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Abstract. We investigate the effect of tissue fluid on the measurement of complex refractive index (RI) of animal tissue. A new model is proposed and verified through experimental results of simulation samples made of glycerol and methyl-red-doped poly(methyl methacrylate). Coupled with polarized optical reflectance measurements performed on several kinds of animal muscle tissues, RIs were resolved using the new model. We find that the tissue fluid existing at the prism-sample interface is unavoidable. We also find that with a change of proportion of the tissue fluid, the RI of muscle tissue can still be measured using the new model. © 2012 Society of Photo-Optical Instrumentation Engineers (SPIE). [DOI: 10.1117/1.JBO.17.7.075011]

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1 Introduction

The complex refractive index (RI) can be defined in terms of a real part and an imaginary part as \( n = n_r + i\kappa \), where \( \kappa \) means the extinction coefficient. In the field of near-infrared tomography, fluorescence diagnosis, laser surgery, and photodynamic therapy (PDT), it is vital to know the precise value of RI.\(^1\)\(^\text{-}^3\) It has been proven that the RI value affects average diffuse intensity solved by the radiative transfer equation and the calculation of other optical parameters of biotissue, namely the absorption coefficient \( \mu_a \), the scattering coefficient \( \mu_s \), and the anisotropy factor \( g \)\(^4\)\(^\text{-}^6\).

The total internal reflection (TIR) method is recommended to have the highest precision for RI measurements of animal tissue and has been investigated by different groups worldwide.\(^7\)\(^\text{-}^1^1\) The excellent work of Ding et al. first introduced the dual-parameter fitting method to obtain \( n_r \) and \( \kappa \) of skin tissue by nonlinear fitting simultaneously.\(^1^2\) The modified version of the TIR method, named the extended derivative total reflection method (EDTRM),\(^1^3\) has recently been applied to the measurement of biotissue and a series of tissue-mimicking phantoms. Using EDTRM, \( n_r \) is directly determined by the derivative of the reflectance curve and \( \kappa \) is obtained from nonlinear fitting.

In the former research, RI is usually treated as the ‘average value’ of tissue fluid and muscle tissue. Bolin et al. resorted to homogenization by a blender and believed that the liquid expressed from homogenate has a similar RI with the overall tissue.\(^9\) Most of the other researchers applied pressures on the tissue sample to eliminate the air gap and tissue fluid between the prism and the tissue,\(^9\)\(^\text{-}^1^3\) while neglecting the role of tissue fluid. Actually, a close relationship between the increase of tissue fluid and the reduction of the local chromophore concentration as well as the scattering coefficient has been proven by a prior study.\(^1^4\) Is there any method to obtain more accurate RI of muscle tissue in the presence of tissue fluid.

In this paper, we discover that the existence of the tissue fluid at the prism-sample interface is unavoidable in the measurement and has an important effect on the determination of RI of animal muscle tissue. The contacting area of the tissue sample consists of tissue fluid and muscle tissue. A new model based on EDTRM is proposed to explain the significant information revealed by the measured results. In order to verify the new model, a simulation sample made of glycerol and methyl-red-doped poly(methyl methacrylate) (MR-PMMA) is measured. Then we applied the new model for the measurement of fresh porcine, chicken breast, and ovine muscle tissues. During the laborious preparation and measurement of tissue samples, we find that a compromised pressure that is between eliminating partial tissue fluid and avoiding damage to the intrinsic properties of the tissue sample is needed in sample preparation. We also find that with a change of the proportion parameter of the tissue fluid, the RI of muscle tissue can still be measured using the new model.

2 Material and Method

The experimental setup for reflectance measuring is schematically shown in Fig. 1, which is similar to that of Ref. 13. A He-Ne laser (632.8 nm) is used. M is a beam splitter. H is a half-wave plate. P is the polarizer. PD1 and PD2 are the two detectors of a dual-channel power meter (PM320E, Thorlabs, New Jersey). The aperture size of the photodiode sensor (S130C, Thorlabs, New Jersey) is 9.5 mm, so we used an aperture diaphragm D with diameter of about 5 mm to eliminate the scattering light and parasitic light. An equilateral triangular prism is fixed on a rotation stage (M-038, Physik Instrumente, Karlsruhe, Germany).

