 2C) re-
don’t use segments 2G, 3G, and part 1. Parts 2 and 3 are
represented by the two 3-bit signals of P transforms in parallel where

Fig. 7 Structure of M-2-B of 2 bit.

Fig. 8 Specification for TN stroke segment LCD.

Fig. 9 Regions and partitions in stroke segment LCD.

Fig. 10 The results of C, P transforms: 11 and uu.
carried out four times in parallel respectively. We obtain the results 1100 and 0uu0 under four C and P transforms, respectively, and are shown in Fig. 12. Here, two TN stroke segment LCDs are juxtaposed to display signals of four C and P transforms. That is, the segments (2B, 2C) of the left LCD display the results of the fourth P transform. Here, (2B, 2C) = (0, 1) and (3B, 3C) = (0, 0). Therefore, the output of the fourth C transform is 1 and the output of the fourth P transform is 0. The segments of the right LCD are used to display the results of the other three C and P transforms as before. Combining the fourth bit with the lowest three outputs of the other three C transforms we obtain 1100 as the output of the four P transforms.

We apply R transform to 1100 and 0uu0 four times bit by bit. The four bits of the sum 10uu are shown in Fig. 13. Here, the segments (2B, 2C, 3B, and 3C) of the left LCD are used to display the fourth bit of R transform, which are (0, 1, 0, 0). It means \( s_4 = 1 \). Parts 2 and 3 of the right LCD are used to display three bits of R transforms. Therefore, we have (2F, 2E, 3F, and 3E) = (0, 0, 0, 0), (2A, 2D, 3A, and 3D) = (0, 0, u, 0), and (2B, 2C, 3B, and 3C) = (0, 0, 0, 0), which means \( s_3 = 0 \), \( s_2 = u \), and \( s_1 = 0 \). That is, the result of the sum is 10u0. It means that 10u + 011 = 10u0 (that is, 3 + 3 = 6), which is correct.

There are \( 9 \times 4 \times 4 \) cases of 2-bit addition \( M + B_1 + B_2 \). The experiments of all 144 cases show that the result for 2-bit M-2-B addition is correct.

6 Conclusions

In this paper, we introduce the design and implementation of the optical adder computing \( M + B_1 + B_2 + \ldots + B_k \). The accumulation principle of M-k-B optical adder and the three related transforms C, P, and R are proposed, and the logical structure of the adder and its implementation are presented as well. 2-bit addition of the form \( M + B_1 + B_2 \) is validated through experiment. The aim of the experiment is just to verify the principle and feasibility of the adder. As the optical components in the experiment are clung closely and there are segregate black lines between pixels, no optical crosstalk interference is found between pixels. For M-2-B adder, we only care for distinguishing the bright and the dark states, and do not consider too much the relative gray level. The key part of realizing \( M + B_1 + B_2 + \ldots + B_k \) is to compute \( M_k + B_{k+1} \) whose sum \( M_{k+1} \) can be directly used in the next step. By converting the result of the sum last step to binary number, the problem of parallel accumulation of the binary numbers of the form \( B_0 + B_1 + B_2 + \ldots + B_k \) is solved.

Acknowledgments

This work was supported by Innovation Program of Shanghai Municipal Education Commission (Grant No. 13YZ005) and Natural Science Foundation of China (Grant No. 61103054). We would like to thank Mr. Liu Xuemin, Miss Shen Luyang, all PhD candidates and graduate students of our research group for their kind help and valuable discussions as well as experiments in preparing the paper.

References


Shen et al.: Principle and design of ternary optical accumulator implementing...

Yunfu Shen currently works as an associate professor at the School of Computer Engineering and Science of Shanghai University. He received his PhD degree in mathematics from Beijing Normal University in 1996. His research experience includes model theory, computational complexity, formalization method of software and hardware, model checking, reliability, ternary optical computer, etc. He is a member of the China Computer Federation.

Benpeng Jiang received his master’s degree in engineering from Shanghai University in 2014. His research interests include optical computing, ternary optical computers, etc. Now he is working as a software engineer in TTPod.

Yi Jin received his PhD degree in computer science from Northwestern Polytechnic University, Xi’an City, in 2003. Currently, he is a professor and senior researcher at Shanghai University. His research interests include ternary optical computers and computer architecture. He is a senior member of the China Computer Federation.

Shan Ouyang now works as a lecturer at the School of Computer Engineering and Science of Shanghai University. He received his PhD degree in 2012 from Shanghai University. His research interests include ternary optical computers and embedded systems, especially the ternary optical computer hardware. At present, he holds a National Science Foundation of Shanghai municipality, and takes over the hardware development work of the third generation prototype of the ternary optical computer.

Junjie Peng is an associate professor with Shanghai University. He is on the editorial board of three international journals, and has served as a referee for more than 40 famous international journals and conferences. He is a senior member of the Chinese Institute of Electronics (CIE), senior member of the China Computer Federation (CCF), member of the Association for Computing Machinery (ACM), and a member of IEEE. His research interests include optical computing, cloud computing, wireless sensor network, etc.