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Abstract. We present measurements of the dispersion of two negative curvature fibers at and around 1 μm. These fibers are suitable for beam delivery of both high power and ultrashort pulse lasers with one designed to operate at 1030 nm and the other designed for dual wavelength delivery at 515 and 1030 nm. Both fibers were found to exhibit anomalous dispersion measured to be $2.17 \pm 0.25 \text{ ps nm}^{-1} \text{ km}^{-1}$ for the fundamental mode rising to $4.69 \pm 0.17 \text{ ps nm}^{-1} \text{ km}^{-1}$ for the first-order mode in the 1030-nm fiber. Dispersion in the double wavelength fiber was found to be higher at $3.81 \pm 0.03 \text{ ps nm}^{-1} \text{ km}^{-1}$ for the fundamental mode guiding at 1030 nm. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: 10.1117/1.OE.55.11.116106]

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1 Introduction

Ultrafast short pulsed (10 ps and shorter) lasers are increasingly used in a range of industrial and experimental areas that should benefit from flexible beam delivery systems over distances of a few meters, i.e., optical fiber; however, for fiber optic delivery of high peak power, ultrafast pulsed lasers are principally limited by either maximum energy densities or through fiber dispersion. In addition, there has been recent interest in hollow core fiber for low latency and ultralow loss telecommunication applications over longer kilometer scales.

Over the last few years, large mode area solid core and hollow core photonic crystal fibers have been presented as possible solutions to this fiber delivery problem. Neither, however, presents a complete solution to the problems of damage threshold and dispersion. Recently new designs of hollow core fibers, principally Kagomi fibers and negative curvature fibers (NCFs), have been proposed. Although there has been considerable interest in developing these fiber designs, there have been, to date, limited direct measurement of the dispersion of these fiber designs.

In this paper, we directly measure the dispersion of two hollow core NCFs at around 1 μm, a wavelength suitable for a range of machining applications that have been demonstrated with such fibers.

2 Negative Curvature Fiber

An NCF is a hollow core fiber guiding through the antiresonance reflecting optical waveguide principle. In essence, the core walls act as a Fabrey–Pérot cavity. Wavelengths in antiresonance with the core walls destructively interfere in transmission and are reflected back into the core providing confinement. Resonant wavelengths by comparison are transmitted from the core into the cladding and lost. Here, the wall thickness is critical to guidance and for operation at 1030 nm is of the order of 910 ± 50 nm.

An idealized structure for this form of fiber (for guidance around 1 μm) is an unsupported 910 nm capillary. This is not practical since a manufactured design requires a supporting structure. This structure includes nodes where supporting struts attach to the core walls. These nodes can themselves support highly lossy modes and, in order to reduce these losses, are pushed away from the guided mode by using negatively curved core walls.

Dispersion measurements of two fibers are presented in this paper. Both fibers were manufactured at the University of Bath and scanning electron microscope (SEM) images are presented in Fig. 1. One is designed to operate with the first-order transmission band around 1030 nm. For this fiber, the comparatively large core (~38 μm) of the fiber supports a small number (<4) of low attenuation core modes and as such is not pure single mode at either 1030 or 1064 nm. This fiber is similar to the fiber presented in Ref. [1], however, it is further optimized with an attenuation of 0.037 and 0.531 dB m⁻¹ at 1030 and 1064 nm, respectively (Fig. 1). This fiber is referred to as the first-order NCF.

The second fiber was designed to guide with a first-order transmission band at ~515 nm. As a result, the fiber has a zero-order transmission band at 1064 nm. Due to the smaller core size (~15 μm), this fiber can operate as a single mode at 1064 nm. Further details on this fiber operating in the green, and, in particular, the bend sensitivity can be found in Ref. [2]. For the purposes of this paper, it is enough to note that the attenuation at 1064 nm is somewhat higher at 0.174 dB m⁻¹ (Fig. 2) and that the transmission window is not smooth. This fiber is referred to as the zero-order NCF.
3 Experimental Setup

The experimental setup is based on the dispersive Fourier transform spectroscopy and specifically based on methods previously reported. This technique is based on measuring the phase difference between Fresnel reflections at the input and output surfaces of a fiber. However, in the case of the NCF, the core is hollow and there are no useable Fresnel reflections; hence, mirrors need to be introduced instead. For clarity, the measurement technique and, particularly, the data analysis used in these experiments are presented here in full.

3.1 Dispersion Measurement

A ~300-mm length of fiber was used (the exact length was determined after the experiment) mounted between two microblocks with a very slight slack. Ideally the fiber would be kept straight to prevent intermodal coupling; however, some flexibility is necessary to allow for fine alignment of the coupling both into and reflecting back from the fiber end.

While intermodal coupling was observed in one of the fibers the effective refractive index of adjacent modes is sufficiently large enough to allow the interference from the modes to be spatially separated along the scanning arm allowing for an unambiguous measurement (see Fig. 1 and Sec. 2.3). Figure 1 shows a schematic of the setup based on a Michelson interferometer. An air bearing retroreflector is used to form the scanning arm. This provides a scan length...
of up to 2 m due to the folded beam path. As the velocity of the retroreflector is not constant, a stabilized HeNe (633 nm) was used to measure the position of the scanning arm.