According to the schematic diagram in Fig. 1, \( n_r \) can be solved by
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\[ n_r = n_1 \sin(\beta \pm \sin(\alpha_c / n_1)) \], \hspace{1cm} (1)

where \( \alpha_c \) is the critical incident angle when TIR occurs at the prism-sample interface. According to the Fresnel formula, the reflectance at the prism-sample interface for a transverse electric (TE) wave \( R_{1,2} \) can be expressed as

\[ R_{1,2} = \frac{(n_1 \cos \theta - u_2)^2 + \nu_2^2}{(n_1 \cos \theta + u_2)^2 + \nu_2^2}, \hspace{1cm} (2) \]

\[ 2u_2^2 = n_r^2(1 - \kappa^2) - n_1^2 \sin^2 \theta 
+ \sqrt{[n_r^2(1 - \kappa^2) - n_1^2 \sin^2 \theta]^2 + 4n_1^2n_r^2\kappa^2}, \hspace{1cm} (3) \]

and

\[ 2\nu_2^2 = -n_r^2(1 - \kappa^2) - n_1^2 \sin^2 \theta 
+ \sqrt{[n_r^2(1 - \kappa^2) - n_1^2 \sin^2 \theta]^2 + 4n_1^2n_r^2\kappa^2}, \hspace{1cm} (4) \]

where parameters \( u_2 \) and \( \nu_2 \) are the intermediate variables. The reflectance at the air-prism interface \( R_{2,3} \) can be expressed as

\[ R_{2,3} = \left\{ \frac{\cos \alpha - n_1 \cos[\sin(\alpha / n_1)]}{\cos \alpha + n_1 \cos[\sin(\alpha / n_1)]} \right\}^2. \hspace{1cm} (5) \]

When emergent light leaves the prism and enters into air, the reflection loss is approximately equal to the loss at the incident air-prism interface. The final measured reflectance \( R_s \) detected by PD2 should include the loss between the two interfaces mentioned above, which is

\[ R_s = R_{1,2} \times (1 - R_{2,3})^2. \hspace{1cm} (6) \]

By measuring the reflectance curves of the sample, \( \alpha_c \) is obtained at the angular position of the derivative maximum of reflectance curve. \( n_r \) is calculated by Eq. (1). There are similar equations for a transverse magnetic (TM) wave.

Using Eq. (6), we found a large distortion between experimental data of animal tissues and theoretical fitting. Taking into account of the tissue fluid, Eq. (6) is modified by a new model as

\[ R_{s1}^+ = b_1 R_{s1} + b_2 R_{s2}, \hspace{1cm} (7) \]

where \( R_{s1} \) and \( R_{s2} \) are the reflectance from tissue fluid and muscle tissue surface, respectively; \( b_1 \) and \( b_2 \) are the proportion parameters of the tissue fluid and the muscle tissue at the illuminated areas, \( b_1 + b_2 = 1 \). \( n_r \) of the muscle tissue is determined by the second angular position of the derivative maximum of the reflectance curve. Using Eq. (7) and a nonlinear fitting program based on the Nelder-Mead simplex algorithm, \( \kappa, b_1, \) and \( b_2 \) can be resolved by minimizing the sum

\[ S(N) = \sum_{i=1}^{N} (R_{s,i} - R_{s,i}^+)^2, \hspace{1cm} (8) \]

where \( R_{s,i} \) is the \( i \)th measured reflectance. \( R_{s,i}^+ \) is the \( i \)th calculated reflectance obtained by Eq. (7).

The reliability of fitting are described by \( E_s^2 \), defined as

\[ E_s^2 = 1 - \frac{\sum_{i=1}^{N} (R_{s,i} - R_{s,i}^+)^2}{\sum_{i=1}^{N} (R_{s,i} - \bar{R})^2}, \hspace{1cm} (9) \]

where \( \bar{R} \) is the mean value of the measured reflectance over \( N \) values of incident angle. The value of \( E_s^2 \) ranges from 0 to 1 and it’s closer to 1 when we obtain a reliable fitting.

