Joint accurate time and stable frequency distribution infrastructure sharing fiber footprint with research network
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Abstract. The infrastructure essentialities for accurate time and stable frequency distribution are presented. Our solution is based on sharing fibers for a research and educational network carrying live data traffic with time and frequency transfer in parallel. Accurate time and stable frequency transmission is mainly based on fiber amplifiers with the same propagation path for both directions of transmission. This paper targets challenges related to bidirectional transmission, particularly, directional nonreciprocities. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction in any form or medium requires full attribution of the original publication, including its DOI (DOI: 10.1117/1.OE.56.2.027101)

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1 Introduction

Accurate time and stable frequency helps to improve the accuracy and resolution of a wide range of precise measurements; it also represents essential prerequisites for a broad range of fields, e.g., different flavors of sensing, Earth sciences, metrology, navigation, geodesy, astronomy, radio-astronomy, seismology, fundamental physics, etc. The use of an optical carrier with a frequency of hundreds of THz outperforms traditional radio frequency-based methods relying on much lower frequencies. Essentially, the length of a propagation path through terrestrial infrastructure is shorter, and the path itself can be greatly stabilized compared to satellite-based methods. In general, the terrestrial optical time and frequency (TF) transfer has been facing increased interest in recent years, e.g., Refs. 2-3.

Previous works have dealt with free-space optical transmission methods, e.g., Ref. 4 and their approach faced the turbulent behavior of the Earth’s atmosphere. Recent works aiming to overcome large distances are oriented toward fiber transmission, where a number of projects are using dedicated fibers or fibers shared with data transmissions. A stable propagation delay in fiber is a crucial parameter for stable and accurate transmissions, but, in addition, optical fibers are influenced by environmental changes around the optical infrastructure. These include not only temperature changes but also mechanical disturbance and acoustic vibrations. Different compensation techniques have been developed, and the majority of them are based on the reciprocity of transport delay between locations A and B: \( \delta = \delta_{AB} = \delta_{BA} \). To achieve such reciprocity in transmission requires utilizing single fiber bidirectionally, so slow acting disturbances will cancel in the first order. This is a very challenging task over long distances, especially when bidirectional optical amplification needs to be deployed. The use of bidirectional amplifiers is limited, namely due to reflections and backscattering from the real optical line. However, methods using a standard fiber pair have been developed and realized; the details can be found in Refs. 4, 5, and 6. Practical implementation of single-fiber bidirectional transmission requires utilization of some kind of directional multiplexing; otherwise, it is impossible to distinguish a useful signal from a spurious one (amplified back reflections and backscattering). In most cases, a wavelength division multiplexing is used, but occasionally, a time division multiplexing can be found.

The paper is structured as follows. Section 2 introduces the paper. Section 3 introduces the TF infrastructure under development, the concepts used for spectral sharing between transmissions, and the method for frequency transfer stabilization. Section 4 discusses directional nonreciprocities caused by relativistic effects and shows the results for the major links of the TF infrastructure. Section 5 discusses directional nonreciprocity caused by a wavelength walk-off of transmitters and shows the concept allowing a more precise determination of this value in a real network environment. Finally, Section 6 concludes the paper.

2 Infrastructure

The CESNET association (the e-Infrastructure for research and education provider in the Czech Republic) began development of TF infrastructure in 2011. The total line length of TF transmissions within the CESNET’s network is about 1683 km and roughly 67% of the infrastructure length (1137 km) is in operation, as is shown in Fig. 1. The shared model of joint TF and data has been chosen because of economic reasons, high costs for fiber leasing. The infrastructure allows the parallel transmission of accurate time and stable frequency distribution, based on wavelength.
division multiplexing (WDM). Another project introduced the feature of a joint TF transmission, however, using T modulated into a frequency signal, which can be quite non-versatile if only a T transmission is required. Recently, the WDM approach has been introduced further by the team from Ref. The two-way time transfer is based on proprietary time transfer adapters (TTAs), which have been designed using a field programmable gate array; for more details, see Ref. TTAs are capable of operating in heterogeneous environments, including multimode fibers, single-mode dedicated fibers, telecom lambdas, and passive channels within other WDM systems. Also, the transmission is performed over a single fiber bidirectional channel and traditional fiber pair setups. More details can be found in Ref.

