Graph theoretical approach to functional connectivity in prefrontal cortex via fNIRS

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1 Introduction

Functional near-infrared spectroscopy (fNIRS) has been proposed as an affordable, fast, and robust alternative to many neuroimaging modalities yet it still has long way to go to be adapted in the clinic. One request from the clinicians has been the delivery of a simple and straightforward metric (a so-called biomarker) from the vast amount of data a multichannel fNIRS system provides. We propose a simple-straightforward signal processing algorithm derived from fNIRS-HbO2 data collected during a modified version of the color-word matching Stroop task that consists of three different conditions. The algorithm starts with a wavelet-transform-based preprocessing, then uses partial correlation analysis to compute the functional connectivity matrices at each condition and then computes the global efficiency values. To this end, a continuous wave 16 channels fNIRS device (ARGES Cerebro, Hemosoft Inc., Turkey) was used to measure the changes in HbO2 concentrations from 12 healthy volunteers. We have considered 10% of strongest connections in each network. A strong Stroop interference effect was found between the incongruent against neutral condition (p = 0.01) while a similar significance was observed for the global efficiency values decreased from neutral to congruent to incongruent conditions \( F(2,33) = 3.46, \ p = 0.043 \). The findings bring us closer to delivering a biomarker derived from fNIRS data that can be reliably and easily adopted by the clinicians.

Keywords: weighted connectivity graph; global efficiency; Stroop task; wavelet-based partial correlation.

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connectivity studies using fMRI, similar studies using fNIRS have emerged recently. Recent studies have shown obviously that human brain connectome networks can be constructed using fMRI, diffusion tensor imaging, electroencephalography (EEG), and magnetoencephalography (MEG) data, and even further be investigated by graph theoretical approaches.

In this study, we aimed to investigate the efficiency of the graphs formed in the prefrontal cortex (PFC) during a modified version of the color-word matching Stroop task. Connectivity patterns obtained from the partial correlations (PC) of the hemodynamic responses acquired from 16 different regions of the PFC to various stimuli are expected to be different from channel to channel and this is related with the cognitive load. A continuous wave 16 channels near-infrared spectroscopy device (ARGES Cerebro, Hemosoft Inc., Turkey) was used to measure the changes in HbO₂ concentrations from 12 healthy volunteers.

An important aspect of our research is the exploration of the potential of fNIRS to be used as a functional neuroimaging modality in an expectation to deliver a clinical marker. The second important contribution of our research is the introduction of a simple and straightforward signal-processing algorithm: a wavelet-based partial correlation (WPC) analysis that allowed us to focus on the functional connectivity in a well-defined frequency interval (0.0035 to 0.08 Hz) while eliminating the use of high order digital filters and preprocessing techniques that end up warping the data dramatically. Use of wavelet transform-based elimination of nonneural sources of noise, such as cardio respiratory effects, has been quite successful in fNIRS signal-processing applications. Moreover, WPC analysis helps to remove the effect of indirect paths; since by applying this method while the WPC between two channels is correlated, an underlying correlation common to all other 14 regions can be regressed out.

Hence the main aim of this study is to explore the feasibility of fNIRS to monitor the neural correlates of the cognitive activity in PFC during a Stroop test by using wavelet analysis and graph theory. The choice of a wavelet-based filtering can in fact be more justified for real-time analysis since wavelets are excellent choices for real-time applications. Usually real-time neurofeedback systems require several seconds of data recording before proving feedback. Hence a collection of initial 10 to 20 s of data for real-time feedback would be ideal and then every new second the previous 20 s would be analyzed to provide the feedback. Correlation and GE calculations are very fast algorithms that can be computed in the millisecond range by any DSP chip.

2 Materials and Methods

2.1 Subjects and Protocol

Data were collected from 12 healthy volunteers (7 females and 5 males) from the university community (right-handed, mean age 26.17 ± 4.30, range 20 to 31) at the Neuro-Optical Imaging Laboratory, Bogazici University Istanbul, Turkey. Control subjects had no history of psychiatric or neurological disorders. Subjects were asked to perform color-word matching Stroop tasks whose trials are the Turkish versions of Zyss et al. Subjects were presented with two words, one written above the other. The top one was written in ink color whereas the bottom one was in white. Subjects were asked to judge whether the word written below correctly denotes the color of the upper word or not. If color and word match, then subjects were to press on the left mouse button with their forefinger, and if not, on the right mouse button with their middle finger.

