Light management through guided-mode resonances in thin-film silicon solar cells

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Abstract. We theoretically explain and experimentally demonstrate light trapping in thin-film solar cells through guided-mode resonance (GMR) effects. Resonant field enhancement and propagation path elongation lead to enhanced solar absorption. We fabricate nanopatterned solar cells containing embedded 300-nm period, one-dimensional gratings. The grating pattern is fabricated on a glass substrate using laser interference lithography followed by a transparent conducting oxide coating as a top contact. A ∼320-nm thick p-i-n hydrogenated amorphous silicon solar cell is deposited over the patterned substrate followed by bottom contact deposition. We measure optical and electrical properties of the resonant solar cells. Compared to a planar reference solar cell, around 35% integrated absorption enhancement is observed over the 450 to 750-nm wavelength range. This light-management method results in enhanced short-circuit current density of 14.8 mA/cm², which is a ∼40% improvement over planar solar cells. Our experimental demonstration proves the potential of simple and well-designed GMR features in thin-film solar cells. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction in whole or in part requires full attribution of the original publication, including its DOI. [DOI: 10.1117/1.JNP.8.083995]

Keywords: guided-mode resonance; interferometric lithography; light trapping; thin-film solar cells.

1 Introduction

Thin-film solar cell technology offers benefits of low-cost material usage and processing relative to currently dominant crystalline silicon solar cells. In contrast to classic thick, wafer-based silicon cells, the higher absorption coefficients of materials used in thin-film photovoltaics allow for a film thickness of hundreds of nanometers to micrometers. The quality of material can be relatively poor since the charge carriers only travel a distance on the order of the film thickness. However, the low-energy photons suffer from short optical paths that ultimately cause low spectral uptake in the cells near the material’s bandedge.1–3 Consequently, efficient light-trapping mechanisms are necessary to obtain comparable performance from thin-film solar cells.

By incorporating properly designed photonic nanostructures, incoming sunlight can be trapped inside the absorbing layer while reducing loss caused by reflection and scattering. With a highly concentrated field, a thin absorbing layer sufficiently absorbs most of the solar spectrum. This allows further reduction of the absorbing layer thickness and ensures minimal usage of materials and better collection efficiency for low-quality materials. Numerous studies have been conducted to improve light-capture and collection efficiency of thin absorbing layers. The application of diffractive optics,4–6 random texturing,7,8 antireflective layers,9,10 plasmonics,11–13 photonic crystals,14–16 guided-mode excitation,16,17,18 and three-dimensional structures like nanowire, nanodome, and nanocone solar cells19–21 shows distinguished improvements in solar absorption. Though each mechanism contributes to the manipulation of optical path lengths inside the films, the most efficient light-harvesting scheme is yet to be convincingly identified. Using numerical simulation tools, it is possible to design
microdomain or nanodomain photonic structures showing enhanced absorption and photocurrents. However, from a practical point of view, application of such features into solar cells has to be technologically and economically feasible.

Here, we report guided-mode resonance (GMR) effects in waveguide-grating structures for enhanced optical absorption. We experimentally demonstrate the application of simple designs of one-dimensional (1-D) nanograting patterns into thin-film hydrogenated amorphous silicon (a-Si:H) solar cells. With these particular operative effects, the periodic spatial pattern couples the input sunlight into a collection of waveguide modes associated with thin wave-guiding films that resonate in the cell and concentrate the light in the active layer. Thereby, the photon interaction path is elongated within the silicon film, which helps particularly to harvest the low-energy photons. We describe the fabrication processes and present experimental results that comply with our theoretical analysis.

2 GMR Effect in Lossy Layers

A subwavelength periodic pattern and a waveguide layer over a substrate constitute a generic GMR element, as shown in Fig. 1(a), with characteristic parameters, period \( \Lambda \), grating depth \( d_g \), waveguide layer thickness \( d_{wg} \), fill factor \( F \), incident beam \( I \), reflected beam \( R \), and transmitted beam \( T \). At resonance, an incident light beam couples to leaky waveguide modes through the grating structure. An efficient energy exchange occurs between the reflected and transmitted waves, resulting in sharp peaks in the diffraction efficiency spectrum of the resonant waveguide grating.22–24

The grating couples the incident wave into the resonant waveguide-grating structure. A resonance occurs when one of the diffracted waves generated by the grating element phase matches to a leaky waveguide mode admitted by the waveguide structure, as schematically depicted in Fig. 1(b). At the phase-matching condition, the effective mode propagation constant \( \beta_i \), corresponding to the \( i \)’th order evanescent diffracted wave, is given by

\[
\beta_i = k_0 (n_c \sin \theta_{in} - i \lambda / \Lambda),
\]

where \( k_0 = 2\pi / \lambda \), \( \lambda \) is the free space wavelength, \( n_c \) is the refractive index of cover medium, \( \theta_{in} \) is the incident angle, and \( \Lambda \) is the period of the grating. The refractive index of the waveguide (\( n_{wg} \)) should be such that \( n_{wg} > n_c, n_s, n_g \), where \( n_s \) is the refractive index of substrate and \( n_g \) is the average refractive index of the grating layer.

