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Abstract. We adapted the critical angle method for measuring rough surfaces under partial contact to acquire an \textit{in vivo} skin refractive index (RI). Assuming that the total reflection is the simple sum of reflection from areas that are in contact and reflection from those that are not in contact, the RI can be estimated even for partial contact with a rough surface. We found that cheek skin is sufficiently soft that a sufficiently large area can be in contact and that the critical angle was detectable. The RIs of the cheeks of adult females were measured. The RI range was about 1.51 to 1.53, at a wavelength of 550 nm, without considering systematic errors. The RIs of cheeks are significantly correlated with their conductance, which corresponds to their water content. We determined the relationship between the RI and conductance within the variation of skin under normal conditions; this relationship was theoretically obtained in previous studies. In the present study, a direct \textit{in vivo} measurement method was developed that enabled us to measure the RI in daily life, although this method contains errors for several reasons, including disregarding absorption.

Keywords: refractive index; skin surface; critical angle method; total reflection; water content; partial contact; rough surface; refractometry.

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1 Introduction

The refractive index (RI) of skin is an important parameter that indicates the condition of skin. It also defines the characteristics of light reflection from skin. Therefore, it has been recognized as an important parameter in applications such as laser therapy\textsuperscript{1} and cosmetics.\textsuperscript{2} Various methods have been developed for measuring RI. Methods for measuring skin RI can be broadly categorized into two kinds based on their measurement area and depth. One class of methods measure the average RI between two interfaces (e.g., the upper and lower surfaces of the epidermis); they utilize the difference between the physical and optical distances between the interfaces.\textsuperscript{3,5} The other class of measurements measures the RI of an area close to a surface and utilizes the relationship between the incident angle and the reflectance.\textsuperscript{6-12} In the case of \textit{in vivo} measurements of skin, the measurement depth is important because the amount of water varies dramatically with depth, and it generates a gradient in the RI with depth.\textsuperscript{13,14} In measuring the behavior of light at the skin-incident angle and the reflectance,\textsuperscript{6-12} the latter class of measurements is more appropriate since those measurements are considered to be sensitive to the ratio of surface reflection to interior reflection.\textsuperscript{1,2,15}

The ultimate goal of our research is to measure \textit{in vivo} the RI of a superficial area of a corneal layer. However, since this is difficult, most studies have performed \textit{ex vivo} measurements of slices of skin.\textsuperscript{16-12} The main source of difficulty of \textit{in vivo} measurements is undulations in the skin surface.\textsuperscript{16} RI measurements generally require precise measurement of the reflectance as a function of the incident angle at the interface between a prism and a sample. Consequently, a flat sample surface is needed to ensure good contact between the prism and the sample. Hence, some modification is required to apply this method to samples with rough surfaces. In some studies, the sample was pressed against the prism with great pressure so as to achieve good contact.\textsuperscript{11,12} However, this method is not suitable for \textit{in vivo} measurements. Another significant problem of \textit{in vivo} measurements is their long acquisition time, which is inconvenient for the subject. Furthermore, skin conditions will change over time since the water content varies due to occlusions. Due to these difficulties, almost all previous studies performed \textit{ex vivo} measurements of skin slices, but doing this causes other problems. First, this method is destructive. In addition, after being cut off, skin will dry out since its water supply is disrupted, and that changes its RI.\textsuperscript{1,17} To make the conditions of samples close to those of living skin and to increase the contact area, other studies have used saline\textsuperscript{10-12} or high-RI immersion oil.\textsuperscript{17} However, various kinds and amounts of liquid are applied, and these factors will affect the RI. Therefore, \textit{in vivo} measurements are desirable for evaluating the RI under different conditions and for different individuals.

In this report, we modify the critical angle method for partial contact to realize \textit{in vivo} measurements of the RI of skin. We then evaluate the feasibility of this method by performing \textit{in vivo} measurements of silicone samples and human skin. We also discuss the effect of absorption, which is disregarded in the proposed method.
2 Materials and Methods

2.1 Critical Angle Method for Partial Contact

The critical angle method is commonly used to take an accurate measurement of the RI of liquids, but it assumes that no absorption occurs and that there is total contact between the probe and sample. Assuming that light is incident on the interface from a medium with an RI of \( n_i \) to a medium with an RI of \( n_t \), the reflectance will be 1 for incident angles larger than or equal to the critical angle:

\[
\theta_c = \sin^{-1}(n_i/n_t),
\]

where \( n_i > n_t \). On the other hand, the reflectance decreases rapidly as the incident angle decreases from the critical angle. This allows the critical angle to be determined easily and precisely, especially for \( p \)-waves. In the critical angle method, the RI of a sample \( n_s \) is determined from Eq. (1) using a prism with a known RI of \( n_t \) and measuring \( \theta_c \). This method is not usually used for solid materials with rough surfaces since partial contact makes \( \theta_c \) indistinct.

