Experimental recovery of intrinsic fluorescence and fluorophore concentration in the presence of hemoglobin: spectral effect of scattering and absorption on fluorescence

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Abstract. The ability to recover the intrinsic fluorescence of biological fluorophores is crucial to accurately identify the fluorophores and quantify their concentrations in the media. Although some studies have successfully retrieved the fluorescence spectral shape of known fluorophores, the techniques usually came with heavy computation costs and did not apply for strongly absorptive media, and the intrinsic fluorescence intensity and fluorophore concentration were not recovered. In this communication, an experimental approach was presented to recover intrinsic fluorescence and concentration of fluorescein in the presence of hemoglobin (Hb). The results indicated that the method was efficient in recovering the intrinsic fluorescence peak and fluorophore concentration with an error of 3% and 10%, respectively. The results also suggested that chromophores with irregular absorption spectra (e.g., Hb) have more profound effects on fluorescence spectral shape than chromophores with monotonic absorption and scattering spectra (e.g., black India ink and polystyrene microspheres).

Keywords: intrinsic fluorescence signal; hemoglobin; optical properties; diffuse reflectance; fluorescence quantum yield.

1 Introduction

Many biological fluorophores in human mucosal tissues, such as collagen, nicotinamide adenine dinucleotide (NADH), and flavin adenine dinucleotide (FAD), can absorb light at shorter wavelengths (e.g., in the ultraviolet region) and emit fluorescence at longer wavelengths (i.e., in the visible region). Their fluorescence properties (e.g., intensity and lifetime) and relative concentration can be used to obtain the status of the studied tissues. For example, the fluorescence of NADH and FAD may increase as cells become dysplastic due to the disruption of the extracellular matrix, whereas collagen density or concentration increases during tumor progression. However, during in vivo measurements, background absorbers and scatterers strongly distort the intrinsic fluorescence and make it difficult to obtain the correct concentration of the fluorophore. The term “intrinsic fluorescence signal” (IFS) was adapted by different research groups to describe the fluorescence without the interference of other absorbers and scatterers. Details of the physical definition of IFS can be found in Sec. 2.3 of the manuscript. In soft tissues, typical absorbers are hemoglobin (Hb, primary absorber), collagen crosslinks, NADH, and FAD (secondary absorbers), whereas scatterers include cell nuclei, organelles, and collagen fibers. The fluorophore concentration can be extracted only if the effect of absorption and scattering is compensated and the IFS is retrieved.

Many studies have attempted to retrieve the IFS using theoretical modeling, experimental approaches, or a combination of both. For example, Palmer and Ramanujam developed a Monte-Carlo method incorporated with Mie theory and a nonlinear optimization algorithm to recover the IFS of furan dye within 10% error. Kanick et al. extended MC algorithms to investigate the effect of absorption on the measured fluorescence intensity, but the information regarding intrinsic fluorescence and fluorophore concentration was not recovered. MC algorithms were also used to calculate the optical fiber’s calibration factor, which was later used to recover the IFS from the measured diffuse reflectance (DR). Although the MC-based method is flexible for different illumination-collection geometries, it requires intensive computation during forward modeling even if modern computational power is applied. Therefore, it is necessary to develop a simpler approach that can perform fast recovery of fluorescence and be adapted to different systems. In studies by Diamond et al., the fluorophore concentration was extracted by applying diffusion theory for the measured fluorescence and DR. However, optical properties extraction based on the diffusion approximation may not be accurate for tumors with high angiogenesis (such as glioblastoma) or for intraoperative surgery where bleeding is unavoidable. In such case, absorption level usually dominates scattering level, and diffuse approximation becomes inappplicable.

Finlay and Foster used a forward adjoint model of fluorescence to recover the shape of intrinsic fluorescence spectra and Hb absorption with the prior knowledge of concentration of known absorbers and known fluorophores. The approach, however, was not able to retrieve the absolute fluorescence intensity...
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and fluorophore concentration. In studies by Kim et al., an analytical method was developed to correct the fluorescence line shape and fluorophore concentration based on the assumption that fluorescence is in a linear relationship with DR at emission wavelengths. However, such an assumption is valid only if an excitation wavelength within 380 to 450 nm is used so that the migration path of emitted photons is approximately the same as that of reflected photons. Furthermore, previous phantom studies considered furan 2 as the fluorophores and red marking dye as the background absorber. Such materials are not relevant to most tissue investigations, and the fluorescence intensity and fluorophore concentration were not recovered. For example, furan 2 has an emission peak at 400 to 420 nm, whereas many endogenous fluorophores such as NADH, FAD, and elastin have emission peaks at longer wavelengths (450 to 550 nm). Hoy et al. attempted to recover the intrinsic fluorescence line shape of fluorescein based on the recovered optical properties with the single-fiber fluorescence (SFF) technique. However, the fluorescence intensity and fluorophore concentration were not recovered for comparison. Moreover, the validation of SFF was performed on phantoms with high concentrations of intralipid while using 365 nm as the excitation wavelength. A recent report has shown that intralipid fluoroses strongly at this concentration and has a longer fluorescence lifetime (4.5 ns) compared to fluorescein (3.8 to 4 ns). Therefore, its fluorescence properties should not be ignored. Although different studies were able to recover the intrinsic fluorescence and concentration of protoporphyrin IX in human skin using excitation light at longer wavelengths from 600 to 800 nm, many fluorophores in human mucosa and brain such as NADH, FAD, and collagen absorb light at shorter wavelengths from 350 to 500 nm. Therefore, additional evaluations on phantoms or tissues with Hb as the dominant absorber are necessary if these approaches are to be applied to image mucosal tissues or brain tissues.