Depending on the device parameters, operating wavelength, and incident angle, there can be a single resonance or multiple resonances. Using powerful electromagnetic design methods, the spectral bands of these resonant leaky-mode elements can be engineered for various photonic

![Figure 1](https://www.spiedigitallibrary.org/journals/Journal-of-Nanophotonics/Download/2014/083995-2)
device applications. For example, it has already been shown that a single periodic layer with 1-D periodicity enables narrow line filters, polarizers, reflectors, and polarization-independent elements.\textsuperscript{26–28} An example of spectral response of a single-resonance device is shown in Fig. 2. For the computations, we use a computer code based on rigorous coupled-wave analysis (RCWA),\textsuperscript{29} which is a proficient algorithm to evaluate diffraction efficiency of periodic structures as further discussed in Ref. 30. In our numerical simulations, we use 11 harmonics and we verify good convergence by test simulations using 21 harmonics. For a simple waveguide-grating structure\textsuperscript{28} with $\Lambda = 280$ nm, $d_g = 55$ nm, $d_{wg} = 110$ nm, $F = 0.5$, $n_{wg} = n_H = 2.02$, $n_c = n_L = 1$, and $n_s = 1.5$, a complete energy exchange occurs between transmitted and reflected waves and a sharp resonance reflectance peak occurs at the 487-nm wavelength when illuminated with normally incident transverse electric (TE) polarized normally incident light. The dashed line represents the reflectance of a corresponding homogeneous layer with the grating replaced by a simple layer with an effective refractive index.

![Fig. 2 GMR spectral response of a waveguide-grating structure with $\Lambda = 280$ nm, $d_g = 55$ nm, $d_{wg} = 110$ nm, $F = 0.5$, $n_{wg} = n_H = 2.02$, $n_c = n_L = 1$, and $n_s = 1.5$. The GMR occurs at the 487-nm wavelength with transverse electric (TE) polarized normally incident light. The dashed line represents the reflectance of a corresponding homogeneous layer with the grating replaced by a simple layer with an effective refractive index.](image1)

![Fig. 3 GMR spectral response of a waveguide-grating structure with $\Lambda = 280$ nm, $d_g = 55$ nm, $d_{wg} = 110$ nm, $F = 0.5$, $n_c = n_L = 1$, and $n_s = 1.5$. The solid line represents the GMR effect for lossless material where $n_{wg} = n_H = 2.02$, and the dashed line represents the reduced reflectance for lossy material where $n_{wg} = n_H = 2.02 + i0.05$. The total internal electric field distributions for both lossless and lossy materials at the resonance wavelength of 487 nm are shown as insets.](image2)
However, the GMR effect is strongly sensitive to material loss. The presence of material loss (complex refractive index $N = n + \text{i} \kappa$, where $\kappa$ is the extinction coefficient) diminishes the external signatures of the resonance. If $\kappa = 0.05$ is considered in the previous example ($n_{wg} = n_H = 2.02 + \text{i}0.05$), the reflectance decreases significantly, as depicted in Fig. 3. The total internal electric field distributions of these elements for both lossless and lossy materials are shown as insets in Fig. 3. We observe that even though the reflectance decreases, the field distribution with loss maintains key features with lower field levels. This shows that the field-enhancement aspect of the GMR effect can be beneficial without the traditional external signatures being present. If we compare the absorbance with a planar reference, an enhancement ratio of around 2.3 is obtained at the resonance wavelength, as shown in Fig. 4.