Here, we assume that the reflection for a prism can be expressed as a simple sum of reflections from areas that are in contact and reflections from areas that are not in contact. In this case, the variation of the reflectance near the critical angle will be indistinct due to mixing of light reflected from areas in contact and from areas that are not in contact. However, the critical angle still exists. Since the RI of air \((n \approx 1)\) is much smaller than that of skin \((n \approx 1.33)\), the reflectance from a noncontact area will be 1 when the incident angle is near the critical angle of skin. Based on the above assumption, the reflectance \( R \) can be expressed as a function of the incident angle as

\[
R(\theta_i) = A \cdot r(\theta_i) + (1 - A).
\]

Here, \( \theta_i \) is the incident angle, \( r(\theta_i) \) is the reflectance of an area where there is contact, and \( A \) is the ratio of the contact area to the total area. The first and second terms in Eq. (2) correspond to areas in contact and areas not in contact, respectively. The Fresnel equation can be substituted for \( r(\theta_i) \). According to Eq. (2), even when there is partial contact between the prism and the sample, the critical angle can still be determined provided that \( A \) is sufficiently high. Since human skin is flexible, this condition is achievable.

2.2 Measurements and Data Analysis

The instrument shown in Fig. 1 was used for RI measurements. Light from the light source (LA-180Me, Hayashi Watch-Works, Tokyo, Japan) passes through a bandpass filter (43178-H, Edmund Optics, Barrington, New Jersey; center wavelength: 550 nm; full width at half maximum: 10 nm) and an aperture. Then it is spread out by a diffuser, and is collimated by two convex lenses before it strikes the equilateral-triangular prism (SFL11, Edmund Optics; RI at 550 nm: 1.791). It illuminates a sample after passing through the prism. The light spot on the sample was about 5 mm in diameter. A polarizer was inserted between two convex lenses to generate a \( p \)-wave. The reflected light was recorded by a camera (D200, Nikon, Tokyo, Japan) with an attached lens (Ai Nikkor, Nikon; 50 mm f/1.2S). The focal point of the lens was set at infinity, so each position of the acquired image can be associated with each incident angle. The exposure time was set to 1/5 s, and the aperture was set to f/1.2. The prism and the camera could be rotated independently about the center of the prism to allow for variations in RI; their positions varied according to the sample used (i.e., silicone or skin).

From the images taken with the system shown in Fig. 1, the correlation between the reflectance and the incident angle was obtained. Below, the protocol is explained using data from Experiment 1. First, images without a sample (when the prism is contact with air) and images with a sample were obtained. They were saved as raw data (12 bits/pixel/channel) and then converted to Tagged Image File Format (TIFF) images (16 bits/pixel/channel) whose pixel values vary linearly with the light intensity (Fig. 2). The difference between adjacent pixels was approximately 0.004 deg in incident angle. The pixel values along the horizontal center line (see Fig. 2) were extracted. Next, the reflectance was derived by dividing the pixel values by the corresponding pixel values in the image obtained without a sample (i.e., pixel values when the reflectance is unity). The repeatability error of the pixel value was evaluated from duplicate measurements of air (the condition shown in Fig. 2(a)). and the standard deviation (SD) of the reflectance was found to be 0.15%.

![Schematic of the measurement system.](image-url)
Using the relationship between the incident angle and the pixel position, a plot of reflectance against incident angle was obtained [Fig. 3(a)]. The relationship between the incident angle and the position in the image was determined from data obtained in advance by performing measurements using an RI-matching liquid (Cargille Laboratories, Cedar Grove, New Jersey). From the position of the critical angle of liquids, the incident angle was correlated with the horizontal axis in the images by making a linear approximation.

A profile of reflectance against incident angle was approximated by two lines [Fig. 3(b)] with tangents of $p_1$ and $p_2$ that are connected at the point $(X_C, Y_C)$:

$$
\begin{align*}
    \text{if } x < X_C: & \quad y = p_1 \cdot (x - X_C) + Y_C \\
    \text{else:} & \quad y = p_2 \cdot (x - X_C) + Y_C
\end{align*}
$$

(3)

$X_C$ was taken to be the critical angle. The four parameters $X_C$, $Y_C$, $p_1$, and $p_2$ were calculated from the profile as an optimization problem. Specifically, the “fminsearch” function in MATLAB software (Mathworks, Natick, Massachusetts) that implements the Nelder-Mead simplex method was used. The area to be fixed was defined visually. Although Eq. (2), in which the Fresnel equation is substituted for $r(\theta)$, is theoretically rigorous, the optimization problem did not converge well. This is probably due to several errors and the degrees of freedom of $A$, which make the prediction ambiguous. In the approximation, the estimation of $X_C$ will not be affected by $A$, which can be confirmed by substituting Eq. (3) for $r(\theta)$ in Eq. (2). Furthermore, $X_C$ will not be affected by fluctuations in the light source intensity, provided the fluctuation percentage is constant.