Subjects were informed to perform the task as quickly and correctly as possible. The words stayed on the screen until the response was given with a maximum time of 3 s. The screen was blank between the trials. The experiment consisted of neutral (N), congruent (C), and incongruent (IC) trials. In the neutral condition (N), the upper word consisted of four X’s (XXXX) in ink color. In the congruent condition (C), ink colors of the upper word and the word itself were the same, whereas in the incongruent condition (IC), they were different. The trials were presented in a semiblocked manner (see Fig. 1 for the details). Each block consisted of six trials. The interstimulus interval within the block was 4.5 s and the blocks were placed 20 s apart in time. The trial type within a block was homogeneous (but the arrangements of false and correct trials were alternating). There were five blocks of each type. The experiments were performed in a silent, lightly dimmed room. Words were presented via an LCD screen that was 0.5 m away from the subjects. The task protocol was approved by the Ethics Review Board of Bogazici University.

2.2 Data Acquisition

The fNIRS device is capable of transmitting near-infrared light at two wavelengths (730 and 850 nm), which are known to be able to penetrate through the scalp and probe the cerebral cortex. Employing 4 LEDs and 10 detectors, the device can sample 16 different channels in the brain simultaneously (see Fig. 2 for the details of the probe). LEDs and detectors were placed in a flexible printed circuit board that was specially designed to fit the curvature of the forehead. The source–detector separation is fixed at 2.5 cm, which is optimized for penetration depth (~1.5 cm from the surface to allow sampling from the cortex) and a wider sampling area of the PFC. Sampling frequency of the device was 1.7 Hz. Calculation of concentration changes of oxy-Hb and deoxy-Hb in blood is based on a modified version of the Beer–Lambert law.

2.3 Signal Processing Algorithm

The signal processing algorithm proposed is summarized in Fig. 3. As can be seen, this is a consolidation of techniques proposed in the literature by many others. The wavelet transform has been proposed to remove artifacts and irrelevant physiological signals. The choice of the details and approximation coefficients was based on the spectral analysis of fNIRS signals.
2.3.1 Wavelet transform-based preprocessing

The discrete wavelet transform (DWT) uses filter banks to perform the wavelet analysis. The DWT decomposes the signal into wavelet coefficients that can represent the signal in various frequency bands. The choice of wavelet function plays an important role in the quality of the analysis of fNIRS signals. Similarity of the mother wavelet to the hemodynamic response function improves the detectability of the estimation accuracy of the signal. Hence, the decomposition was done by the Daubechies 5 (Db5) as the mother wavelet because of its high similarity to hemodynamic response. The wavelet domain is advantageous to focus in a defined frequency interval to emphasize the functional association between brain regions subtended by cognitive activity. Neuronal activity-related hemodynamic response observed in fNIRS-HBO2 data are shown to occupy the frequency range of (0.003 to 0.08 Hz). According to the wavelet decomposition tree, the frequency band of the hemodynamic response falls in the approximation at level 3 (CA3: 0.0035 to 0.110 Hz) with respect to the sampling frequency of the fNIRS instrument. The coefficients at very low and higher frequency values were nullled and then a new fNIRS-HBO2 signal was reconstructed for each detector.