According to the normal sample preparation procedure of animal tissue for RI measurement, fresh porcine tissue was frozen for 30 min first and then sliced to a thin section of about 5 mm thickness. After 15 min, the surface of tissue was cleaned with alcohol to reduce the influence of condensation. The sample was pressed on the surface of the prism to make sure no air gap exists and some tissue fluid exudates at the interface. Fresh chicken breast and ovine muscle tissue were prepared the same way as the porcine sample. Each sample was continuously measured five times to calculate the standard deviation. In order to get the RI of pure tissue fluid, we picked up some tissue fluid by pressing heavily on the fresh porcine tissue and measured it.

Since the proportions of tissue fluid and muscle tissue at the prism-sample interface are variable for different types of tissues and conditions, we made a simulation sample to simulate the reflection of tissue and verify the new model. The simulation sample is made of two materials with known \( n_r \) and \( \kappa \): the glycerol (1.4709 ± 0.000014i) and MR-PMMA (1.5205 ± 0.000571i). The choice of these two materials is according to the difference between their RIs, which is close to the difference between the tissue fluid and the muscle tissue. The front and right side views of the cross section of the simulation sample are schematically shown in Fig. 2(a) and 2(b). For the simulation sample fabrication, methyl-red and PMMA (with a weight ratio of about 3%) were first dissolved in cyclohexanone separately and then mixed together. After stirring for 30 min, the mixture was poured carefully on the one surface of the prism. After 24 h
for the volatilization of cyclohexanone and the hardening of the mixture, deposited thick MR-PMMA film was obtained with a thickness of about 5 mm. Then a small groove made of a black plastic plate is fixed on the prism. Glycerol was added into the groove. The interface of the glycerol and MR-PMMA is almost parallel to the horizontal plane. As seen in Fig. 2(b), the illuminated area inside a circle of radius about 3 mm was divided into two parts by the interface, while the upper white area is the glycerol and the lower shadow area is the MR-PMMA. The proportions of glycerol in the illuminated area can be adjusted by moving the prism vertically. Here, the subscript ‘1’ and ‘2’ in Eq. (7) denote the glycerol and the MR-PMMA, respectively, \( n_r \) and \( \kappa \) of the MR-PMMA, and \( b_1 \) and \( b_2 \) can be resolved using the method depicted above.

### 3 Results and Discussion

Measurements for three proportions of glycerol in the illuminated area were taken, with \( b_1 \) equal to 38.83%, 14.39%, and 10.48%, respectively. Figure 3 shows the measured reflectance data, fitting curves, and the derivative of reflectance curves for the simulation samples. The calculated \( n_r \) of glycerol is about 1.4698 and has a shift of 0.0011 compared with the pure glycerol sample. \( n_r \) of MR-PMMA are 1.5205, 1.5217, and 1.5218, respectively, which have shifts of less than 0.002. \( \kappa \) of MR-PMMA are 0.00030, 0.00040, and 0.00032, respectively. The values of \( E_r^2 \) are larger than 0.9920. The results have proved the reliability of the new model described by Eq. (7). In Fig. 4, it’s distinct that the amplitude of the first peak increases with the proportion of glycerol \( b_1 \), while the positions of two derivative maxima are not sensitive to \( b_1 \). The result implies that the proportion of glycerol has no impact on the measured RI of glycerol and MR-PMMA.

![Fig. 3](image-url)  
(a) Measured reflectance data and fitting curves of the simulation sample with three different proportions of glycerol (TE wave). (b) The derivative of the reflectance curves.

![Fig. 4](image-url)  
Measured reflectance curve of porcine tissue and the derivative of the reflectance curve (TM wave).

We compared the values of \( n_r \) and \( \kappa \) of MR-PMMA determined using the new model, the dual-parameter fitting method,12 and EDTRM.13 Results are listed in Table 1. Clearly we can see that using EDTRM, only the right \( n_r \) can be obtained and \( k \) is much smaller compared with the real values. The dual-parameter fitting method achieves a better fitting than EDTRM while both \( n_r \) and \( \kappa \) have a large shift from the real value, for example, the shift of \( n_r \) is about 0.05 when \( b_1 \) equals to 38.83%. \( b_1 \) has an obvious impact on the misleading results and a smaller \( b_1 \) will lead to a much smaller error. Results have indicated that when the sample has two components, a new model is required to achieve accurate RI of each component. Glycerol in the liquid state has close contact with the MR-PMMA. There is no air gap between the two materials, so the effect of diffraction is subtle and was not observed in the experiment. Though the interface in the illumination spot has variable proportion, it is almost an ideal line and parallel to the horizontal plane, which occupies a rather small part and the effect of the interface can be neglected.