In this paper, we explored the ability of a simpler approach for fast recovery of fluorescence peaks and fluorophore concentration in highly absorptive media using an excitation wavelength at 355 nm. The approach was validated on tissue-simulating phantoms using fluorescein as fluorophore, polystyrene microspheres as background scatterers, and black India ink and ferrous-stabilized Hb as background absorbers.

2 Methods

2.1 Tissue-Simulating Phantoms

Stock solution of fluorescein with a concentration of $10^{-3}$ M was prepared by dissolving fluorescein powder (46955-100G-F, Sigma-Aldrich, Missouri) in concentrated ethanol 95% (Commercial Alcohols, GreenField Specialty Alcohol Inc., Ontario, Canada). Fluorescein concentrations of $10^{-4}$ and $10^{-3}$ M were prepared by simply diluting the stock solution in deionized (DI) water. The absorption and emission spectra of fluorescein are extremely sensitive to alcohol residue, and careful sample preparation is necessary to obtain accurate measurements. To simulate tissue scattering, polystyrene microspheres with diameter of 1 μm (07310-15, Polysciences Inc., Pennsylvania) were used. These spheres were preferred because their scattering properties are similar to biological tissues, and their well-controlled size, index of refraction, and accurate estimation of scattering properties are calculated using Mie theory. To investigate the effect of scattering on fluorescence, six phantoms (S1 to S6) with six different concentrations of microspheres (from 0.05% to 0.72% w/v) were created. These concentrations were obtained by diluting the original concentration of 2.65% w/v in DI water.

To observe the effect of Hb absorption on fluorescence, three phantoms with Hb concentrations of 3.5, 10, and 20 mg/ml (Hb3.5, Hb10, and Hb20) and microsphere concentration of 0.4% w/v were produced. To investigate the effects of secondary absorbers on fluorescence, five phantoms (I1 to I5) with various India ink concentrations (0.05% to 0.6%) and microsphere concentration of 0.72% w/v were created. In all phantoms, optical properties were controlled and calculated by applying Beer-Lambert’s law to the absorbance of pure solute absorbers (fluorescein, India ink, or Hb) measured with a spectrophotometer (Ultraspec 3000, Pharmacia Biotech Inc., New Jersey) for absorption coefficient ($\mu_a$) and Mie theory for reduced scattering coefficient ($\mu_s$). Scattering anisotropy ($g$) of polystyrene microspheres can be found in a previous study.

The volume and depth of each phantom were 6 ml and 5.5 cm, respectively. Each phantom was contained in a test tube with diameter of about 12 mm.

2.2 Instrumentation

DR signal from the phantoms was generated using a broadband light source (Dolan-Jenner MI-150, Edmund Optics, New Jersey) for illumination, whereas steady state fluorescence (SSF) signal was generated using a solid-state laser (PNV-001525-140, Teem Photonics, Meylan, France) at 355 nm with 300-ps full width at half maximum for excitation. Measurements of both DR and SSF signals were performed with the same customized optical probe. Figure 1 shows the geometry of the optical probe, including a DR/SSF source fiber; different DR/SSF detection fibers bundled into three groups at three source–detector distances (SDD) of 0.23, 0.59, and 1.67 mm; and a center fiber for time-resolved fluorescence (TRF) measurement. Three spectrometers (UV-NIR-200, StellarNet Incorporation, Tampa, Florida) were used to record the reflectance signal and SSF signal and were controlled by a moderately equipped computer (IBM Core 2 Duo L7500, 2 GB RAM). The position of the fiber probe was unchanged during both measurements. This enabled the correction of fluorescence using the DR measured at the same location.

Later, the fluorescence lifetime of fluorescein in each phantom was recorded using center optical fiber with a core diameter of 400 μm and numerical aperture of 0.12 (Fig. 1) and a calibrated acousto-optic tunable filter-based time-resolved
Details of the time-resolved system can be found elsewhere.\textsuperscript{43,44} In all measurements, the fiber-optic probe was held perpendicular to the phantom surface and slightly touched the phantoms. The time-resolved measurements merely served as a secondary verification of the stability and consistency in fluorescence properties of fluorescein in all phantoms (the primary verification was spectrometer measurement of absorbance spectra) and had no role in retrieving fluorescein concentration.

In the current study, experimental measurements with India ink and microspheres were performed on different days with different batches and concentrations of fluorescein. Therefore, consistency in our time-resolved measurements would also ensure that the use of additional absorbers and scatterers did not alter the chemical structure of fluorescein and that the same alcohol concentration was present in all the phantoms.

