Temperature-dependent behavioral model of pixels in active-matrix liquid crystal displays with fringe-field switching mode

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Abstract. This paper proposes a temperature-dependent behavioral circuit model to predict the optical characteristics of an active-matrix liquid crystal display with a fringe-field switching (FFS) mode. The optical responses of liquid crystal displays (LCDs) are strongly affected by their ambient temperature. We optimized the time-constant parameters that describe the movement of liquid crystal molecules so that simulated optical responses of FFS LCD provide the best fit to the measured responses over the temperature range of 0 to 50°C. It is found that these time-constant parameters have a linear relationship with the ambient temperature, which enables the prediction of optical responses at any given temperature. The simulation results of the transient responses show an excellent match with the measured results regardless of the ambient temperature.

Keywords: active-matrix liquid crystal display; ambient temperature; behavioral circuit model; time constant.

1 Introduction
Liquid crystal display (LCD) technology is rapidly becoming a universal choice for display applications because of its high performance and low power requirement. LCDs are now being used for mobile devices, computer monitors, large-sized televisions, and digital information displays. This means that the LCDs operate in diverse environments, such as cold and hot climates. However, color and response characteristics of LCDs are strongly affected by their ambient temperature. Therefore, the temperature-dependent characteristics of LCDs should be carefully investigated.

In order to achieve higher and advanced performance of active-matrix LCDs (AMLCDs), electrical and optical characteristics of the liquid crystal (LC) should be accurately predicted. Conventionally, the electrical and optical behaviors of LC can be solved using Poisson and Euler–Lagrange equations. These mathematical methods guarantee accurate results if all the environmental variables are known. However, these equations require significant computational time. In addition, these methods are also not compatible with circuit simulations. To solve these problems, we successfully developed a behavioral circuit model of AMLCDs by applying a first-order circuit system. In this model, the first-order circuit system is represented by a simple resistor-capacitor (RC) circuit. Further, the behavioral circuit model’s universality is verified over many types of LC modes, such as the twisted nematic, in-plane switching (IPS), patterned vertical alignment, and charge-shared vertical alignment modes.

In this paper, we propose a temperature-dependent behavioral circuit model to predict the optical characteristics of AMLCDs with a fringe-field switching (FFS) mode.

In Sec. 1, the behavioral model of pixels in AMLCDs is reviewed. In Sec. 2, we investigate the capacitance-voltage (C – V) and transmittance-voltage (T – V) characteristics of the temperature-dependent behavioral circuit model of FFS panel. In Sec. 3, the application results of the proposed model are presented. Also, the relationship between the time-constant parameters and the temperature is investigated. Finally, the conclusion is drawn in Sec. 4.

2 Review of De Smet’s Macro-Model
In this section, we review the macro-model proposed by De Smet et al. The model presents a method to simulate the optical response of an LC cell depending on the externally applied direct-current voltage. In order to achieve a simpler LC model, two assumptions were made such that the model did not lose its accuracy. The first assumption is that the behavior of all the LC molecules can be represented by a single director LC, even though a unit pixel has many LC molecules in it. The second assumption is that the LC molecules, at an equilibrium state, are affected by three main forces: (1) electric (F_{elec}), (2) elastic (F_{elas}), and (3) viscous (F_{visc}) as shown in Fig. 1(a). Thus, the motion equation can be described as

\[ cE^2 = kx(t) + \gamma \frac{dx(t)}{dt}, \]

where \( E \), \( c \), \( k \), and \( \gamma \) denote the electric field across the LC cell, a linear proportionality constant, the elastic constant, the viscosity, and an average director orientation of LC molecules with time, respectively. The electric field \( E \) can be replaced with the applied voltage \( V_{ext} \) as follows:

\[ \frac{V_{ext}^2}{c} = k \frac{d^2 x(t)}{dt} + \gamma c \frac{dx}{dt} \Rightarrow E = \frac{V_{ext}}{d}. \]
$V_{\text{ext}}$ and $d$ are the applied data voltage across the LC cell and the cell gap, respectively. Thus, the representative equilibrium motion equation is obtained as

$$V_{\text{ext}}^2 = v_i(t) + \frac{r}{k} \frac{dv_i(t)}{dt}, \quad v(t) = \frac{kd^2}{c} x(t).$$