2.3.2 Partial correlation

PC is a useful statistical tool for determining the relationship between two variables after removing the effects of other variables. The goal of PC analysis is to figure out the hidden relation between two channels, while the interactions of other channels on them have been eliminated. In our study, 16 channels were used to investigate the functional connectivity (D = 16). Suppose that \( x = (x_i)_{i=1,...,D} \) are the time signals related to each of the 16 channels of the fNIRS signal. The PC coefficient between the two channels \( i \) and \( j \) is defined by \( \Pi_{i,j} \), which is a calculation of the conditional correlation between channels \( i \) and \( j \) irrespective of the effect of D-2 remaining channels \( (R_{D-2}/\{i,j\}) \).

\[
\Pi_{i,j} = \text{corr}[x_i, x_j|x_{R_{D-2}/\{i,j\}}].
\]

(1)

It has been shown that the PC matrix can be obtained by calculating the covariance matrix (\( \Sigma \)) from D channels. Thus, for \( D = 16 \), the number of PC coefficients will be equal to \( D(D-1)/2 = 120 \), which is obtained from the PC matrix. Matrix \( \Pi \) can be easily calculated through the reverse of covariance matrix \( Y = [Y_{i,j}] = \Sigma^{-1} \). The reverse covariance matrix of \( X \) is called precision matrix or concentration matrix. Thus,

\[
\Pi_{i,j} = -\frac{Y_{i,j}}{\sqrt{Y_{ii}Y_{jj}}},
\]

(2)

where \( i \) and \( j \) are the two separate channels and \( \Pi_{i,i} = 1 \). The value range of PC is between +1 and −1. PC values were computed for each frequency band in three types of stimuli. Since PC analysis helps to remove the effect of indirect paths, by applying this method, the PC between two channels is correlated with the activity at all other 14 regions regressed out. By applying this method, we investigated connectivity graphs based on PCs between the inverse wavelet transformed (reconstructed) data that correspond to the specific frequency band of interest.

2.3.3 Weighted connectivity graph

Graph-based network analysis represents the state-of-the-art methodology in brain connectivity. We considered the channels as a set of vertices \( V \) and the PC coefficients assigned weights on the set of edges \( E \), leading to an undirected complete weighted graph \( G = (V; E) \). We investigated the connectivity graphs of the PCs computed between wavelet coefficients at the third level (corresponding to 0.0035 to 0.110 Hz frequency range) of each channel. The graphs were computed for each stimulus type.

2.3.4 Global efficiency and cost of a graph

Efficiency can be evaluated for a wide range of networks, including weighted graphs. The formal definition is as follows:

\[
GE = \frac{1}{N(N-1)} \sum_{i \neq j \in G} \frac{1}{L_{ij}},
\]

(3)
where \( N \) is the number of nodes in the network, \( L_{ij} \) is the shortest path length between nodes \( i \) and \( j \). Maximal possible global efficiency (GE) occurs when all edges are present in the network. We used Latora and Marchiori's efficiency measure, since it allows us to work with weighted connectivity graphs. In this case, the GE is computed as
\[
GE = \frac{1}{N(N-1)} \sum_{i \neq j} \frac{1}{d_{ij}},
\]
where \( d_{ij} \) is defined as the smallest sum of the physical distances throughout all the possible paths in the graph from \( i \) to \( j \). This has an interpretation, as stronger connection weights intuitively correspond to shorter lengths. Equation (4) generates values of GE in the range of [0; ∞]. This value can be normalized to [0; 1] by dividing it into randomly generated networks with the same number of nodes. This analysis provides an insight to the robustness of the network and its closeness to small network properties.

We generated 100 degree matched random networks to compute the ratios of global efficiency (GE/GE\text{random}) between the real brain functional networks and 100 degree matched random networks to assess small-worldliness of brain functional networks. Typically, GE of a small world network (GESW) approximates to the GE of a random network (GESW/GE\text{random} ~ 1).

We, then, investigated the topological properties of the brain functional network as a function of GE and \( K_{\text{cost}} \). The total number of edges in a graph divided by the maximum possible number edges \( N(N-1)/2 \)
\[
K_{\text{cost}} = \frac{1}{N(N-1)} \sum_{i \in G} K_i \tag{5}
\]
is called the cost of the network, which measures how expensive it is to build the network. The degree of each node, \( K_i \), \( i = 1, 2, \ldots, 16 \), is defined as the number of nodes in the subgraph \( G_i \). A subgraph \( G_i \) is defined as the graph including the nodes that are the direct neighbors of the \( i \)th node. \( K_{\text{cost}} \) is the average of the degrees of all the nodes in the graph, which is a measure for the sparsity of a network.