### 2.3 Retrieving of Intrinsic Fluorescence

When the excitation light with intensity $I_x$ was used to illuminate the sample, fluorescence was emitted with a spectral distribution $f_{xm}(\lambda_m)$. However, due to absorption and scattering in the tissue sample, only a fraction of $f_{xm}$, defined as $F_{xm}(\lambda_m)$, was collected. The subscripts $x$ and $m$ indicate the dependence of the quantity on excitation and fluorescence emission wavelengths ($\lambda_x$ and $\lambda_m$), respectively. Hence, $F_{xm}$ and $f_{xm}$ represent the measured fluorescence and intrinsic fluorescence at emission wavelength $m$ due to excitation wavelength $x$, respectively. Muller et al. and Zhang et al. defined $f_{xm}$ as the total fluorescence intensity of a thin slab of thickness $l$ (cm) of a material that does not absorb or scatter photons while containing the same concentration of fluorophores.\textsuperscript{12,16,31} In a closed form, $f_{xm}$ can be written in terms of Eq. (1), where $\mu_{a,x}$ is the absorption coefficient (cm\textsuperscript{-1}) due to the slab’s fluorophore at excitation wavelength $x$, and $\phi_{xm}$ (dimensionless) is the fluorescence quantum yield.\textsuperscript{12,16,31}

\[
f_{xm} = \frac{\lambda_x}{\lambda_m} I_x \mu_{a,x} \phi_{xm}. \tag{1}\]

In Eq. (1), ratio $\lambda_x/\lambda_m$ corrects for the difference in photon energy at excitation and emission wavelength, whereas the product $\mu_{a,x} \phi_{xm}$ represents the probability of a photon at excitation wavelength $\lambda_x$ to be absorbed by the fluorophore, and $\phi_{xm}$ represents the probability of a photon at emission wavelength $\lambda_m$ to be generated after the absorption event at $\lambda_x$. $\mu_{a,x}$ can be defined as $c \varepsilon \ln(10)$, where $c$ is fluorophore molar concentration (M) and $\varepsilon$ extinction coefficient (cm\textsuperscript{-1} M\textsuperscript{-1}) at $\lambda_x$.

Because $f_{xm}$ directly relates to $c$, Eq. (1) can be rewritten in the form of Eq. (2) with a consideration of a mixture of $i$ fluorophores:

\[
f_{xm} = \frac{\lambda_x}{\lambda_m} I_x l \ln(10) \sum_i c_i \phi_{xm}^i. \tag{2}\]

By using the escape probability distribution function ($\rho$), the phase-function dependence of the scattering was separated from the scattering and absorption coefficients, and the diffuse reflectance ($R$) and the measured fluorescence ($F_{xm}$) can be modeled using Eqs. (3) and (4).\textsuperscript{12,31}

\[
R = \sum_{n=1}^{\infty} \rho_n w_n, \tag{3}\]

\[
F_{xm} = \sum_{n=1}^{\infty} \sum_{i=0}^{n-1} \rho_n w_{ni}, \tag{4}\]

where $w_n = a^n = [\mu_x/(\mu_a + \mu_s)]^n$, $w_{ni} = a_i^{n-i}(f_{xm}/\mu_a)w_{n-i-1}$, and $\rho_n = R_0[e^{-\mu_s l} - 1]e^{-\mu_a l}$. In Eqs. (3) and (4), $n$ is the number of scattering events (dimensionless), $S$ is a constant calibration factor for each individual fiber (dimensionless), $a$ is the photon weight (dimensionless), $\mu_a$ is the absorption coefficient (cm\textsuperscript{-1}), $\mu_s$ is the scattering coefficient (cm\textsuperscript{-1}), $g$ is the anisotropy parameter (dimensionless), and $R_0$ is the diffuse reflectance from a standard sample containing only scatterers (dimensionless). By combining the expressions of $R$ and $F_{xm}$ into Eq. (1), a relationship between $f_{xm}$ and $F_{xm}$ can be written as Eq. (5).

\[
f_{xm} = \frac{\mu_a s l F_{xm}}{\left[R_0 R_{bg} \left[e^{\mu_s l} - 1\right] \left[e^{\mu_a l} - 1\right]\right]^{1/2} R_x R_0 \frac{R_{xm}}{R_0} + \left[e^{\mu_a l} - 1\right]} \tag{5}\]

In Eq. (5), $R_x$ is the diffuse reflectance from the targeted samples. In the studied phantoms, $\mu_a$ and $g$ were obtained by applying Mie theory for specific microsphere diameter and concentration.\textsuperscript{27} To calculate the diffuse reflectance $R$, the measured reflectance intensity of the sample $I_{r,\text{sample}}$ was normalized to the reflectance intensity of a standard spectroplan with 99.9% reflectivity $I_{r,\text{std}}$ (LabSphere, Inc., New Hampshire) after subtracting the background signal intensity $I_{r,\text{bg}}$. This method is described via Eq. (6).

\[
R = \frac{I_{r,\text{sample}}}{I_{r,\text{std}} - I_{r,\text{bg}}} \tag{6}\]

The retrieved signal $f_{xm}$ in Eq. (5) can be used to recover the concentration of fluorophore for a known value of $\phi_{xm}$. In the current study, fluorescence quantum yield of fluorescein in basic