3 GMR-Enabled Light Management

In this study, our interest lies in showing absorption enhancement in thin-film solar cells by applying the GMR effect. The grating layer, which is a phase-matching element, forces the incoming light into multiple resonances in the device, eventually increasing the probability of light absorption. A simple planar structure fails to offer such light confinement. Thus for efficient solar absorption, the GMR structure should support multiple resonances over the broadband solar spectrum. Designing the grating-pattern period to be smaller than the wavelengths in the solar spectrum ($\Lambda < \lambda$) allows the GMR structure to operate as multiple resonant devices. To demonstrate the multiresonant GMR spectral response, we consider a structure consisting of an a-Si:H grating and a waveguide layer over a glass substrate with $\Lambda = 350$ nm, $d_g = 50$ nm, $d_{wg} = 250$ nm, and $F = 0.5$. Hydrogenated a-Si has a complex dispersive refractive index, $N(\lambda) = n(\lambda) + \text{i} \kappa(\lambda)$, capable of absorbing light up to the 750-nm wavelength corresponding to bandgap energy of 1.7 eV. The numerical value of $N(\lambda)$ provided by Fontcuberta i Morral and Roca i Cabarrocas is given in Fig. 5.

Figure 6 shows the spectral responses of a multiresonant GMR structure with three different $\kappa$ values. Plot 1 indicates lossless a-Si:H with $\kappa = 0$, plot 2 indicates a constant $\kappa = 0.05$, and plot 3 indicates the original dispersive $\kappa(\lambda)$ over the spectrum, while $n(\lambda)$ remains the same (as in Fig. 5) for all three plots. The observed resonance peaks originate from input light coupling to leaky-modes across the spectrum. We observe the reduction of reflection and subsequent enhancement of absorption with the increase of the $\kappa$ value over the spectrum of 450- to 750-nm wavelengths.

The total electric field patterns for the three different $\kappa$ values ($\kappa = 0$, $\kappa = 0.05$, and $\kappa = 0.082$) at the 651-nm resonance wavelength are shown in Fig. 7. The original value of $\kappa$ at 651 nm is 0.082.
The field pattern gradually decays with the increase of the $\kappa$ value. Based on the simulation results, we intend to implement the photonic resonant structure into a real p-i-n thin-film a-Si:H solar cell to observe enhanced absorption through intensified field patterns and subsequent increased electrical efficiency. However, fabrication of resonant patterns into the active region of a planar solar cell requires sacrifice of materials and junction interruption, which will cause electrical performance degradation. Instead, we consider a superstrate cell configuration to incorporate the

![Fig. 5 Dispersive refractive index of a-Si:H as derived from Ref. 31.](image)

![Fig. 6 GMR spectral response for a waveguide-grating structure with $\Lambda = 350$ nm, $d_g = 50$ nm, $d_{wg} = 250$ nm, $F = 0.5$, $n_c = n_e = 1$, and $n_s = 1.5$. Plot 1 represents the GMR effect for lossless material where $\kappa = 0$, plot 2 represents the reduced reflectance for lossy material where $\kappa = 0.05$, and plot 3 represents reflectance for lossy a-Si:H with the original dispersive $\kappa(\lambda)$.](image)

![Fig. 7 Total electric field distribution inside an a-Si:H waveguide-grating structure for three different values of $\kappa$ (0, 0.05, and 0.082) at $\lambda = 651$ nm. The original $\kappa$ value of a-Si:H at 651 nm is 0.082.](image)

The field pattern gradually decays with the increase of the $\kappa$ value. Based on the simulation results, we intend to implement the photonic resonant structure into a real p-i-n thin-film a-Si:H solar cell to observe enhanced absorption through intensified field patterns and subsequent increased electrical efficiency. However, fabrication of resonant patterns into the active region of a planar solar cell requires sacrifice of materials and junction interruption, which will cause electrical performance degradation. Instead, we consider a superstrate cell configuration to incorporate the
patterns into the active region as schematically shown in Fig. 8. We fabricate a nanopattern on a glass substrate, and the pattern is gradually transferred to the silicon region without interrupting the junctions. We consider a thin indium-tin-oxide (ITO) layer in between the glass and silicon as a top contact. To observe the GMR-induced absorbance enhancement exclusively, we conduct the optical characterization before the bottom contact is made.

4 Fabrication

We fabricate the 1-D nanograting patterns on a glass substrate; Fig. 9 summarizes the fabrication steps. First, a 1 × 1 in.² glass substrate is cleaned with acetone, isopropanol, and deionized water and dried with blown nitrogen. Then an 80-nm bottom antireflection coating (BARC: DUV30J-6) is spin-coated over the glass substrate at 1200 rpm and baked for 60 s on a heating plate.

Fig. 8 Schematic view of a GMR solar cell without bottom contact.