### 2.3.5 Behavioral results

To achieve the behavioral results, we analyzed the reaction times (RTs) from data of 12 subjects. In order to compare each pair of stimuli, we applied a two-tailed paired \( t \)-test for RTs. The interference effect for the RTs between IC and N conditions (\( p = 0.01 \)) and facilitation effect for the RTs of N against C conditions are significantly different (\( p = 0.03 \)). However, there is no significant difference between RT of IC and C (\( p = 0.8 \)).

### 3 Results

#### 3.1 Global Efficiency Results

We averaged across all 100 generated random networks to obtain a mean GE\text{random} for each degree \( K \) and threshold \( T \). Over a wide range of cost (0.005 < \( K < 0.04 \)), results are consistent with previous functional brain network studies.

Figure 4(a) shows GE values for N, C, and IC in a real network (average of 12 subjects) and random networks for each \( K \) cost. We investigated the small-world that corresponded to the degree of connectivity threshold 0.01 < \( T < 0.99 \) (with steps of 0.01). Analysis of variance (ANOVA) was used to test the statistical significance among GE values from different stimulus types (i.e., GE\text{N}, GE\text{C}, and GE\text{IC}). Figure 4(b) shows significance at six different threshold values. The purple triangles indicate that there are significant differences between the GE of three types of stimuli (\( p < 0.05 \)). We investigated the topological properties of the brain functional network as a function of GE and \( K \), following the studies by Stam et al and Liao et al.

The choice of a threshold value will have a major effect on the topological properties of the resulting networks. This allowed us to compare the topological properties among the three types of stimuli in a manner that is relatively independent of the network size. The threshold is selected to ensure that brain networks have a lower GE compared to random networks with relatively the same degree of connectivity distribution. Ten percent of the strongest connections in each network (highest values of wavelet PC) is considered, which corresponded to the degree of connectivity threshold [see Fig. 4(b)]. GE values were computed for each stimulus condition. Path length is inversely related to the GE of a network for the transfer of information among nodes by multiple parallel paths, and that GE is easier to estimate than path length when studying sparse networks.
GE decreased as the stimulus type became more difficult $[F(2,33) = 3.46, p = 0.043]$ as seen in Fig. 5 (GEN > GEC > GEIC). Although the two-way ANOVA provided a significance, this significance is clearly between the GEN and GEC but not between GEC and GEIC as expected. Normally, the Stroop findings focus on the interference effect (null hypothesis is that the mean value of GEIC is the same as the mean value of GEN).

3.2 GE versus Behavioral Results

We investigated the relationship between the RTs and GE values in the N, C, and IC matrices. We computed the change in RTs for different stimulus types and also the change in the GE of the N, C, and IC. Behavioral results and GE analysis according to the stimulus type are shown simultaneously in Fig. 5. The most sought after finding in a color-word matching Stroop task is the contrast of the incongruent condition against the neutral condition. We show that both in RTs and GE values there is a strong interference effect between the incongruent and neutral conditions.

All in all, we believe that the decreasing GE throughout a task might possess clinical significance.

4 Discussion

This study proposes a simple and straightforward algorithmic method to quantify the functional connectivity of the brain using graph theoretical techniques applied to fNIRS-HBO2 signals. We also propose to integrate the well-studied wavelet-based filtering and PC analyses as preprocessing tools before graph efficiency is computed. Graph theory gives us a language for networks. It allows us to define networks exactly and to quantify network properties at many different levels. This quantification is likely to improve further since new graph measures are described regularly.