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**Fig. 1** Schematics of the fiber probe geometry. Diffuse reflectance/ steady-state fluorescence (DR/SSF) detection fibers are bundled together into three groups, each at the indicated distance (0.23, 0.89, and 1.67 mm) from the DRS/SSF source fiber (measured from the center of each fiber). In addition, a central fiber was used for time-resolved fluorescence (TRF) spectroscopy measurements. Diameter of DR/SSF fibers is 200 µm and diameter of the TRF fiber is 400 µm.
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ethanol was assumed to be 0.97 at emission peak. In experimental measurement, due to the strong intensity of the laser, a neutral density filter with optical density of 2 and a short exposure time (~1 ms) was applied when measuring \( I_x \) to avoid saturation at spectrometers. Therefore, to enable accurate estimation of \( c \) from Eq. (2), a correction factor \( k \) was applied so that \( k = 10^{-2}(1/1130) \), where 1/1130 is the ratio of exposure time used for \( I_x \) and for \( F_{xm} \) (or \( f_{xm} \)). The concentration \( c \) of fluorescein in the phantom can be experimentally estimated in Eq. (7):

\[
c = \frac{k \cdot f_{xm} \lambda_m}{I_x \lambda_m \varepsilon \phi_{xm} \ln(10)}.
\]  

To obtain the calibration factors \( l \) and \( S \) in Eq. (5), the least squares fitting routine \( \text{fminsearch()} \) in MATLAB® was used to fit the measurement of \( f_{xm} \) (from the reference nonscattering phantom), \( F_{xm} \), and \( R_{xm} \) of calibration phantoms into Eq. (5). This optimization method is based on the Nelder–Mead simplex algorithm and has been widely used for spectral analysis in spectral imaging. In the fitting routine, the ideal intrinsic fluorescence \( f_{xm} \) was measured directly on a phantom consisting solely of fluorescein \( 10^{-4} \) M (in DI water), whereas \( F_{xm} \) and \( R_{xm} \) were measured with phantoms consisting of fluorescein \( 10^{-4} \) M and various India ink and microsphere concentrations. To simplify the fitting routine, \( l \) was set at 1 cm. Fitting routines for known spectra of \( f_{xm} \), \( F_{xm} \), and \( R_{xm} \) yielded values of 54.6, 45.5, and 48.2 for fibers with an SDD of 0.23, 0.59, and 1.67 mm, respectively. These values were later used to retrieve \( f_{xm} \) in Hb phantoms.

Similar to previous methods, the current method utilized the ideas that enabled the retrieving of intrinsic fluorescence from the measured DR. The main difference lies in the calibration approaches. The current method incorporated system characteristics such as light source intensity and position of the fiber probe into the calibration. Therefore, the current method enabled recovery of absolute fluorescence intensity via Eq. (5) and of fluorophore concentration via Eq. (7), whereas the previous methods could recover only the relative fluorescence intensity and spectral shape.

3 Results

3.1 Effect of Hemoglobin Absorption on Fluorescence

Figure 2 shows \( \mu_\text{a} \) of Hb and fluorescein, as well as \( \mu'_\text{a} \) of polystyrene microspheres used in the Hb-based phantoms (Hb3.5, Hb10, and Hb20). In these phantoms, the concentration of fluorescein and microspheres remained the same, whereas Hb concentration was varied. The inset of Fig. 2(b) shows that the measured \( \mu_\text{a} \) was in excellent agreement with reference \( \mu_\text{a} \) values for fluorescein \( 10^{-4} \) M in alcohol. The reference \( \mu_\text{a} \) was calculated by multiplying fluorescein concentration to that of its tabulated molar extinction coefficients. As indicated elsewhere, an Hb concentration of 3.5 mg/ml best simulates background absorption in mucosal tissue. In addition, a microsphere concentration of 0.4% w/v (≈0.0073 spheres per cubic micrometer) was used to simulate background scattering.

Figure 3(a) shows the measured SSF \( (F_{xm}) \) from three phantoms using SDD of 0.59 mm. Due to the similarity in the measured fluorescence spectra at different fibers, only the signal at one fiber is shown [Fig. 3(a)]. In general, increasing absorption (from 3.5 to 20 mg/ml) decreases the measured fluorescence intensity due to the decrease in the number of emitted photons escaping to the tissue surface. To compare the spectral shapes, the fluorescence spectrum of fluorescein in DI water (intrinsic) and in Hb and microspheres (distorted) is shown in the same graph [Fig. 3(b)]. As shown in Fig. 3(b), the spectral shape of the measured fluorescence was highly distorted in the wavelength regions where Hb strongly absorbs photons (540 nm and 580 nm). Figure 3(c) shows examples of the absorption dependence of the measured fluorescence at the fluorescein emission peak of 520 nm.

Despite the distortion in the measured SSF, it was observed that average lifetime in the phantoms remains unchanged, indicating that lifetime was not affected by background absorption (Fig. 4). A biexponential deconvolution method was used to obtain the lifetime information of the measured fluorescence signals. Figure 4(a) shows that fluorescence lifetime is consistent at the emission wavelength for a phantom with Hb concentration of 3.5 mg/ml. In addition, Fig. 4(b) shows that the fluorescence lifetime of fluorescein in Hb phantoms agreed with that of the intrinsic signal within one standard deviation. In Fig. 4(b), the fluorescence lifetime was averaged over six repeated measurements, and standard deviations were calculated and shown as error bars.

