Nonlinear topological valley Hall edge states arising from type-II Dirac cones

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Abstract. A Dirac point is a linear band crossing point originally used to describe unusual transport properties of materials like graphene. In recent years, there has been a surge of exploration of type-II Dirac/Weyl points using various engineered platforms including photonic crystals, waveguide arrays, metasurfaces, magnetized plasma and polariton micropillars, aiming toward relativistic quantum emulation and understanding of exotic topological phenomena. Such endeavors, however, have focused mainly on linear topological states in real or synthetic Dirac/Weyl materials. We propose and demonstrate nonlinear valley Hall edge (VHE) states in laser-written anisotropic photonic lattices hosting innately the type-II Dirac points. These self-trapped VHE states, manifested as topological gap quasi-solitons that can move along a domain wall unidirectionally without changing their profiles, are independent of external magnetic fields or complex longitudinal modulations, and thus are superior in comparison with previously reported topological edge solitons. Our finding may provide a route for understanding nonlinear phenomena in systems with type-II Dirac points that violate the Lorentz invariance and may bring about possibilities for subsequent technological development in light field manipulation and photonic devices.

Keywords: photonic topological insulator; type-II Dirac cone; valley Hall edge soliton.

1 Introduction

Loosely speaking, topological insulators in condensed matter physics refer to materials that only allow electrons to conduct along the surface but not in bulk.1,2 The concept was introduced into the realm of photonics about a dozen years ago, and has since led to the burgeoning development in photonic topological insulators (PTIs)3–13 and topological photonics in general.14,15

Recently, nonlinear topological photonics has attracted increasing attention,16 as nonlinearity exists inherently in many photonic topological systems such as topological insulator lasers17–21 and nonlinearity-induced topological insulators.22,23 Topological solitons, for example, have been proposed in several photonic settings,24–31 which typically require breaking of the time-reversal-symmetry (TRS) by applying external magnetic fields or equivalently the z-reversal symmetry by nontrivial longitudinal modulation. Indeed, topological bandgap solitons were recently observed in the bulk of an anomalous PTI,32 which relied on a Kerr nonlinearity and periodic driving of anomalously coupled waveguide arrays.33,34

It is natural to ask if topological edge solitons can exist in a TRS-preserved system, or systems without complex modulation or external magnetic fields, which is essential for practical applications. For instance, coupling and locking of semiconductor laser arrays to produce coherent high-power laser sources is one of the key motivations behind the development of topological insulator lasers.17–21 The most promising approach could rely on PTI symmetry design,35 such as using the valley Hall effect36–39 without breaking the TRS. Relevant progress on photonic valley

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Hall effect can be found in a recent review. Indeed, it has been demonstrated that valley Hall edge (VHE) states can be used in topological laser fabrication and on-chip communications. Even though gap solitons were found in the Dirac model, VHE solitons have never been realized as they are completely different from all previously investigated solitons: the topological VHE soliton is an inheritor of the linear VHE state, so its appearance does not feature power threshold, in sharp contrast to those standard photonic bandgap solitons.

A general consensus is that many topological and valley Hall effects are mediated by materials with nontrivial degeneracy in momentum space, characterized by Dirac/Weyl cones. In the two-dimensional case, a well-celebrated example is graphene, in which electrons around the Dirac cones behave as massless Dirac fermions. Different from type-I Dirac cones in graphene where the corresponding Fermi surface is a point, there are also so-called tilted type-II Dirac cones with the Fermi surface being a pair of crossing lines. Type-II Dirac cones violate the Lorentz symmetry, thus allowing for quasi-particle-mediated phenomena that do not exist in high-energy physics analogically investigated in condensed matter physics. In photonics, for example, type-II Dirac cones are expected to bring new features due to their nonisotropic transport properties arising from the distinctive dispersions. Photonic lattices can be readily designed to possess such Dirac cones, making them attractive for investigation of nontrivial topological phenomena.

In this work, as one typical example, we propose and demonstrate experimentally a scheme to establish type-II Dirac photonic lattices in a nonlinear medium and, more importantly, to reveal the existence of topologically protected nonlinear VHE states. Such nonlinear VHE states in Dirac systems have inherited topological features from their linear counterparts, thus benefiting from easy implementation without any need of “time” modulation or external magnetic fields.