(3)

First-order linear differential equations can be modeled by a simple RC circuit. Figure 1 shows a schematic diagram of our circuit model. Equation (3) can be behaviorally described by the RC circuit. In order to improve the accuracy, Watanabe et al. modified the time constant ($\tau$) concept on the basis of De Smet et al.'s approach. The time constant $\tau = RC$ is given by Eq. (4), where $a_1$ and $a_2$ are the physical parameters that represent the LC characteristics.

$$\tau = \frac{1}{a_1 + a_2 V_{\text{ext}}^2}.$$  

(4)

Furthermore, we defined an effective voltage, $V_{\text{eff}}(t)$, as follows:

$$V_{\text{eff}}(t) = \sqrt{v_i(t)}.$$  

(5)

$V_{\text{eff}}(t)$ proves helpful to determine the LC characteristics since it is directly related to $x(t)$, the orientation of LC molecules that defines the capacitance and transmittance of an
LC cell. If the steady-state \( C - V \) characteristics of the LC cell are known, the transient capacitance \( C_{\text{LC}}(t) \) can be determined, for a given \( V_{\text{eff}}(t) \). However, \( V_{\text{eff}}(t) \) is not identical to the voltage across the LC cell. The voltage of the cell can be calculated by considering the current through the pixel, as shown in Fig. 1(b). Therefore, \( C - V \) characteristics are the most important parameters to establish the circuit model of the pixel. In addition, the transient optical responses can also be obtained if the \( T - V \) characteristics are known.

In case of FFS mode, the pixel and the common electrodes are located in the lower glass substrate, which is not the same as shown in Fig. 1(a). Thus, the behavioral model cannot be applied to the panel structure of FFS mode. However, we have already verified that this model can be applied to the IPS mode. In this paper, we investigate the relationship between the behavioral characteristics of FFS mode and the ambient temperature. A behavioral model developed by considering a unique pixel structure of FFS mode is expected to be reported in the near future. Therefore, the above-described relations are implemented by using the analog hardware description language Verilog-A. The FFS panel is simulated by importing the behavioral circuit model into the circuit simulator SmartSPICE. Figure 2 shows the rising transitions of the FFS panel starting from gray level 0 at 30°C. Symbols and lines represent the measurement and simulation results, respectively. In the simulation, time-constant parameters \( a_1 \) and \( a_2 \) take the values \(-67.7 \text{ s}^{-1}\) and \(6.1 \text{ s}^{-1} \text{ V}^{-2}\), respectively. As shown in Fig. 3, there is a very good match between the simulation and measurement results for the rising transitions.

### 3 Temperature-Dependent Behavioral Circuit Model

#### 3.1 Capacitance–Voltage Characteristics

In our circuit model, \( C - V \) characteristics of the pixel are very important. However, the AMLCD has a lot of switching devices such as thin-film transistors, making it impossible to directly measure \( C - V \) characteristics of the pixel. To solve this problem, we proposed the use of natural transient responses. Figure 3 shows the method to determine \( C - V \) data from rising transitions. It is assumed that the initial capacitance of a pixel and the initial voltage across the pixel are \( C_0 \) and \( V_0 \), respectively (point \( P_0 \) in Fig. 3). At the beginning of the first frame, the target voltage level \( V_T \) is applied to the pixel through the switching transistor for a short time interval (point \( P_{1i} \) in Fig. 3). Thus, the total charge across the pixel becomes \( Q = C_0 \times V_T \). After the switch is turned off, the LC molecules undergo reorientation during the rest of the frame time due to the updated electric field. The capacitance of the pixel changes in accordance with the reorientation of the LC molecules. After the transistor is turned off, there is no current path at the pixel. Thus, the accumulated charge \( Q \) has to be maintained (\( Q = \text{constant} \)) during the rest of the frame time. The increased capacitance due to the reorientation of the LC molecules causes the voltage across the pixel to decrease, such that \( Q = C_0 \times V_T = (C_0 + \Delta C) \times (V_T - \Delta V) = \text{constant} \). At the end of the first frame, the final capacitance and voltage become \( C_1 \) and \( V_1 \), respectively (point \( P_{1f} \) in Fig. 3). Thus, \( C_1 \times V_1 = C_0 \times V_T \), \( C_0 < C_1 < C_T \), \( V_1 < V_T \), where \( C_T \) is the capacitance of the target level. Therefore, the capacitance