Fig. 9 Schematic view of nanopatterned solar cell fabrication steps.
adjusted to 205°C. A 350-nm thick photoresist coating (PR: SEPR-701) is spin-coated at 1100 rpm and baked for 90 s at 110°C. A 1-D grating pattern with a 300-nm period is transferred into the PR by UV laser interferometric lithography using a laser with $\lambda = 266$ nm. The purpose of using the BARC layer beneath the PR is to reduce the reflection from the glass substrate and ensure uniform pattern exposure over the PR. After developing the PR, the BARC is removed from the open area of the pattern by reactive ion etching (RIE) using oxygen plasma. The glass substrates are etched using an argon (Ar) and trifluromethane (CHF$_3$) gas mixture. The remaining PR and BARC are removed by RIE using oxygen plasma. In a systematic experimental process, gratings with 50-, 60-, and 70-nm depths are fabricated on glass substrates. Here, we present the results obtained from solar cells with 60-nm grating depths since the results are similar to those obtained with 50- and 70-nm grating depths.

The patterned glass substrates are coated with a 140-nm thick film of ITO by sputtering. From the scanning electron microscope (SEM) images, we confirm that ITO film deposition over the 60-nm deep grating area conforms to the grating structures and serves well as the top contact. The ITO-coated glass substrates are annealed in a rapid thermal annealer in a vacuum chamber at 490°C for 15 min. The resistivity of the film is 50 $\Omega$/$\text{sq}$. The average transmittance of the annealed ITO thin film is around 90% over the 450- to 750-nm wavelength range. Figure 10 shows the measured transmittance of the annealed ITO film. Using a multichambered plasma-enhanced chemical vapor deposition system, a complete p-i-n single-junction solar cell with an approximate thickness of 10-nm p-type, 290-nm i-type, and 20-nm n-type a-Si:H is deposited over the ITO pattern. Finally, consecutive sputter deposition of 130-nm thick ITO and 300-nm thick aluminum films constitutes the bottom contact. Thin-film solar cells on planar...
glass substrates are also deposited with identical film thicknesses for performance comparison. Recently, we have shown that using thermal nanoimprint lithography, the nanopatterns can be fabricated by single step on plexiglas substrate which offers cost-efficient large area fabrication of nanostructured thin-film solar cells.32

The surface image of the ITO-coated oxide grating with a grating depth of 60 nm, taken with an atomic force microscope, is shown in Fig. 11. The grating specifications are \( \Lambda = 304 \text{ nm} \), \( d_g = 60 \text{ nm} \), and \( F = 0.5 \). Figure 12 includes images from an SEM; Figs. 12(a) and 12(b) show cross-sectional images of the ITO-coated glass pattern and Fig. 12(c) shows the top view. The cross-sectional images of the complete patterned solar cell, including top and bottom contacts, are presented in Figs. 12(d) and 12(e). Figure 12(f) displays a photograph of the patterned solar cell.

5 Results and Discussions

5.1 Optical Absorbance

Regarding the superstrate structure of the solar cell, Fig. 8 illustrates that light is shone from the glass side of the structure at normal incidence. We obtain optical absorbance measurements before the bottom contacts are made in order to ascertain GMR-induced absorption enhancement exclusively. The reflected and transmitted light associated with the patterned a-Si:H solar cells are measured with a fiber optic spectrometer. The light source used is a tungsten halogen lamp with a wavelength range of 360 to 2400 nm. We conduct the same measurements on a corresponding planar solar cell to establish a comparison. Since the grating pattern has a 300-nm period and the refractive index of glass is 1.5, the Rayleigh wavelength of the patterned structure is \( \lambda_R = n\Lambda = 450 \text{ nm} \), i.e., only the zero-order diffraction prevails beyond the 450-nm wavelength. The primary reason for selecting a 300-nm period is to operate the solar cells in a zero-order diffraction regime for a substantial portion of the solar spectrum. Since no higher diffraction orders exist beyond the 450-nm wavelength, it suffices as a good approximation to measure the reflectance and transmittance for normally incident light without using an integrating sphere. We measure zero-order reflectance \( (R_0) \) and transmittance \( (T_0) \) spectra normalized to the source spectrum and the absorbance is obtained as \( A = 1 - (R_0 + T_0) \) for \( \lambda > 450 \text{ nm} \). The measurement setup is schematically shown in Fig. 13.