Measured reflectance and the derivative of the reflectance curves for porcine chicken breast and ovine muscle tissues are shown in Figs. 4 and 5. In Fig. 4, \( b_1 \) equals 31.29%. We found that double peaks appear on the derivative curves. From the first peak position of the derivative curve, the calculated \( n_r \) is 1.3565, which is similar to the measured value of pure tissue fluid \( (n_r = 1.3552) \). The result has proved that the first smaller ‘hump’ on the reflectance curve should originate from the tissue fluid. From the second peak, the calculated \( n_r \) of 1.3861 is similar to the reported values of porcine tissue.9,12,16 Significant information is revealed that the contacting area of the sample consists of the tissue fluid and muscle tissue.

In Fig. 5, the proportion parameters of tissue fluid \( b_1 \) equals 20.79% for chicken breast and 12.17% for ovine tissue. The \( n_r \) of chicken breast tissue is about 1.3907, which is almost equal to the result of 1.399 measured using low-coherence interferometry.17 For ovine tissue, \( n_r = 1.3958 \), which is similar to the reported results of 1.402 and 1.389 (Refs. 12 and 16, respectively).

The standard deviation of \( n_r \) is smaller than 0.001 for tissue samples. Fitting reflectance curves of ovine tissue obtained using EDTRM, dual-parameter fitting, and the new model are shown in Fig. 6. Comparisons of the three methods are listed in Table 2. The new model reveals a more superior fitting than the other two methods. Take ovine muscle tissue, for example. Similar to the analysis of the simulation sample, both the dual-parameter fitting method and EDTRM have
caused errors to $n_r$ and $k$. $E_2^s$ is 0.9905 for dual-parameter fitting method and 0.9680 for EDTRM, which was usually thought to get a satisfactory fitting. The new model obtains the best fitting with $E_2^s$ larger than 0.9960. The subtle hump on the measured reflectance curve was enlarged in the inset of Fig. 6.

Actually, the similar small 'hump' was also recorded by Fig. 2 of Ref. 10 and Fig. 7 of Ref. 12 in the RI measurement of porcine kidney and epidermis, but it was not discussed. As seen in Fig. 2, the incident light at the surface of the sample has a beam diameter of about 3 mm. There is a random distribution of tissue fluid and muscle tissue at the prism-tissue interface. Either the fluid or the muscle tissue part can be simplified as homogenous and shows an average RI value. The first peak on the derivative curves of Figs. 4 and 5(a) originates from the reflectance of the tissue fluid, while the real $n_r$ of the muscle tissue should be calculated from the second peak. The measured reflectance curve is the summation of the reflectance from the two kinds of contacting areas. It was commonly believed that the main differences among published results should be ascribed to sample-to-sample variance and sample preparation conditions, so the existence of tissue fluid didn’t receive much attention. A strong positive relationship was shown between the value of $b_1$ and the difference using the three methods. For porcine and chicken breast tissues, the values of $E_2^s$ vary a lot using the three methods because a larger amount of tissue fluid exists. For ovine tissue, the difference is much smaller with $b_1$ equal to 12.17%.

The knowledge of the optical properties of biological tissue is of fundamental importance for RI measurement. Tissue fluid usually consists of extracellular fluid ($n_r \approx 1.335$) and intracellular fluid ($n_r \approx 1.354$). In our experiment, most of the capillaries of the tissue samples run predominantly parallel with the muscle fibers. The main component of the tissue fluid should be the intracellular fluid, because the incisions were made perpendicular to the long axis of muscle fibers. From the optical point of view at the cells, structures with different RIs in the surroundings and in the interior of the cells contribute to the average RI of tissue. The aqueous solution of salts and proteins consisted in the cells lead to a mean RI of approximately 1.38. In membrane structures, there are about 5% of lipids having a higher RI of about 1.48. The measured $n_r$ of tissue fluid or muscle tissue should be the average RI in the illumination spot. According to the electromagnetic theory, when TIR occurs, the energy of the incident light decays rapidly and some light penetrates into the less dense medium over relatively short distances. The penetration depth is usually on the order of wavelength or smaller. If large amounts of tissue fluid or water exists and forms a thin layer between the prism and the muscle tissue, the RI of muscle tissue cannot be