### 2.3 Silicone Samples

Silicone samples with flat and rough surfaces were prepared using a transparent, room-temperature-curing silicone resin [KE-108 (condensed); Shin-Etsu Silicones, Tokyo, Japan] as a base. A catalyst (CAT-108, Shin-Etsu Silicones) was added to KE-108, and the mixture was poured into a mold. Rough surfaces were formed by taking the topography of the surface of the forearm of a 38-year-old male using polyether impression material (Impregum Soft, Sumitomo 3M, Tokyo, Japan) and using it as a part of the mold to imitate the topography of actual skin. The RI obtained by the dipping method was $n_D = 1.41 \pm 0.01$.

### 2.4 Conductance (Water Content) Measurements

The conductance, which is expected to reflect the water content\textsuperscript{19,20} was measured using a Skicon 200 EX instrument (IBS, Shizuoka, Japan) along with RI. In addition to the conductance method, capacitance measurements are considered to be a straightforward method for evaluating moisture content\textsuperscript{19,20}. However, conductance measurements are more suitable than capacitance measurements in the present case since conductance depends more on the water content of shallower regions than does capacitance\textsuperscript{19,20}.

### 2.5 Experiment 1: Silicone Samples

The RIs of silicone samples with flat and rough surfaces were measured to verify the assumption stated in Sec. 2.1. Each area was measured several times, and the average was taken.
2.6  Experiment 2: In Vivo Measurements of Human Skin (Cheek)

The left and right cheeks of Japanese adult females (n = 16) in their 20 to 40 s were measured. After removing makeup and washing her face, each subject remained in a controlled room (temperature: 20°C; relative humidity: 40%) for over 20 min. The conductance and RI of the left and right cheeks were then measured. Each site was measured five times, and the average was taken.

3  Results

3.1  Experiment 1: Silicone Samples

From the acquired images (Fig. 2), the intensity of the reflected light was derived as a function of the incident angle. Then it was converted to reflectance [Fig. 3(a)] and fitted using Eq. (3) [Fig. 3(b)]. The profile shown in Fig. 3 represents the average of multiple measurements. The number of measurements performed for flat and rough surfaces are 10 and 37, respectively. The RIs of the flat and rough surfaces were calculated to be 1.407 (SD = 4.9 × 10⁻⁵) and 1.408 (SD = 3.6 × 10⁻³), respectively (Fig. 4). These average values are very similar, while the SD of the rough surface is larger than that of the flat surface.

3.2  Experiment 2: In Vivo Measurements of Human Skin (Cheek)

Figure 5 shows a representative example of the profile of human skin (cheek) and the result of fitting. This representative profile was compared to Eq. (2), obtained using the Fresnel equation with complex RIs (N = n + ik) and varying k [Fig. 6(a)]. Here, n was set to the estimated RI, and A was visually selected to make the range of the theoretical profile fit the range of the measured profile. The value of k that gave the closest profile to the measured profile (in terms of sharpness of the shoulder) was 0.004. A representative profile was compared to Eq. (2), with k = 0.004 varying n [Fig. 6(b)]. The value of n for the closest profile to the measured profile near the shoulder was 1.513.

RI was plotted against the conductance at each site (i.e., two points on the left and right cheek of each subject) (Fig. 7). There is a significant correlation between the conductance and RI, at a 99.9% confidence level.
4 Discussion and Conclusions
The critical angle of the rough surface is indistinct due to partial contact [Fig. 2(e)], but it was still recognizable (Fig. 3). From the profiles, RIs were derived for partial contact with the rough surfaces, although the SD was greater than that for the flat surface, which had better contact (Fig. 4). This result indicates that the critical angle method can be used for rough silicone surfaces, provided that a sufficiently high proportion of the area is in contact and that the material has a low absorption.

As shown in Fig. 5, in the in vivo measurements of cheek skin, the RIs were measured in the same manner as for the silicone sample sites. In other words, a sufficiently high contact area for the RI measurement was confirmed by getting each subject to press the measurement site against the prism. A short acquisition time was realized, which reduces problems associated with time-varying conditions such as skin surface deformation and water content variation due to occlusions. From Fig. 7, the RI range was about 1.51 to 1.53, which is relatively higher than those of previous studies (which are less than 1.5).10–12

This is probably due to the skin surfaces being relatively dry in our experiment. Although the present experiments were performed using a p-wave, a previous study indicated that the anisotropy is small.11

Assuming the discrepancy between the theoretical and measured profiles is only due to absorption, we estimated the effective absorption by extending RI to complex RI. The imaginary part k of complex RI is visually estimated to be about 0.004 from the sharpness of the shoulder in the profiles shown in Fig. 6(a). Although the sharpness of the shoulder can be changed by varying A in Eq. (2), this will also alter the reflectance range so that the profile will not be close to the measured profiles. For the measured site in Fig. 6(b), the RI value is possibly overestimated by about 0.008. Although earlier studies found that the epidermis has a higher absorption (k = 0.02),11,12 the actual value may be smaller than that determined from plots of the actual reflectance against the incident angle, which are sharper than the fitting results shown in the studies.11,12 Since other causes may smooth the profile of the reflectance against the incident angle, our estimate may represent an upper limit for k.