2 Principles and Methods

The propagation of a light beam in a photonic lattice is described by the Schrödinger-like paraxial wave equation:

\[ i \frac{\partial \psi(\xi, \eta, \zeta)}{\partial \zeta} = -\frac{1}{2k_0} \left( \frac{\partial^2}{\partial \xi^2} + \frac{\partial^2}{\partial \eta^2} \right) \psi(\xi, \eta, \zeta) - k_0 \Delta n(\xi, \eta) \psi(\xi, \eta, \zeta), \tag{1} \]

where \( k_0 = 2n_0 \pi / \lambda_0 \) is the wave number in the crystal with refractive index \( n_0 \). Note that \( \zeta \) in Eq. (1) plays the role of time in the quantum mechanics Schrödinger equation. For the specific photorefractive strontium barium niobite (SBN) crystal used in our experiment, we take

\[ \Delta n(\xi, \eta) = \frac{1}{2} n_0^3 \gamma_{33} E_0 \frac{1}{1 + I(\xi, \eta)}, \tag{2} \]

with \( I(\xi, \eta) \) being the intensity pattern of the lattice beam that is measured in units of the background illumination. The parameters corresponding to experiment are \( \lambda_0 = 532 \) nm, \( n_0 = 2.35 \), the bias field \( E_0 = 1 \) kV/cm, and the electro-optic coefficient \( \gamma_{33} = 280 \) pm/V. The photorefractive index change reaches typically \( \Delta n \sim 1.82 \times 10^{-4} \). In experiment the lattices are written point by point; the corresponding lattice intensity pattern can be considered as an appropriate superposition of Gaussian beams \( I(\xi, \eta) = \sum_{i=\{A,B,C\},m=1}^{3} \delta_i \exp\left\{-\left[(\xi - \xi_m)^2 + (\eta - \eta_m)^2\right] / \omega_i^2 \right\} \) in which \( \delta_i \) represents the beam amplitude, \( (\xi_m, \eta_m) \) is the beam center, \( A, B, C \) represent the lattice sites, and \( m \) is an integer. The distance between two nearest-neighbor sites is set to be \( d = 30 \) \( \mu \)m and \( w = 0.32d \). The diffraction length is \( L_\zeta = k_0 \rho_0 \), with \( \rho_0 = 12 \) \( \mu \)m representing the typical width of the experimental incident beam. If we replace \( \xi, \eta, \zeta \) by \( \rho_0 x, \rho_0 y, L_\zeta \), one obtains the dimensionless version of Eq. (1), which is

\[ i \frac{\partial \psi(x, y, z)}{\partial z} = -\frac{1}{2} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) \psi(x, y, z) - k_0 a \Delta n(x, y) \psi(x, y, z), \tag{3} \]

the solution of which can be written as \( \psi(x, y, z) = u(x, y) \exp(\pm i k \zeta) \) with \( \beta \) being the propagation constant and \( u(x, y) \) being the Bloch function. We would like to note that there is a minus sign in the solution, so that the sign of \( \beta \) is completely opposite if the solution without the minus sign is adopted. When nonlinearity is considered, the refractive index change is written as

\[ \Delta n(x, y, z) = \frac{1}{2} n_0^3 \gamma_{33} E_0 \frac{1}{1 + I(x, y) + |\psi(x, y, z)|^2}, \tag{4} \]

which is dependent on the beam intensity \( |\psi(x, y, z)|^2 \) upon propagation. With the nonlinear refractive index change, the solution can be written as \( \psi(x, y, z) = u(x, y) \exp(\pm i k \zeta) \) with \( \mu \) being the nonlinear propagation constant.