<table>
<thead>
<tr>
<th>$b_1$</th>
<th>$n_r$</th>
<th>$k$</th>
<th>$E_2^s$</th>
<th>$n_r$</th>
<th>$k$</th>
<th>$E_2^s$</th>
<th>$n_r$</th>
<th>$k$</th>
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<tbody>
<tr>
<td>38.83%</td>
<td>1.5205</td>
<td>0.00030</td>
<td>0.9929</td>
<td>1.4785</td>
<td>0.00015</td>
<td>0.9839</td>
<td>1.5205</td>
<td>0.00015</td>
<td>0.2889</td>
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<tr>
<td>14.39%</td>
<td>1.5217</td>
<td>0.00040</td>
<td>0.9960</td>
<td>1.5210</td>
<td>0.00057</td>
<td>0.9346</td>
<td>1.5217</td>
<td>0.00029</td>
<td>0.9269</td>
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<tr>
<td>10.48%</td>
<td>1.5218</td>
<td>0.00032</td>
<td>0.9983</td>
<td>1.5214</td>
<td>0.00042</td>
<td>0.9694</td>
<td>1.5218</td>
<td>0.00024</td>
<td>0.9644</td>
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</tbody>
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![Table 1](Downloaded From: https://www.spiedigitallibrary.org/journals/Journal-of-Biomedical-Optics on 18 Apr 2020 Terms of Use: https://www.spiedigitallibrary.org/terms-of-use)
measured because the total reflection will only occur at the fluid-prism surface. The RI value depends much on the conditions of sample preparation and storage; fresh or frozen tissue samples are needed. For frozen samples, the water brought by surface condensation should be removed by surface cleaning.

Pressure is often added on the surface of the sample for the measurement. In the former research, damage to the samples and the significant change of \( n_r \) values were observed when the pressure was higher than 0.4 Mpa.\(^{12}\) so high pressure is forbidden. Similar to the tissue-machine interface concerns brought up by Chaiken et al. in their in vivo apparatus setup,\(^{21}\) pressure registration on the surface of these in vitro tissues is of essential importance in this study. They provided an appropriate apparatus for applying and maintaining pressure on the tissue surface and discussed the effects of pressure in detail. The applied pressure needs to be maintained in a reasonable range that should avoid a discernible change of the intrinsic properties of the tissue, while also guaranteeing no air gap exists at the sample-prism interface.

Cancer progression obviously alters the tissue organization, as exhibited by consistently higher RI variance in tumors versus normal regions.\(^{22}\) For other types of tissue, the composition of protein, lipid, and polysaccharide may lead to RI change. Studies have shown that membrane RI values can be estimated from composition studies.\(^{23}\) Further studies of RI are needed for more types of tissues carried with pathological indication and composition information, which may enable more accurate diagnosis and earlier disease detection.

4 Conclusion

In conclusion, we proposed a new model based on EDTRM for accurately extracting the RI of animal tissue samples. In the simulation sample study, the theoretical results calculated by the new model show good agreement with the measured reflectance data. This work also aims to emphasize the unavoidable influence of tissue fluid on the RI measurement of animal tissue. At the prism-tissue interface, part of the contacting area is filled with tissue fluid and part is muscle tissue. Misleading results should avoid a discernible change of the intrinsic properties of the sample-prism interface.

**References**


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**Table 2** RIs of porcine, chicken breast, and ovine tissue (TM wave).

<table>
<thead>
<tr>
<th>Sample</th>
<th>( n_r )</th>
<th>( k )</th>
<th>( E_r^2 )</th>
<th>( n_r )</th>
<th>( k )</th>
<th>( E_r^2 )</th>
<th>( n_r )</th>
<th>( k )</th>
<th>( E_r^2 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Porcine</td>
<td>1.3861</td>
<td>0.0022</td>
<td>0.9961</td>
<td>1.3770</td>
<td>0.0041</td>
<td>0.9522</td>
<td>1.3861</td>
<td>0.0014</td>
<td>0.6808</td>
</tr>
<tr>
<td>Chicken</td>
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<td>0.0022</td>
<td>0.9960</td>
<td>1.3840</td>
<td>0.0035</td>
<td>0.9829</td>
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<td>0.9421</td>
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<tr>
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<td>0.0045</td>
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