The RI is significantly correlated with the conductance, which depends on the water content19,20 (Fig. 7). The water content is expected to affect the RI greatly because the RI of water (1.33) differs significantly from that of dry tissue (≈1.5).1 The water content is known to vary between sites and individuals.21 Although the sebum is also a variable factor, it is not expected to affect the RI measurements greatly because the sebum at the measurement sites is expected to be washed away by washing the skin. To the best of our knowledge, this is the first time that a correlation between these two parameters has been observed above the natural variation, although the relationship has been theoretically predicted in previous studies.1,13

From this result, we estimate the RI from conductance C (μS) using the formula RI = 1.529 – 3 × 10⁻³C, without considering systematic errors. Alternatively, we can use RI = 1.521 – 3 × 10⁻³C by assuming that the offset of 0.008 from the results of the above discussion can be applied to all subjects. This formula for the conductance varies between measurement devices; the above formula is unique to Skicon 200 EX.

Despite being a straightforward and well-studied method for estimating the water content in skin,19,20 the conductance method has some problems, the most serious of which is the contact resistance between the skin and the probe, which affects the conductance. An increase in the contact area will reduce the contact resistance and hence increase the measured value. In future studies, the relationship between RI and the water content should be determined by direct methods that are insensitive to the contact ratio, such as confocal Raman microscopy.13,21 Other factors such as temperature and dielectric substances are considered to be suppressed since the room temperature was controlled and the measurement sites were cleaned prior to the measurements.

This method can be applied to other wavelengths by using bandpass filters for different wavelengths. However, we used a single wavelength in the present study for the stable measurement because replacing the filter prolongs the measurement time and makes it difficult to perform quick measurements. This problem can be overcome by improving the system design.

The derivation of θc from these profiles has the potential to be improved in future studies. Theoretically, the profile should be fitted by the Fresnel equation with a complex RI6,7,10–12 RIs have been measured in this manner in recent studies.10–12

We also tried this method but found that it did not work well, which is probably due to errors from other sources. An alternative method has been proposed that involves detecting the maximum of the first derivative.22 Although detection is difficult, this method is worth considering since it seems to be more robust against absorption than our method.22

There are some other probable causes of errors in the present measurement method. First, there may be multiple reflections in the prism and in the skin, which would reduce the angular resolution. In most previous studies, the effect of stray light from other incident angles was nullified by performing successive measurements at different incident angles.8,9,11,12 Simultaneous measurements in the present method are essential for realizing a short measurement time, but they adversely affect the angular resolution. A second potential source of errors is intermediate regions between contact and noncontact areas. Although we assumed a binary condition in Eq. (2), the gap between the prism and the sample changes vary continuously between contact and noncontact areas. In intermediate regions, the light behavior will differ from that of either contact or noncontact areas due to the effect of evanescent waves.23 In addition to these errors, the RI may vary on the surface because the stratum corneum is composed of materials with different RIs, including lipid, water, and cell membrane. As Fig. 5 shows, the profiles of some subjects exhibit a plateau (about 57 deg for this figure), which implies such a composition.

This method assumes that deformation of the skin will provide a sufficiently high contact area to enable the critical angle to be determined. However, skin deformability and topography varies between sites, individuals, and conditions (e.g., water content). Consequently, the method will not always give valid results. As a preliminary study, we show a representative profile of the inner side of a forearm along with that of a cheek (Fig. 8). The folding point of the forearm gives more ambiguous results than the cheek; this is probably due to the smaller contact area and the stronger absorption. In fact, the estimation for the forearm profile performed in the same manner as the cheek profile indicated A ≈ 0.09 and k ≈ 0.02, which is smaller and larger than the values for cheek, respectively. The cheek is more measurable than the forearm due to its greater deformability and lower absorption, making detection of the folding point easier.
We found that the critical angle method is applicable to cheek skin, provided that there is a high contact ratio and low absorption. In addition, we explained the variation in the RIs of individuals in terms of water content using the critical angle method, which suggests that the method is sufficiently accurate for detecting the variation under normal conditions (at least relatively). Although measurable sites are currently limited to the cheek, it is anticipated that the application range of this method can be extended by improving the method.

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