Mesquita et al. performed an fNIRS study during resting state and then applied correlation analysis to determine the functional connectivity among brain regions. They used the correlation analysis between two optodes. This approach is prone to incorrect correlations since both data might contain similar trends due to interference from systemic fluctuations. Tachtsidis et al have shown how these fluctuations can alter the accuracy of detection and diagnosis if not taken care of. Lindauer et al. have proven that the underlying cerebrovascular dynamics are greatly affected by the metabolism, pharmacological interventions, and even diseases and hence hinder the accurate estimation of the neuronal response. In recent years, several investigators decided to tackle this problem either by proposing optical probe geometries or advanced signal processing techniques. While a remedy to this interference problem might be adding optodes with short separation, it comes at a cost of increased device complexity and expense. Signal processing tools have shown to reliably improve this desensitization to superficial fluctuations with a common physiological background. Tak and Ye have provided an excellent review on the capabilities of such alternatives. The nature of this interference is the basic underlying physiology and it can be assumed to be present with a varying degree of contamination in each and every time series of fNIRS data. One alternative to eliminate this contamination and achieve nuisance-free fNIRS data representing the neural activity is the use of PC analysis. The method we used in this study based on PC eliminates this deceiving correlation by considering the similar trends underlying other optode data and eliminating them. This approach also provides a means to bypass any unnecessary pre-processing of the data. Among many denoising algorithms, we decided to use the wavelet transform-based approach since the effectiveness of this technique has been shown in many cases where there might be spike-like or stepwise motion artifacts in the signal. Such artifacts will not be removed by any bandpass infinitive impulse response filtering technique and in fact lead to a more fatal distortion in the signal as the smearing of that spike onto the adjacent time points. Yet another advantage of wavelet-based denoising is its use of very short duration filters causing minimal phase distortion possibly minimizing an error in calculation of the correlation coefficient. ICA can be considered as an alternative yet the assumption in ICA-based approaches is that the sources are already independent of each other. The noise might be independent but the systemic physiological background signal is not. Hence, it is nearly impossible to find ICA sources that are band limited yet uncorrelated with the noise. So the natural choice was a wavelet-based approach.

Graph theoretical metrics have been applied to many neuro-imaging data especially from fMRI studies. Studies by Supekar et al. have shown that functional connectivity computed by the correlation approach provides clinically significant value specifically in Alzheimer’s patients. Studies by Skidmore et al. have shown functional connectivity computed by wavelet correlation analysis in individuals with idiopathic Parkinson’s disease. A graph theoretical metric, GE, was used in discriminating the functional connectivity patterns observed in these patients. We used the same metric to investigate further in healthy people how this metric is influenced among various cognitive loads. In contrast to these fMRI studies, we performed an analysis to prove that fNIRS can reliably be applied to obtain these metrics. Recently, Niu et al. used the graph theoretical network analysis approach to examine the topological organization of the human whole-brain functional network constructed using resting-state fNIRS data. Studies by Liu et al. have shown that functional connectivity computed again by the PC approach provides clinically significant values specifically in schizophrenia patients. Previous fNIRS studies have shown that patients with schizophrenia have impaired activity in the PFC. Taniguchi et al. measured reduced brain activity in PFC of schizophrenia patients.
patients compared to healthy controls during the Stroop task. GE has an intuitive interpretation, as higher connection weights intuitively correspond to shorter lengths.