Figure 5(a) shows the corresponding DR of three Hb-based phantoms using SDD of 0.59 mm. In general, the drops of reflectance at the 540 and 580 nm regions were due to Hb absorption in these regions [Fig. 2(a)], whereas the drop at 470 to 520 nm was mainly due to fluorescein absorption [Fig. 2(b)]. Figures 5(b) and 5(c) compare the measured fluorescence \( (F_{xm}) \) to that of recovered and intrinsic fluorescence for a phantom with Hb concentration of 3.5 mg/ml using SDD of 0.59 mm. The recovered fluorescence \( (f_{xm}) \) is the fluorescence signal calculated using Eq. (5). The least-square fitting routine \( \text{fminsearch()} \) was also applied to fit \( f_{xm} \) to the shape of the intrinsic spectrum (ideal) and obtain the fitted spectrum \( f_{xm2} \) of \( f_{xm1} \). The square errors between \( f_{xm1} \) and \( f_{xm2} \) were used to optimize the results of the fitting. Figure 5(d) compares the percentage difference among \( F_{xm} \), \( f_{xm1} \), and \( f_{xm2} \) with respect to the ideal intrinsic fluorescence for phantom Hb3.5 (Hb concentration of 3.5 mg/ml).

On average over 480 to 620 nm, the percentage error was ~81%, 24%, and 8% for \( F_{xm} \), \( f_{xm1} \), and \( f_{xm2} \), respectively.

![Figure 2](https://example.com/fig2.png)  
**Fig. 2** (a) Absorption coefficients \( \mu_\text{a} \) of hemoglobin (Hb) phantoms (Hb3.5: 3.5 mg/ml, Hb10: 10 mg/ml, and Hb20: 20 mg/ml) as a function of wavelength and (b) reduced scattering coefficients \( \mu'_\text{a} \) of polystyrene microspheres and \( \mu_\text{a} \) of fluorescein as a function of wavelength. In these phantoms, the concentration of microsphere and fluorescein was kept constant at 0.4% w/v and \( 10^{-4} \) M, respectively. The inset in (b) compares \( \mu_\text{a} \) of fluorescein \( 10^{-4} \) M measured in the current study (measured) to that extracted from the literature (reference).
These numbers were 91%, 26%, 9% and 99%, 30%, 13% for phantoms Hb10 and Hb20, respectively (Table 1). On average over 480 to 620 nm, the accuracy of the signal was improved by 70% without fitting and by 90% with fitting. Considering only peak emission at 522 nm, the percentage errors of $F_{xm}$, $f_{xm1}$, and $f_{xm2}$ are 79%, 3%, and 8%, respectively. The recovered fluorescence at 522 nm was used to calculate the concentration of fluorescein using Eq. (7). With $\phi_{355,522}$ assumed to be 0.97, the value of $I_{355}$ and $I_{355,522}$ are 61225 counts and 45093 counts, respectively. The extinction coefficient $\varepsilon_{355}$ of fluorescein was assumed to be $3.2 \times 10^4$ M$^{-1}$ cm$^{-1}$. Therefore, the $c$ value of $1.07 \times 10^{-4}$ M was estimated using Eq. (7). Table 2 summarizes the extracted concentration of fluorescein in three Hb phantoms. On average, the extracted concentration was within 10% of the controlled value of $10^{-4}$ M.

### 3.2 Effect of India Ink Absorption on Fluorescence

To further investigate the absorption effect on fluorescence, black India ink with increasing concentration from phantoms H1 to I5 was used to simulate background absorption and a microsphere concentration of 0.72% was used to simulate background scattering. Figure 6 summarizes the optical properties of the phantoms used in this section. The goal of this subsection is to investigate the effects of a monotonic decreasing absorption on fluorescence intensity and spectral shape, and to compare it to the Hb cases.

Figure 7(a) summarizes the measured fluorescence ($F_{xm}$) from phantoms H1 to I5, whereas Fig. 7(b) compares the spectral shape of $F_{xm}$ and $f_{xm}$, and Fig. 7(c) summarizes the corresponding $R$. These data were collected at SDD = 0.59 mm. A similar trend to that of Fig. 3(a) was observed in Fig. 7(a):

### Table 1 Average percentage difference (AVG) of $F_{xm}$, $f_{xm1}$, $f_{xm2}$ with respect to the ideal intrinsic fluorescence over 490 to 620 nm. Analysis for all three phantoms (Hb3.5, Hb10, and Hb20) is shown.