\[
T(V_{\text{eff}}) = T_{\min} + (1 - T_{\min}) \tanh \left( \frac{\beta + (\beta^2 + \eta^2)^{\frac{1}{2}}}{2} \right)
\]

\[
\beta = \frac{V_{\text{eff}} - V_{\text{to}}}{V_{\text{mo}}}
\]

\[T(V_{\text{eff}}) = T_{\min} + (1 - T_{\min})\tanh\left(\beta + (\beta^2 + \eta^2)^{1/2}\right)/2\]

\[
\beta = \frac{V_{\text{eff}} - V_{\text{to}}}{V_{\text{mo}}}
\]

**Fig. 5** Transmittance-voltage \((T - V)\) characteristics for different ambient temperatures. Symbols represent the measured data and lines represent the approximation results.
of the LC at the end of the first frame can be calculated by using Eq. (6):

$$C_1 = C_0 \times \frac{V_T}{V_1} \rightarrow \frac{C_1}{C_0} = \frac{V_T}{V_1}$$

(6)

At the beginning of the second frame, $V_T$ is applied again as shown in Fig. 3, which results in a charge of $C_1 \times V_T$ across the pixel. The updated charge has to be conserved (point $P_{2i}$ in Fig. 3). Thus, the LC molecules reach the point $P_{2f}$ ($V_2$, $C_2$) in the $C-V$ space at the end of the second frame, such that $C_2 \times V_2 = C_1 \times V_T$. The $C-V$

Fig. 6 Transient optical responses starting from gray level 0 at (a) 0°C, (b) 10°C, (c) 20°C, (d) 30°C, (e) 40°C, and (f) 50°C. Symbols represent the measured data and lines represent the simulation data.
data at the end of the second frame can be extracted by using Eq. (6):

\[
C_2 = C_1 \times \frac{V_T}{V_2} = \frac{C_0 V_T}{V_1} \cdot \frac{V_T}{V_2} 
\]

Using the above-described method, at least two \(C - V\) data can be obtained from one natural response. Additional \(C - V\) data can be obtained using other rising transitions with different target levels. Open circles in Fig. 3 represent some extracted \(C - V\) data from natural rising responses at 30°C. We measured rising transitions with different target levels for various ambient temperatures and used these to calculate the temperature-dependent \(C - V\) data. Figure 4 shows the calculated \(C - V\) characteristics for different ambient temperatures by using Eqs. (6) and (7). It can also be seen from Fig. 4 that the ratio of maximum capacitance and minimum capacitance becomes lower as the temperature increases.

### 3.2 Transmittance–Voltage Characteristics

Accurate knowledge of the \(T - V\) characteristics depending on the ambient temperature is necessary for estimating the dynamic optical behavior. In addition, the \(T - V\) characteristics should be expressed by a formula in order to obtain the transmittance corresponding to any given \(V_{\text{eff}}(t)\). The \(T - V\) characteristics of the LC cell can be expressed as a function of \(V_{\text{eff}}(t)\), given by

\[
T(V_{\text{eff}}) = T_{\text{min}} + (1 - T_{\text{min}}) \tanh \left( \frac{\beta + (\beta^2 + \eta^2)^{1/2}}{2} \right) 
\]

\[
\beta = \frac{V_{\text{eff}} - V_{\text{min}}}{V_{V_0}}. 
\]

In Eq. (8), \(T_{\text{min}}, V_{\text{max}}, V_{V_0}\), and \(\eta\) are the minimum transmittance, the optical modulation voltage, the threshold voltage, and the smoothing constant, respectively.