Figure 14 shows the comparison of unpolarized absorbance between the patterned and planar solar cells. Integrated absorbance enhancement of \( \sim 35\% \) is obtained in patterned solar cells with 60-nm deep grating depths over the wavelength range of 450 to 750 nm.
Figure 15 shows the unpolarized reflectance comparison between planar and patterned cells. The reflectance is significantly suppressed in patterned solar cells. Designing the period to be smaller than the operating wavelength permits the antireflection effect to contribute to the enhanced optical absorbance. Due to this interdependency, it is difficult to differentiate the impact from the GMR effect. However, the absorption coefficient of a-Si:H weakens beyond 550 nm. The propagation distance of the captured light along the weakly absorbing film, i.e.,...
the decay length of the resonant leaky mode, must be much longer than the film thickness to achieve successful absorption in the long wavelength region. Thus, the GMR effect can ensure such optical path elongation through multiple resonances. Figure 16 shows the TE and transverse magnetic (TM) components of the total absorbance of the patterned solar cell, where the electric field vectors in TE and TM polarizations are orthogonal and parallel to the plane of incidence, respectively. As described in the previous section, the spectral signature diminishes with a higher extinction coefficient. Therefore, the individual GMR peaks are not visible over the entire wavelength range. In the long wavelength region, where the absorption coefficient is low, distinguishable GMR resonances are visible at 716 nm for TM polarization and at 675 and 723 nm for TE polarization.

The absorbance of the patterned solar cell is theoretically calculated using the RCWA computational method. The simulated and experimental absorbance comparisons for a 60-nm deep patterned solar cell are shown in Fig. 17. There are two possible reasons for the discrepancy. First, the dispersion data of a-Si:H used for simulation is not measured from the fabricated device, rather taken from literature. Second, the fabricated pattern does not completely follow the sharp binary pattern as schematically shown in Fig. 8. According to simulation, the integrated absorbance enhancement factor is $\sim 32\%$ for patterned solar cell compared to a homogeneous reference, over the 450- to 750-nm wavelength range.
5.2 Electrical Characteristics

Solar cell efficiency measurement is carried out under AM1.5G illumination. The current density ($J$) versus voltage ($V$) plots for the patterned and planar solar cells are given in Fig. 18. Open-circuit voltage ($V_{oc}$), short-circuit current density ($J_{sc}$), fill factor (FF), and conversion efficiency ($\eta$) for the patterned and planar solar cells obtained from $J$–$V$ plots are summarized in Table 1.

Short-circuit current density improves by $\sim40\%$ from 10.5 to 14.8 mA/cm$^2$ for patterned solar cells with $d_g = 60$ nm, compared to the planar cell. Each cell has an effective area of approximately 0.1 cm$^2$. Open-circuit voltage is 0.82 V for both types of solar cells. The power conversion efficiencies of the planar and patterned solar cells are measured as 2.6% and 4.1%, respectively, with $\sim57\%$ enhancement. The fabricated solar cells exhibit rather low FFs, which is the main reason for the low conversion efficiencies obtained. FFs for the planar and patterned cells are 3 and 3.3, respectively. By enhancing the contact resistivity, a-Si:H material, and p-i-n interface quality, the FF and subsequently the efficiency of these solar cells can be improved. The higher optical absorbance obtained through GMR resonances in patterned solar cells compared to the planar reference cell are reflected in the enhanced electrical performance. The experimental results motivate the application of nanograting patterns in thin-film photovoltaics.

6 Conclusion

We explain light trapping in thin-film solar cells through GMRs with numerical examples and experimentally implement nanograting patterns into a-Si:H solar cells with 300-nm periods and 60-nm grating depths. Theoretically simulated GMR-enabled enhanced optical absorption is experimentally observed in fabricated patterned solar cells, which leads to improved electrical performance. For the particular device design used, integrated absorbance enhancement of $\sim35\%$ over the 450- to 750-nm wavelength range and short-circuit current density enhancement of $\sim40\%$ are found in a 60-nm deep nanograting patterned solar cell compared to an equivalent

![Fig. 18 Current density/voltage plot of planar and patterned solar cells.](image-url)

<table>
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<th>Parameters</th>
<th>Planar cell</th>
<th>Patterned cell</th>
<th>Enhancement (%)</th>
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<tr>
<td>Open-circuit voltage, $V_{oc}$ (V)</td>
<td>0.82</td>
<td>0.82</td>
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<tr>
<td>Short-circuit current density, $J_{sc}$ (mA/cm$^2$)</td>
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<td>14.8</td>
<td>$\sim40$</td>
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<tr>
<td>Fill factor, FF (%)</td>
<td>3</td>
<td>3.3</td>
<td></td>
</tr>
<tr>
<td>Conversion efficiency, $\eta$ (%)</td>
<td>2.6</td>
<td>4.1</td>
<td>$\sim57$</td>
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planar reference cell. GMR phenomena strongly depend on dispersion properties and thickness of the absorbing photovoltaic materials. Enhanced optical absorbance leading to an increased conversion efficiency holds the same potential for micro-crystalline and organic thin-film solar cells with optimal structural and material device parameters.

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References
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