The WDM approach mentioned above is also often used for directional multiplexing to distinguish a useful signal from spurious reflections and cross-talks. The same applies for the presented infrastructure. Time transmission utilizes the standard ITU-T grid, and the spectral walk-off was set to 100 GHz due to poor commercial availability of single-channel filters for a 50-GHz channel plan.

The spectral directional division of frequency transmission is influenced by the method used for transmission stabilization; it uses acousto-optic modulators (AOMs) to produce spectral walk-off. The AOM shifts the optical frequency of the incoming optical signal \( \nu_o \) by the value given of electrical modulation signal frequency \( f_{AOM} \):

\[
\nu_T = \nu_o + f_{AOM}.
\] (1)

The signal with a frequency \( \nu_T \) is launched into the fiber, where its frequency is subject to a shift \( \nu_D \) caused by the Doppler effect. The main contributors are thermal effects, vibrations, etc.

\[
\nu_F = \nu_T + \nu_D = \nu_o + f_{AOM} + \nu_D.
\] (2)

At the remote end, the signal with the frequency \( \nu_F \) is partially reflected and travels back to the transmitting side. Its frequency is again subject to the Doppler shift and the shift in AOM at the transmitting end:

\[
\nu_R = \nu_F + \nu_D + f_{AOM} = \nu_o + 2(f_{AOM} + \nu_D).
\] (3)

At the transmitting side, the signal is mixed with the original signal. After detection, we obtain beat frequency \( f_{BEAT} \):

\[
f_{BEAT} = \nu_T - \nu_o = (\nu_o + 2(f_{AOM} + \nu_D)) = 2(f_{AOM} + \nu_D).
\] (4)

The \( f_{BEAT} \) can be used to advantage as an error quantity to continuously modify \( f_{AOM} \) to compensate for the frequency shift \( \nu_D \) caused by the Doppler effect:

\[
f_{ERROR} = -\nu_D = -(f_{BEAT} - 2f_{AOM})/2.
\] (5)

The AOM is now fed by frequency \( f_{AOM} + f_{ERROR} \). At the receiving side, the signal with optical frequency \( \nu_T \) is delivered in Eq. 4:

\[
\nu_F_{stab} = \nu_o + f_{AOM} + f_{ERROR} + \nu_D = \nu_o + f_{AOM} = \nu_T.
\] (6)

The example of a real line Prague–Brno sharing both TF transmission is shown in Fig. For more details, see Ref.

Figure shows a spectral measurement taken at the Prague–Brno line. We can see two time channels on the right, two frequency channels (appearing as one, due to a very low walk-off) in the middle, and amplified spontaneous emission on the left. Further in the paper, we will deeply analyze the sources of directional nonreciprocities.

### 3 Nonreciprocities

As stated earlier, we expect the reciprocity of transport delay between A and B to be \( \delta = \delta_{AB} = \delta_{BA} \). However, this is not possible to achieve exactly, even during single-fiber bidirectional transmission, and we have to introduce a delay asymmetry \( \Delta \):

\[
\Delta = \delta_{BA} - \delta_{AB}.
\] (7)
The delay asymmetry $\Delta$ has to be measured and is a subject of a system calibration. For a picoseconds level of propagation time analysis, a precise description needs to be used.

### 3.1 Calibration Issues

There are several approaches for calibration of a time transfer system. The simple one is to compare the whole system with another independent time transfer method, e.g., one based on a Global Navigational Satellite System. Unfortunately, such a system can typically reach the accuracy of 1 ns, according to Ref. [4], while an optical fiber-based system can be more accurate. The solution is to calibrate individual components of the optical fiber system.

**Adapters**: calibration of the adapters including the optical transceivers is possible by measurement of the delay between an incoming electrical signal and an outgoing optical signal at the transmitter part and, similarly, between an incoming optical and an outgoing electrical signal at the receiver part.

**Optical fiber**: a bidirectional optical fiber time transfer systems assume delay cancelation in both directions (with possible evaluation of residual asymmetry as discussed later) as the delay varies due to environmental influences, mainly the temperature. The single-fiber system uses the same fiber carrying signal in both directions; therefore, the physical length is the same and the delay fully cancels in case of an identical wavelength. However, two wavelengths are typically used for both directions and the difference effect is a subject of evaluation.