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Hb3.5</th>
<th>Hb10</th>
<th>Hb20</th>
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<tr>
<td>$F_{xm}$</td>
<td>80.8 ± 2.7</td>
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<td>98.7 ± 0.4</td>
</tr>
<tr>
<td>$f_{xm1}$</td>
<td>24.1 ± 12.4</td>
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SSF decreases as absorption increases. However, there is a significant difference between Figs. 3(b) and 7(b): the spectral shape of the fluorescence for phantoms with ink as background absorber was not distorted and remained similar to that of the intrinsic signal (measured with only fluorescein in DI water). This can be explained by referring to either the India ink absorption spectra [Fig. 6(a)] or the phantom DR spectra [Fig. 7(c)]. Similar to the Hb phantom cases, increasing absorption (from I1 to I5) decreases the reflectance signal collected [Fig. 7(c)]. However, in contrast to the Hb phantoms, there are no peaks in the India ink absorption spectra [Fig. 6(a)] or DR spectra [Fig. 7(c)]. Note that the drop of DR at 500 nm in Fig. 7(c) was due to the strong absorption of fluorescein at this region. Again, Eq. (7) can be applied to extract fluorescein concentration. An average error of 5% was obtained for the recovered fluorescein concentration (Table 3). Furthermore, the fluorescence lifetime of India ink phantoms remained the same as that of the intrinsic signal, as expected (Fig. 8). Table 4 provides a brief summary of the average fluorescence lifetime of fluorescein in Hb and India ink phantoms over the emission region of 500 to 600 nm. 

### Table 2

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Phantom</th>
<th>Hb3.5</th>
<th>Hb10</th>
<th>Hb20</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f_{555,522}$ (counts)</td>
<td>45,093 ± 786</td>
<td>49,958 ± 232</td>
<td>44,174 ± 317</td>
<td></td>
</tr>
<tr>
<td>$F_{555,522}$ (counts)</td>
<td>9472 ± 165</td>
<td>4527 ± 21</td>
<td>557 ± 4</td>
<td></td>
</tr>
<tr>
<td>$c$ (M)</td>
<td>1.07E−04</td>
<td>1.19E−04</td>
<td>1.05E−04</td>
<td></td>
</tr>
</tbody>
</table>

### Fig. 6

(a) Absorption coefficients $\mu_a$ of the India ink in phantoms I1 to I5 as a function of wavelength and (b) reduced scattering coefficients $\mu_s'$ of polystyrene microsphere and $\mu_a$ of fluorescein as a function of wavelength. In these phantoms, the concentration of India ink increased from phantom I1 to I5, and the concentration of microsphere and the fluorescein was kept constant at 0.72% w/v and $10^{-4}$ M, respectively.

### Fig. 7

(a) Measured fluorescence emission spectra of the phantoms (I1 to I5), (b) normalized fluorescence emission spectra, and (c) the corresponding DR spectra. These data were collected with the fiber at SDD = 0.59 mm. In all phantoms, fluorescein concentration was $10^{-4}$ M.

### Table 3

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Phantom</th>
<th>I1</th>
<th>I2</th>
<th>I3</th>
<th>I4</th>
<th>I5</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f_{555,522}$ (counts)</td>
<td>43,652 ± 741</td>
<td>46,230 ± 420</td>
<td>46,589 ± 744</td>
<td>42,442 ± 837</td>
<td>41,342 ± 823</td>
<td></td>
</tr>
<tr>
<td>$F_{555,522}$ (counts)</td>
<td>10,479 ± 149</td>
<td>8778 ± 58</td>
<td>8282 ± 112</td>
<td>7281 ± 115</td>
<td>5918 ± 93</td>
<td></td>
</tr>
<tr>
<td>$c$ (M)</td>
<td>1.04E−04</td>
<td>1.10E−04</td>
<td>1.11E−04</td>
<td>1.01E−04</td>
<td>9.84E−05</td>
<td></td>
</tr>
</tbody>
</table>

SSF decreases as absorption increases. However, there is a significant difference between Figs. 3(b) and 7(b): the spectral shape of the fluorescence for phantoms with ink as background absorber was not distorted and remained similar to that of the intrinsic signal (measured with only fluorescein in DI water). This can be explained by referring to either the India ink absorption spectra [Fig. 6(a)] or the phantom DR spectra [Fig. 7(c)]. Similar to the Hb phantom cases, increasing absorption (from I1 to I5) decreases the reflectance signal collected [Fig. 7(c)]. However, in contrast to the Hb phantoms, there are no peaks in the India ink absorption spectra [Fig. 6(a)] or DR spectra [Fig. 7(c)]. Note that the drop of DR at 500 nm in Fig. 7(c) was due to the strong absorption of fluorescein at this region.

### Table 4

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Phantom</th>
<th>I3</th>
<th>I5</th>
</tr>
</thead>
<tbody>
<tr>
<td>$f_{555,522}$ (counts)</td>
<td>43,652 ± 741</td>
<td>41,342 ± 823</td>
<td></td>
</tr>
<tr>
<td>$F_{555,522}$ (counts)</td>
<td>10,479 ± 149</td>
<td>5918 ± 93</td>
<td></td>
</tr>
<tr>
<td>$c$ (M)</td>
<td>1.04E−04</td>
<td>9.84E−05</td>
<td></td>
</tr>
</tbody>
</table>

SSF decreases as absorption increases. However, there is a significant difference between Figs. 3(b) and 7(b): the spectral shape of the fluorescence for phantoms with ink as background absorber was not distorted and remained similar to that of the intrinsic signal (measured with only fluorescein in DI water). This can be explained by referring to either the India ink absorption spectra [Fig. 6(a)] or the phantom DR spectra [Fig. 7(c)]. Similar to the Hb phantom cases, increasing absorption (from I1 to I5) decreases the reflectance signal collected [Fig. 7(c)]. However, in contrast to the Hb phantoms, there are no peaks in the India ink absorption spectra [Fig. 6(a)] or DR spectra [Fig. 7(c)]. Note that the drop of DR at 500 nm in Fig. 7(c) was due to the strong absorption of fluorescein at this region. Again, Eq. (7) can be applied to extract fluorescein concentration. An average error of 5% was obtained for the recovered fluorescein concentration (Table 3). Furthermore, the fluorescence lifetime of India ink phantoms remained the same as that of the intrinsic signal, as expected (Fig. 8). Table 4 provides a brief summary of the average fluorescence lifetime of fluorescein in Hb and India ink phantoms over the emission region of 500 to 600 nm.