In contrast to studies emphasizing whole-brain network, we found that data from a specific region (i.e., PFC) can be used to generate a global connectivity metric during cognitive tasks. As Eq. (3) dictates, GE is “the average inverse shortest path length” that may significantly contribute to an integration in larger and sparser networks. GE values are inversely related to link weights, as large weights typically represent strong associations, so might GE decrease as the cognitive activity becomes more demanding. GE results are consistent with the hypothesis that information transfer among the regions of PFC will increase with the increasing cognitive load. Path length provides a measure of the network’s capacity for serial information transfer among nodes, whereas global efficiency is a measure of the network’s capacity for parallel information transfer among nodes via multiple series of edges. Since the evidence is strong that the brain is already massively parallel processing, it seems preferable to adopt comprehensive measures of the efficiency of the brain’s functional network topology. Among various graph theory metrics, we focused on the GE as a marker of the engagement of the PFC with respect to cognitive load since on a global scale, GE quantifies the exchange of information across the whole network where information is concurrently exchanged while local efficiency quantifies a network’s resistance to failure on a small scale. That is, the local efficiency of a node characterizes how well information is exchanged by its neighbors when it is removed. Since PFC is usually considered to have been one large network, it would seem only reasonable to treat it as one network and so focused on a metric that would provide the connectivity of the whole network. Intrinsic functional networks of the human brain have been generated by EEG, fMRI, or MEG modalities and they all demonstrate a converging and highly conserved topological organization over different scales, such as small-world and modular structures. More importantly, some of these features exhibit specific changes associated with normal development, aging, and various pathological attacks, which indicates the potential value of these approaches in capturing and monitoring the brain organization under different mental states. Our findings on the decrease of GE as the cognitive demand increases might sound counterintuitive since a major hypothesis of network theory is that an adaptive network should reorganize itself to minimize its cost and increase efficiency under increasing load. Considering the increase in RT to represent an increase in cognitive load, we see a consecutive decrease in the GE values. There might be several explanations for this finding: (1) a flaw with the signal processing methodology and (2) a lack in observing only a piece of a larger network. The PC algorithm we employed uses the remaining 14 channels data as regressors for computing the correlation between the two channels. It is quite possible that this approach might be leading to an over regression (removing too much of the dependence) from the channels leading to a smaller correlation value. Hence the functional connectivity matrix calculated after this operation might leave only the very close channels as strongly correlated. This will eventually lead to a lower GE value. Second, PFC is a part of a larger brain network, albeit its fundamental role in decision-making, fNIRS has access only to this region and it might be quite possible that as the cognitive demand increases many other parts of the brain might be employed that are not visible to fNIRS sampling. Hence, we might be observing a piece of a network and the cognitive demand could be distributed over other parts of the brain. That could also explain a decrease in GE as the cognitive load increases.

4.1 Limitation of the Study

We reiterate the rationale behind our choice of this source–detector separation. This has been a long debate and many authors have favored the use of source–detector separations as close as 2.5 cm. In fact one of the pioneers of fNIRS, the late Dr. Britton Chance himself has used rectangular probe geometry with an SD separation of 2.5 cm in most of his studies. We would like to bring to your attention to a paragraph from his one of the most cited articles. The major intracerebral contribution probably comes from the gray matter. This has been confirmed in two studies performing PET and NIRS simultaneously that have shown the best correlation between PET and fNIRS parameters in the outer 1 cm of the brain tissue. Interestingly, it seems that even at interoptode distances as short as 2 to 2.5 cm gray matter is part of the sample volume. This is consistent with work assessing changes in local brain activity successfully with interoptode distances of 2.5 cm. Other authors have reported measurements at even smaller interoptode distances.

Our group has also shown through Monte Carlo simulations run on a realistic head model that we can actually probe the gray matter. We agree that the probed gray matter area will increase when the source–detector separation is enlarged to 3 cm, albeit at the cost of reduction in SNR. Even at an SD separation of 2.5 we are losing ~1/10th of the photons. Hence, this choice becomes an optimization issue. Even though only about 2% to 3% of the signal we collect comes from the gray matter, the dynamical changes observed and extracted with proper signal processing techniques correlate significantly with the task. Hence as engineers we are faced with the dilemma ensuring a deeper penetration depth via a larger SD separation at the expense of complexity and cost of equipment and bulkiness of the probe, or choosing an optimized distance at the expense of lesser probing of the gray matter but a higher SNR and far less inexpensive and complex instrumentation.

5 Conclusion

In this study, a modified version of the color-word matching Stroop task was employed during fNIRS data collection. The aim was to elucidate the adaptation of brain connectivity patterns in the PFC during the task. The data were preprocessed with WPC and local efficiency values were assessed among the 16 different regions. The findings show promise when interference between incongruent and neutral conditions is considered. The simple yet straightforward signal processing approach proposed may lead to new findings in the assessment of connectivity changes for diagnostic and prognostic purposes. The choice of this specific signal processing algorithm was motivated from the literature findings where a convergence was observed to a wavelet-based elimination of irrelevant physiological background activity and some instrumentation noise. The choice of PC to compute the functional connectivity matrix was motivated by the need to eliminate a common background systemic physiological activity that can be observed in each recording. The study is limited in its choice of the graph theoretical metrics to only global efficiency. Although many metrics could have been employed, we believe that global efficiency actually is the
major metric since it is derived from other metrics of graph theory.

Disclosures

No conflicts of interest, financial or otherwise, are declared by the authors.

References