**Amplifiers**: a single path amplifier has, in principle, the same delay in both directions. Its effect on different wavelengths can be directly measured.
3.2 Relativistic Effects

Propagation delay is described in Eq. (8). It takes into account the relativistic effects caused by the Earth’s rotation and gravitational potential. Only terms with a contribution higher than 1 ps on a 1000-km long link are taken into account. $\tau$ is the propagation delay, $c$ is the speed of light in a vacuum, $L$ is the fiber path length, $n$ is the refractive index, $S$ is the Sagnac term, and $G$ is the gravitational term:

$$\tau = \frac{1}{c} \int_0^L n \, dl + \frac{1}{c^2} \int_0^L S \, dl + \frac{1}{c^3} \int_0^L n \, G \, dl.$$  

(8)

The first term simply represents the influence of the refractive index, the second term describes the Sagnac effect caused by the Earth’s rotation, and the third term represents the influence of the Earth’s gravitational potential. The last term can be omitted for a two-way time transfer. Typical values of these terms for a 1000-km long link at the Earth’s equator on the surface are 5 ms, ±5 ns, and 3 ps. The higher terms can be easily omitted for picoseconds precision; for example, the contribution of $c^{-4}$ term will be of the order $10^{-17}$ for the mentioned 1000-km line. Equation (9) describes the contribution of the Sagnac correction to the propagation delay; the sign depends on the direction of the transfer (eastward or westward):

$$|\Delta \tau| = \frac{2\omega A}{c^2},$$

(9)

where $\omega$ is the angular velocity of the Earth’s rotation, numerically $7.292115 \times 10^{-5}$ rad/s. It changes in time with the Earth’s tides, but, as stated in Ref. 15, the contribution to a Sagnac term Eq. (9) is only 0.3 fs for a 1000-km link, so it is possible to omit such influence. The last variable, $A$, is the so-called Sagnac area and corresponds to the area laying on the plane perpendicular to $\omega$ defined by the projection of the fiber path to this plane and connecting endpoints of the projected path to the rotation axis; see Fig. 4.

The exact path of a leased fiber line is not commonly available (for security reasons, etc.); typically, only some points are known, for example, see the Brno–Temelin line in Fig. 5. The basic problem is the inconsistency of a real length of fiber–its known length. The known length is represented by a set of subequent line segments. For the real length, we have only meta- information in terms of the numerical value. We applied the method described in Ref. 14 to determine a minimal and maximal possible value of the Sagnac area $A$ based on the given points. Furthermore, an algorithm for detection and correction of loops has been applied. Table 1 summarizes the contribution of the Sagnac effect to directional nonreciprocities for the major lines of the TF infrastructure. Corrections were determined both using a simplified model of a single line directly interconnecting endpoints and using the known fiber line points and loop detection; see Figs. 4 and 5.

3.3 Wavelength Walk-Off

The first term in Eq. (8) describes the influence of the refractive index, whose value is wavelength dependent for a given fiber. Thus, the used directional walk-off is a source of non-reciprocity. The difference in the propagation time of the two
signals with a wavelength difference $\Delta \lambda$ is described by chromatic dispersion (CD):

$$\Delta = CD \cdot \Delta \lambda = (CD \text{ coef.} \cdot L + CD \text{ pas}) \cdot \Delta \lambda.$$  \hspace{1cm} (10)

The total value of CD is given by the fiber CD and CD of the passive components, where the fiber CD is proportional to the fiber CD coefficient and the fiber length. A standard single-mode fiber G.652D exhibits a CD coefficient of about 17.2 ps/nm · km at 1550 nm. For nonzero dispersion-shifted fibers G.655.C and G.655.E, the dispersions are 5 and −3 ps/nm · km, respectively.

In the presented infrastructure, the CD compensation is used only at one link operating over unidirectional lambdas (link Prague–Vienna). Both dispersion compensating fibers (DCF) and fiber Bragg gratings (FBG) are used as CD compensators. DCFs naturally extend the transmission path, typically adding 12 km to each 80-km span. This practically decreases the optical signal-to-noise ratio due to the necessity of more optical gain. Their contribution to temperature dependence of propagation time is limited as both DCF and FBG are deployed in controlled rooms where temperature is kept reasonably stabilized. Furthermore, FBGs have an atthermal design. The remaining bidirectional lines do not use CD compensation at all to avoid relatively lossy DCFs, meanwhile FBGs do not allow bidirectional operation at all. The large residual CD thus contributes to the uncertainty of $\Delta$ as follows. In Ref. 4, we discussed the contribution of wavelength instabilities (uncertainty of $\Delta \lambda$) to the uncertainty of $\Delta$, but we used only the high boundary of the CD estimation. For a precise determination of $\Delta$, we have to evaluate CD more precisely. The fiber CD coefficient is temperature dependent and real operation possesses other challenges; for example, a line might consist of fiber spans by different fiber vendors (or a vendor might be unknown) and, in the worst case, different fiber types with different CD coefficients and with unknown exact lengths of particular segments.