### Table 2

The recovered fluorescein concentration ($c$) in three hemoglobin (Hb) phantoms from Eq. (5). The controlled concentration of fluorescein in these phantoms was $10^{-4}$ M.
Table 4. Overall average lifetime of fluorescein in different phantoms (in region 480 to 550 nm). Concentration of fluorescein in these phantoms was $10^{-4}$ M. Concentration of microspheres was 0.4% w/v and 0.72% w/v in Hb and India ink phantoms, respectively.

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Phantom</th>
<th>Intrinsic</th>
<th>Hb3.5</th>
<th>Hb10</th>
<th>Hb20</th>
<th>(I3)</th>
<th>(I4)</th>
<th>(I5)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\tau$ (ns)</td>
<td></td>
<td>3.92 ± 0.12</td>
<td>3.96 ± 0.16</td>
<td>3.97 ± 0.31</td>
<td>3.95 ± 0.32</td>
<td>3.78 ± 0.26</td>
<td>3.84 ± 0.25</td>
<td>3.74 ± 0.26</td>
</tr>
</tbody>
</table>

480 to 550 nm. Overall, the fluorescence lifetime remained constant and agreed with previously reported values for fluorescein in diluted alcohol.\(^1\)

3.3 Effect of Microsphere Scattering on Fluorescence

Figure 9 summarizes the optical properties of phantoms S1 to S6. In these phantoms, microsphere concentration increases from S1 (0.05% w/v) to S6 (0.72% w/v) [Fig. 9(a)], whereas the concentration of fluorescein is kept constant at $10^{-5}$ M. No other absorbers were added. Figure 9(b) shows the $\mu_a$ spectrum of fluorescein $10^{-5}$ M solution. The goal of this subsection is to inspect the effects of a monotonically decreasing reduced scattering on fluorescence intensity and spectral shape.

The measured SSF of the phantoms is shown in Fig. 10 for all collection distances: 0.23 mm [Fig. 10(a)], 0.59 mm [Fig. 10(b)], and 1.69 mm [Fig. 10(c)]. In general, adding microspheres decreased the fluorescence intensity at first due to the effect of scattering (intrinsic versus S1). The fluorescence intensity eventually increased if more microspheres were added from S1 to S6. Figure 11(a) further illustrates this trend by plotting the normalized intensity at the emission peak of 520 nm. This phenomenon was consistent with what was reported previously.\(^12\) To compare the intensity trend between SDDs, the fluorescence collected at each SDD was normalized to the intrinsic fluorescence at the same SDD [Fig. 11(a)]. The current results indicated that increasing SDD from 0.23 to 0.59 mm might increase the fluorescence signal up to 40% in highly scattering media, although further increasing of SDD showed the reverse [Fig. 11(a)].

The corresponding DR of phantoms for SDD = 0.59 mm is also shown in Fig. 11(b), and the normalized measured

Fig. 9 (a) Reduced scattering coefficients $\mu_s'$ and (b) absorption coefficients $\mu_a$ of phantoms S1 to S6. In these phantoms, the concentration of microspheres increased from phantoms S1 to S6, whereas the concentration of fluorescein was kept at $10^{-5}$ M. No other absorbers were added.

Fig. 10 Measured fluorescence emission spectra of the phantoms using (a) SDD = 0.23 mm, (b) SDD = 0.59 mm, and (c) SDD = 1.67 mm. Microsphere concentration increased from sample S1 to sample S6. Fluorescein concentration was kept constant at $10^{-5}$ M.

Fig. 11 (a) Normalized fluorescence intensity as a function of $\mu_s'$ at emission peak of 520 nm for all three SDDs, (b) corresponding total DR spectra at SDD = 0.59 mm, and (c) normalized fluorescence intensity. Fluorescein concentration was kept constant at $10^{-5}$ M.
Du Le et al.: Experimental recovery of intrinsic fluorescence and fluorophore concentration...

**Table 5** The extracted fluorescein concentration (c) in microsphere phantoms from Eq. (5). The controlled concentration of fluorescein in these phantoms was 10⁻⁵ M.