An exemplary type-II Dirac photonic lattice is displayed in Fig. 1(a) with \( \delta_i = 4 \), and its Brillouin zone (BZ) spectrum is shown in Fig. 1(b) in which the first BZ is indicated by the shaded hexagon. The design process of type-II Dirac photonic lattices can be found in the Supplementary Material. There are three sites in each unit cell of the type-II lattice, and they are labeled as A, B, and C in Fig. 1(a). Such a lattice can be considered as the direct outcome from properly stretching a dislocated Lieb lattice in the vertical direction. The experimental lattice structure and measured BZ spectrum shown in Figs. 1(c) and 1(d) match perfectly with the numerical results in Figs. 1(a) and 1(b). Moreover, we calculate the band structure of the type-II lattice as shown in Fig. 1(e) based on the plane-wave expansion method. Evidently, under proper lattice design, the bands are tilted and connected at some points—the type-II Dirac points, which are induced solely by the spatial geometry of the lattice. To see more clearly, we zoom in on one Dirac cone indicated by a red circle in Fig. 1(e), and let one horizontal plane (corresponding to the Fermi surface) go across the Dirac point. The intersection at the Dirac cone forms a pair of crossing lines in the momentum space [see the inset in Fig. 1(f)]—the characteristic feature of the type-II Dirac cone.
symmetry of the lattice will be broken. In Fig. 2(a), we intentionally increase the depth of site C from $\delta_C = 4$ to $\delta_C = 4.5$, and in Fig. 2(b), we increase the depth of site A from $\delta_A = 4$ to $\delta_A = 4.5$, while keeping that of other sites still at $\delta_I = 4$. The band crossings in the band structure indeed disappear as the gap opens, as shown in Fig. 2(c). We also display the calculated Berry curvature $\Omega$ of the first band in the $(k_x, k_y)$ plane shown in Fig. 2(d), with the red and blue colors representing the positive and negative values. The valley Chern number $C_v$ for each valley, which is $j = j/C_6$, can be numerically obtained from $\Omega(k_x, k_y)$ coordinates goes across the Dirac point and intersects with the Dirac cone to form a pair of crossing lines—a direct manifestation of the type-II Dirac cone.

3.2 Nonlinear Valley Hall Edge States and Quasi-Solitons

The appearance of topological edge solitons inherited from their linear counterparts strongly depends on the dispersion condition of the linear topological edge states.\(^{27}\) One may obtain bright solitons or dark solitons depending on the different dispersions for given self-focusing nonlinearity. Indeed, the inversion-symmetry-breaking perturbation lifts the degeneracy at Dirac points. However, the bands do not lose their symmetry properties around the Dirac points and affect the dispersions of the VHE states. According to our numerical analysis, the VHE states arising from type-II Dirac cones fulfill the dispersion condition ($\beta'' > 0$, i.e., the normal dispersive regime), which is a necessary condition for the existence of bright VHE solitons, but such a condition is not satisfied for the type-I Dirac photonic lattices. However, we do not claim that VHE solitons are not supported in lattices with type-I Dirac cones. In fact, the realization of VHE solitons from type-I Dirac cones is still an open question and merits further exploration. We thus solve for the first-order derivative $\beta'$ (group velocity of the edge state) and the second-order derivative $\beta''$ of the linear VHE state in Fig. 2(f), and the results are displayed in Fig. 3(a). Here the VHE state with $\beta' > 0$ moves along the positive $x$ direction. Notably, as shown in Fig. 3(a), the normal dispersion ($\beta'' > 0$) region is $\left(-0.235 \leq k_x/K \leq 0.235\right)$, where $K = 2\pi/d$ defines the width of the first BZ. By adopting the Newton method, we found a...
family of such nonlinear solutions; the peak amplitude \( a = \max \{|\psi|\} \) and power \( P = \iint |\psi|^2 \, dx \, dy \) of the nonlinear VHE states at \( k_x / K = 0.1 \) are plotted in Fig. 3(b) as a function of the nonlinearity-dependent propagation constant \( \mu \). One finds that both \( a(\mu) \) and \( P(\mu) \) decrease as \( \mu \) increases, reducing to nearly zero at \( \mu \sim 2.741 \) where the nonlinear localized states resemble or reduce to the linear ones.