Also contributing to an overestimation of total CD is the fact that a TF channel contains plenty of passive devices, and a CD of passive components $CD_{pas}$ is provided by vendors as an upper boundary. For example, the previously mentioned line Prague–Brno contains 12 passive filters and 5 bidirectional erbium-doped fiber amplifiers (EDFAs), each containing typically 4 more passive components (directional couplers and pump couplers). Another challenge for a day-by-day operation is the fact that during any maintenance (especially unscheduled), a fiber route can be rerouted to a backup path with a very different length and sometimes a different fiber type.

The elimination of this overestimation system, based on temporary wavelength changes, has been proposed and verified. As a reference setup, two 89 km spans of G.652.D field deployed fiber with attenuation 22 dB each were interconnected into a loop and amplified by one bidirectional EDFA; for details, see Ref. 14. The smallest uncertainty of 2.2 ps, over an averaging interval of 512 s in terms of time deviation, was achieved; see Fig. 8.

We deployed a periodical wavelength change over the reference line; corresponding delay changes are depicted in Fig. 9. Over a two-day measurement, we obtained an average value of CD = 3017.6 ps/nm with a deviation 82.5 ps/nm.

As the total length is 178 km, the resulting value is in very good correspondence with the value given by the CD coefficient. Finally, the observed nonreciprocity for a 100-GHz walk-off of transmitters was 2.424 ns, with an uncertainty of 29 ps. The observed long-term wavelength instability of transmission lasers was $\Delta \lambda = 12$ pm for each transmitter laser.

In addition to the effects discussed above, a polarization mode dispersion (PMD) represents a source of uncertainty rather than directional nonreciprocity due to its stochastic

### Table 1

<table>
<thead>
<tr>
<th>Line</th>
<th>Sagnac correction – direct path</th>
<th>Sagnac correction – segments + loops detection</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brno–Temelin</td>
<td>$-0.543737 \pm 0.021341$</td>
<td>$-0.540961 \pm 0.000101$</td>
</tr>
<tr>
<td>Rez–Brno</td>
<td>$0.535933 \pm 0.017503$</td>
<td>$0.536158 \pm 0.000181$</td>
</tr>
<tr>
<td>Chaberska, Prague–Pecny</td>
<td>$0.079466 \pm 0.001396$</td>
<td>$0.079739 \pm 0.000004$</td>
</tr>
<tr>
<td>Prague–Brno</td>
<td>$0.534958 \pm 0.014714$</td>
<td>$0.534447 \pm 0.000180$</td>
</tr>
</tbody>
</table>

![Fig. 6 Operating wavelength dependable delay, reference loop 187 km.](image)

![Fig. 7 Reference loop, time stability.](image)
nature. The used modern fibers have a PMD value limited by the PMD coefficient of 0.06 ps/km\(^{1/2}\), and their maximal contribution to the uncertainty is 1.05 ps for the whole link; see Ref. 3.

We measured the PMD on some fiber links in the CESNET network and on aerial cables. Aerial cables tend to be unstable due to weather conditions and railway traffic. We found that the PMD was up to 0.4 ps, with maximum variations on order of 0.1 ps. Subsequently, we may assume that the PMD for a modern optical fiber does not affect the system significantly.

We have not evaluated the real impact of the PMD of passive devices in the transmission path due to the very complicated nature of the PMD in telco equipment. Our estimate is that the total PMD for 12 passive filters is expected to be <0.35 ps.

4 Conclusions

In this paper, we briefly introduced the infrastructure for an accurate time and stable frequency transfer being gradually developed. Theoretical aspects have been verified on the real lines, which reach over 1137 km. We also focused on the determination of bidirectional nonreciprocity caused by relativistic effects and on pilot verification of fine determination of directional nonreciprocity caused by wavelength walk-off of transmitters. By such optical TF transmissions, current satellite-based methods have been outperformed. The maximal precision of TF transmissions requires careful consideration of all contributing factors including the very small ones.

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