Figure 5 shows the \(T - V\) characteristics for different ambient temperatures. Symbols and lines in Fig. 5 represent the measured and the estimated \(T - V\) characteristics, respectively. It is seen that the \(T - V\) characteristics are negatively shifted when the ambient temperature increases. Further, the estimated \(T - V\) curves are a perfect fit to the measured data over the entire voltage range regardless of the ambient temperature.

### 4 Experimental Results and Discussion

Figure 6 shows the simulation and measurement results of rising transitions starting from gray level 0 in the FFS panel for different ambient temperatures. Symbols and lines represent the measurement and simulation results, respectively. The simulation and measurement results fit very well with each other regardless of the ambient temperature. Figure 7 shows the relationship between the time-constant parameters \(a_1\) and \(a_2\), and the ambient temperature. As shown in Fig. 7, it is found that the time-constant parameters, \(a_1\) and \(a_2\), are linearly proportional to temperature. The temperature dependency of the time-constant parameters is approximated by using linear approximations. These approximations are expressed as follows:

\[
a_1 = s_1 T + a_{1,0} \quad a_2 = s_2 T + a_{2,0}. 
\]

In Eq. (9), \((s_1, a_{1,0}), (s_2, a_{2,0})\), and \(T\) represent slopes, \(y\)-intercepts, and the ambient temperature, respectively. In FFS panel, the parameters \(s_1, s_2, a_{1,0}\), and \(a_{2,0}\) take the values of \(-1.6 \text{ s}^{-1} \text{T}^{-1}\), \(0.14 \text{ s}^{-1} \text{V}^{-2} \text{T}^{-1}\), \(-20.4 \text{ s}^{-1}\), and \(2.0 \text{ s}^{-1} \text{V}^{-2}\), respectively. As shown in Fig. 7, \(R^2\) values of the linear approximations were 0.986 and 0.997, respectively. This means that the temperature-dependent optical movement of FFS LCs can be easily estimated by simple linear approximations. Figure 8 shows simulation results of the FFS panel using the linearly estimated time-constant parameters given by Eq. (9). The simulation and measurement results fit very well with each other regardless of ambient temperature.

The work described here deals with the behavioral model to predict optical responses according to the ambient temperature. The results show that our model can accurately predict the optical responses of FFS AMLCD panel regardless of the ambient temperature. It is found that the time-constant parameters \((a_1, a_2)\) that describe the movement of LC molecules have a linear relationship with the ambient temperature. The response characteristics of FFS panel can be estimated using the four parameters given by Eq. (9). If response characteristics of FFS panels can be accurately predicted, panel manufacturers can provide customers with expected response characteristics of FFS panels before mass production so that the customers can take the temperature dependency into account while designing the display product. In addition, the findings of this study can be applied to overdrive technologies for improving responses of LCD panels. It is reported that the overdrive values are highly dependent on the temperature. Accurate prediction of responses enables engineers to obtain overdrive values for all transitions. We have been able to accurately predict the responses regardless of temperature. Therefore, we can easily obtain very accurate overdrive values depending on
temperature without any time-consuming work of extracting overdrive values at several temperatures. The research results presented in this paper will make a significant contribution to the manufacturing and designing of LCD panels and products, as designers will be able to predict optical performance very accurately regardless of temperature.

5 Conclusion
We have proposed a behavioral model of AMLCDs for precise prediction of optical responses by using a first-order circuit system. The time-constant parameters that describe the movement of the LCs have a linear relationship to the ambient temperature. The simulation results of transient optical...
responses with linearly estimated time-constant parameters show an excellent match with the measured results regardless of the ambient temperature. This research will contribute significantly to designing LCD products because designers will be able to predict optical performance accurately regardless of the temperature. In addition, the research results can be applied to overdrive technologies for improving responses of LCD panels. Accurate prediction of responses enables engineers to obtain overdrive values for all transitions regardless of temperature.

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References

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