Let us now examine the modulational instability (MI) of nonlinear VHE states under the action of self-focusing nonlinearity, which is possible since \( \beta'' > 0 \) at \( k_x / K = 0.1 \). To do so, we add a random noise to the nonlinear VHE state obtained at \( \mu = 2.736 \), with a noise amplitude about 5% of the nonlinear edge state shown in Fig. 3(c). Representative propagation of the peak amplitude \( a = \max \{|\psi|\} \) of the perturbed state is shown in Fig. 3(d). The amplitude profiles of the nonlinear edge state at two selected distances [marked by two red dots in Fig. 3(d)] are displayed in Fig. 3(c), showing growth of MI during propagation which leads to formation of quasi-soliton filaments along the DW. The larger the noise amplitude is (e.g., 10% of the nonlinear edge state), the faster the growth of the MI is, and the quicker the formation of quasi-soliton filaments. These MI-induced soliton filaments are considered as precursors for the formation of optical solitons, but here they also benefit from the topological protection inherited from the corresponding linear VHE states. Without loss of generality, we take out one of such bright filaments at \( z = 1750 \) [indicated by a red circle in Fig. 3(e)] as the input and investigate its long-distance propagation dynamics. To this end, we introduce another physical quantity—the barycenter of the filament defined as \( x_c = P^{-1} \iint x |\psi|^2 \, dx \, dy \)—to record its movement during propagation. We first shift the selected filament in Fig. 3(c) to the center of the window \( (x = 0) \) and then track its propagation. The peak amplitude and barycenter of the filament are displayed in Fig. 3(e), showing the stability of a moving VHE quasi-soliton. Even over an extremely long propagation distance \( (z \sim 32,000) \), the peak amplitude remains nearly invariant and the barycenter exhibits a saw-tooth-like oscillating behavior. The appearance of the saw-tooth behavior in the center of mass of the wavepacket is mainly due to the simulation method (the split-step Fourier method) we adopted: for a chosen window along \( x \), part of the transporting VHE quasi-soliton appears at the left end of the numerical window when it reaches the right end, resulting in an apparent periodic jump of the barycenter between two ends. The same reason holds for the panel with \( z = 1000 \) in Fig. 3(g). In Fig. 3(f), snapshots of the quasi-soliton taken at different propagation distances are displayed. We observe clearly that the quasi-soliton moves along the positive \( x \) direction with a constant speed (it is same as \( \beta' \)), and it remains localized with negligible radiation loss either along the DW or into the bulk—a result of interplay between nonlinearity and topological protection. For direct comparison, we propagate the same input filament in the linear lattice, i.e., removing the nonlinear term \( |\psi|^2 \) in Eq. (4). As expected, without the balance from the nonlinearity, the filament spreads quickly along the DW because of diffraction [see Fig. 3(g)], yet remains localized in the direction perpendicular to the DW. Here we only discuss the case of VHE solitons with \( \mu = 2.736 \), but the approach and analysis also apply to other parameter cases.

Fig. 2 Linear topological VHE states at the DW between two type-II Dirac cone photonic lattices. (a) and (b) Inversion-symmetry-broken photonic lattices with the depth of site C and site A increased, respectively. (c) Band structure corresponding to the lattice in (a) [which looks the same for the lattice in (b)]. (d) Berry curvature of the first band displayed in the \((k_x, k_y)\) plane. The top panel corresponds to (a); the bottom panel, which is opposite, corresponds to (b). The dashed hexagon represents the first BZ. (e) A DW is established by combining (a) and (b) with an interface, highlighted by a green rectangle. The lattice is periodic along the \( x \) direction but has boundaries along the \( y \) direction. (f) Band structure of the lattice in (e); the red curve represents the topologically protected VHE state along the DW. In panels (a), (b), and (e), blue and red spots represent the lattice sites with different detunings.
Since there is no power threshold for the nonlinear VHE state [see the continuous peak amplitude and power curves in Fig. 3(b)], the corresponding quasi-soliton possesses a higher intensity if it bifurcates from the nonlinear VHE state with a larger amplitude. Since the nonlinearity can induce a defect in the topological structure, the topological property will be broken if the strength of the defect is larger than the bandgap width. From this point of view, one cannot seek for the VHE solitons with very high intensity. In the region with $\mu > 2.736$, the obtained solitons have a smaller peak amplitude and intensity. It is impossible to design corners for the DW of type-II Dirac photonic lattices due to the spatial symmetry, yet artificial corners can play a role of disorder but would result in intervalley scattering due to weak valley protection. Such issues are further addressed in the Supplementary Material, where we use a large-scale random disorder to check the robustness of the quasi-soliton over extremely long distances, as seen also in the intensity pattern snapshots (f) during transport. (g) Spreading of the same input at $z = 0$ as in (f) along the DW during linear propagation for comparison. (Here, $z = 1000$ corresponds to a physical distance 4 m.)

3.3 Experimental Observation of Nonlinear Valley Hall Edge States

In the experiment, an inversion-symmetry-broken type-II Dirac photonic lattice with a DW [corresponding to Fig. 2(e)], as shown in Fig. 4(a1), is established by employing the CW-laser-writing technique (similar for writing the uniform lattice in Fig. 1(c) but with a judiciously controlled writing process). The technique relies on writing the waveguides site-by-site in a 10-mm-long nonlinear photorefractive crystal (SBN:61 with cerium doping: 0.002% CeO$_2$). The experimental setup (more details about the setup can be found in the Supplementary Material) involves a continuous wave laser beam ($\lambda = 532$ nm) to illuminate a spatial light modulator, which creates a quasi-non-diffracting writing beam with variable input positions. Because of the noninstantaneous photorefractive "memory" effect, all waveguides remain intact during the writing and the subsequent probing processes. After the writing process, the lattice structure can be examined by sending a broad beam (quasi-plane-wave) to visualize the whole lattice. Once the structure is established, the probe beam is used to excite the lattice along the DW, and it can undergo either linear propagation (when the bias field is turned off) or experience a self-focusing nonlinearity under a positive bias field. Of course, the probe beam can locally change the index structure of the lattices due to its self-action during nonlinear propagation—the ingredient needed to study the nonlinear effects experimentally.