<table>
<thead>
<tr>
<th>Phantom</th>
<th>Quantity</th>
</tr>
</thead>
<tbody>
<tr>
<td>S1</td>
<td>f₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>F₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>c (M)</td>
</tr>
<tr>
<td>S2</td>
<td>f₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>F₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>c (M)</td>
</tr>
<tr>
<td>S3</td>
<td>f₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>F₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>c (M)</td>
</tr>
<tr>
<td>S4</td>
<td>f₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>F₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>c (M)</td>
</tr>
<tr>
<td>S5</td>
<td>f₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>F₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>c (M)</td>
</tr>
<tr>
<td>S6</td>
<td>f₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>F₃₅₅.₅₂₂ (counts)</td>
</tr>
<tr>
<td></td>
<td>c (M)</td>
</tr>
</tbody>
</table>

**Table 6** Overall average lifetime in region 480 to 550 nm of fluorescein for phantoms S1 to S6.

<table>
<thead>
<tr>
<th>Phantom</th>
<th>Quantity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intrinsic</td>
<td>τ (ns)</td>
</tr>
<tr>
<td>S1</td>
<td>τ (ns)</td>
</tr>
<tr>
<td>S2</td>
<td>τ (ns)</td>
</tr>
<tr>
<td>S3</td>
<td>τ (ns)</td>
</tr>
<tr>
<td>S4</td>
<td>τ (ns)</td>
</tr>
<tr>
<td>S5</td>
<td>τ (ns)</td>
</tr>
<tr>
<td>S6</td>
<td>τ (ns)</td>
</tr>
</tbody>
</table>

**Discussion and Conclusions**

The current study has shown that Hb absorption strongly distorted the fluorescence spectra of fluorescein at emission wavelength regions near 540 and 580 nm. Most endogenous fluorophores in human tissues emit in this wavelength region upon irradiation with ultraviolet light. Using the proposed method and the constructed phantoms with optical property ranges reported for mucosal tissues and brain tissues (μᵩ of 1.2 to 20 cm⁻¹ and μᵦ of 1.7 to 24.5 cm⁻¹ at 540 nm), fluorescein concentration was recovered with an average error of 10% (Fig. 5, Table 1), considering only the emission peak at 522 nm. On average over 450 to 650 nm, the intrinsic fluorescence intensity of fluorescein was recovered with an error of 27% (versus 90% with raw signal). Although spectral fitting reduced error in recovering fluorescence by 66% on average over 450 to 650 nm, the percentage error of fitted data was higher than that of nonfitted data at the emission peak 522 nm (3% versus 8%). Although absorption affects fluorescence and DR differently due to the difference in light path shown in Eqs. (3) and (4), this difference was accounted for in Eq. (5). In addition, the absorption distortion on the f₃₅₅ line shape was accounted for by the ratio of Rₘ₉/Rₘ₉ in Eq. (1). The proposed method was also efficient in retrieving fluorescein’s concentration in India ink and microsphere phantoms with an average percentage error of 5% and 8%, respectively (Tables 3 and 4). The current approach used the same concept as previous studies to the extent to which the measured DR was used to compensate the effect of Hb absorption on fluorescence signal. What made our approach unique were the abilities to recover absolute fluorescence intensity and to estimate fluorophore concentration via the experimental calibration of individual fibers without the expense of complicated computation. Our ultimate goal is to recover fluorophore concentration using DR and fluorescence measurements and optical properties of the targeted volume. In this manuscript, we demonstrated that the proposed method is feasible to recover fluorophore concentration if...
optical properties are known. In the next step, an inverse solution is being developed to recover optical properties and to demonstrate that this approach is able to perform real-time tissue measurement. This addition will make the current approach more practical in studying tissue samples. Although a single fluorophore was used in our study, this should not limit the application of the proposed method in media with multiple fluorophores. As demonstrated in the current study, the recovered intensity at the emission peak is crucial to extract fluorophore concentration. In biological tissues, each fluorophore (NADH, FAD, and collagen) has a known emission peak, which can be recovered using Eq. (1), allowing extraction of its concentration via Eq. (7). Although Müller and Hendriks were unable to recover fluorophore concentration, their studies demonstrated the ability of the proposed method to recover multiple fluorescence peaks via Eq. (1).

The current results also show that scattering and absorption materials whose attenuation coefficients decay exponentially with wavelengths (such as black India ink and polystyrene microspheres) have a minor effect on the spectral shape of the fluorescence [Figs. 7(b) and 11(c)]. These observations were made when studying the broadband emission signal of fluorescein in 500 to 625 nm. This finding might indicate that absorption and scattering from NADH, FAD, and collagen fibers do not have significant effects on the fluorescence spectral shape because their attenuation coefficients decay exponentially with wavelength, similar to those of India ink or microspheres. Therefore, Hb is the only absorber of concern. In addition, a consistency in the average fluorescence lifetime measured with the time-resolved system verified that the chemical structure of fluorescein was not affected by the introduction of India ink, microspheres, or Hb. Furthermore, the current results suggested that increasing SSD from 0.23 to 0.59 mm has the potential to increase the fluorescence signal in highly scattering media, especially for S4 to S6 [Fig. 11(a)]. Therefore, a small increase in collection distance could increase the probability of detection. However, a larger increase of SDD would decrease the probability of an emitted photon reaching the detection fiber. As a result, fluorescence intensity was high at SSD of 0.59 mm and low at SSD of 1.67 mm. Additional theoretical analysis is necessary to confirm this result and to optimize the design to maximize the measured fluorescence signal.

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