To appreciate the formation of nonlinear VHE states presented in Fig. 3(e), two out-of-phase elliptical Gaussian beams (due to the property of the VHE state that has a staggered phase structure along the $y$ axis) are superimposed as a probe beam with an input power of only 3 $\mu$W, whose position is marked by the white dashed oval in Fig. 4(a1). The linear and nonlinear
output intensity patterns in real space and their corresponding spectra in momentum space for three different excitation conditions (e.g., with Bloch momentum $k_x/K = -0.3, 0, +0.3$) are shown in Figs. 4(b)–4(d). When the bias field is off, the probe beam itself does not exhibit nonlinear self-action, but it is localized in the vertical direction without spreading into the bulk due to the excitation of the linear VHE states, although somewhat extended along the DW after 1 cm of propagation. However, the probe beam undergoes self-focusing when the bias field is turned on (0.7 kV/cm) and, as a result, the corresponding nonlinear output also becomes more localized along the DW direction [Figs. 4(b2)–4(d2)]. This can be seen more clearly from the overall beam width (full width at half maximum (FWHM)), which decreased approximately from 100 μm (linear case) to 80 μm (nonlinear case) [Figs. 4(e2)–4(e4)]. Interestingly, we found that the output pattern moves slightly to the left (right) even in the linear condition for the Bloch momentum $k_x/K = -0.3 (0.3)$, thanks to the initial transverse velocity of the VHEs, while that for $k_x = 0$ remains invariant [Fig. 4(e1)]. Due to the nonlinear action, an appreciable portion (about 20%) is “diminished” from the initial position of the probe beam (marked by a solid ellipse) as compared with the linear case. This is a direct signature of nonlinearity-induced transport of the VHEs. Indeed, by using the barycenter of the beam defined earlier, and plotting the superimposed linear and nonlinear output profiles along the $x$ direction [Figs. 4(e2)–4(e4)], we can see clearly that the center is further shifted away from the initial input position under nonlinear propagation. Furthermore, nonlinearity-induced spectral reshaping is evident due to formation of nonlinear VHEs by comparing nonlinear [Figs. 4(b4)–4(d4)] with linear [Figs. 4(b3)–4(d3)] output spectra. Our results indicate that self-trapped nonlinear VHE states indeed exist in type-II Dirac photonic lattices. Due to the limited crystal length, it is not feasible to experimentally show the long-distance transport of the quasi-solitons as demonstrated in our theoretical analysis. However, these experimental results in Fig. 4 are corroborated by numerical simulations, as detailed in the Supplementary Material. Here we would like to note that the waveguide is assumed uniform without appreciable losses along the propagation direction. Thus the transmission efficiency is nearly invariant for the probe beam.

### 4 Discussion and Conclusion

We have proposed and experimentally demonstrated photonic lattices exhibiting type-II Dirac points, thereby unveiling the existence of nonlinear VHE states and the formation of topological quasi-solitons. We have shown theoretically that it is crucial to have the type-II Dirac dispersion and a DW between two lattices of opposite Berry curvatures in order to achieve self-
trapping of the VHE solitons in the TRS-preserving topological systems. We would like to note that the nonlinear experiments with topological VHE states may also be implemented in femtosecond laser writing photonic lattices, now that optical nonlinearity has been demonstrated in such a platform.\cite{22,23,25} We believe that our results may prove relevant to other type-II systems such as nonlinear effects and high-frequency rectification in type-II topological semimetals\cite{26} and may also enlighten new ideas in nonlinear non-Hermitian topological systems.\cite{27}

Moreover, there is still a plethora of interesting topics yet to be explored in nonlinear systems that could involve type-II Dirac points, including higher-order topological phases\cite{28,29,30} new physics arising from engineered longitudinal modulation,\cite{31,32} and even the innovation of topological semiconductor laser technologies.\cite{15,16,20}

Thus, our work on nonlinear VHE states in engineered type-II lattices will surely stimulate further interest in topological photonics—an area that will continue to grow in the next decade.\cite{33}

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References


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