The HeNe light passes through an optical isolator, a pair of steering mirrors and is incident onto the beamsplitter. The transmitted light is reflected from a fixed reference mirror while the other passes through the retroreflector scanning arm. On recombination, the HeNe beams pass through a dichroic mirror and finally interfere on a silicon detector.

The optical source used for dispersion measurements was an Exalos EXS210063 SLED, centered at 1047 nm with a full width at half maximum (FWHM) bandwidth of 60.5 nm (coherence length \( \sim 8 \mu m \)). This was coupled to 10 m of Nuferen 1060XP fiber which is single mode over this bandwidth and acts as a mode filter. An optical polarizer was used to fix the polarization of the source with respect to the test fiber at launch. At the beamsplitter, the IR beam is split into test and scanning arms. The scanning arm light passes through and is returned back by the scanning retroreflector. The test arm light, meanwhile, is coupled through a pair of alignment mirrors and then into the NCF via a microblock arrangement. An aspheric optic is used to couple into the fiber providing an numerical aperture (NA) match for the given NCF and the measured optic is used to couple into the fiber providing an numerical aperture (NA) match for the given NCF and the measured optic is used to couple into the fiber providing an numerical aperture (NA) match for the given NCF and the measured optic is used to couple into the fiber providing an numerical aperture (NA) match for the given NCF and the measured optic is used to couple into the fiber providing an numerical aperture (NA) match for the given NCF and the measured optic is used to couple into the fiber providing an numerical aperture (NA) match for the given NCF.

Measurement surfaces (Ag mirrors) were introduced to the system to provide reflection both with and without the fiber in place. For the reference measurements, a mirror was mounted to the microblock at the focus of the coupling optic such that the reflection is returned and recollimated by the focusing optic [Fig. 4(a)]. Alignment of the reference mirror is trivial due to the microblock arrangement; this surface is referred to as the “front face.”

Alignment of the system to the fiber is more challenging. By use of a CCD and observing the output of the fiber, it was possible to dynamically adjust the coupling conditions to ensure primarily single mode transmission through the fiber [Fig. 4(b)]. This CCD can observe the far field and, using a 20x microscope objective, near field in transmission.

In the measurement arrangement, this mirror is moved into contact (butt-coupled) with the output of the NCF. This mirror is mounted on a x, y tilt mirror mount to facilitate alignment [Fig. 4(c)]. Alignment of the second reflective surface, referred to as the “back face,” in contact with the NCF must be carefully adjusted to ensure the returned beam fills the fundamental mode as fully as possible. A high speed camera (Kodak EKTAPro 45401mx) was used at the position of the detectors (Fig. 4) to observe the far field and allow dynamic adjustment of the mirror-recoupling conditions. This camera was also used for Fourier imaging (cf. Sec. 3.2).

Data were acquired by a free running LeCroy 9354L 500 MHz oscilloscope recording the intensity at both the 1030 and 633 nm silicon detectors simultaneously. Up to 2.5 mm of scan data were acquired for each measurement, sufficient to include the complete interferogram from either the front or back reflection. At this rate, data were taken at \( \sim 1 \) nm increments with a single interferogram recorded in \( \sim 80 \) ms. As outlined in Sec. 3.2, multiple interferograms were recorded for each reflection surface, a process taking \( \sim 2 \) min, and then combined and processed to calculate the dispersion as outlined in Sec. 3.2.

3.2 Mode Identification

As mentioned above, the fiber supports a small number of modes. For this experiment, the fiber length and the different effective refractive indices of these modes are sufficient for modes to appear separately within the scanned data. Although it can be assumed that the shortest path length (hence lowest effective refractive index) corresponds to the fundamental mode, we believed it necessary to verify this experimentally. This was accomplished by performing a Fourier analysis on the two-dimensional far-field image at the measurement point. A Kodak EKTAPro HS camera imaging at 40.5 kHz was used to image the interferograms at a sufficient rate to resolve the interferograms (this camera can also be used to aid alignment of the back face mirror). These data were then processed to provide an image of the interfering mode as outlined in Sec. 3.2. Note that this measurement was, by necessity, carried out separately from the dispersion measurement.

![Flow diagram of data processing process for a single measurement.](https://www.spiedigitallibrary.org/journals/Optical-Engineering)
4 Data Processing

4.1 Dispersion

A flow chart of the data processing steps is presented in Fig. 5. To convert the collected data to a useable format, it was first necessary to interpolate and resample the IR intensity data to equal, known, scan distance steps. To do this, the HeNe data were used. Each individual fringe of the HeNe interferogram (i.e., \( \pi \) phase, \( 633/2 \) nm) was fitted to a sinusoid and the phase extracted for each datum. This phase information was unwrapped over the whole dataset and converted to a distance, zeroed arbitrarily at the shortest scan length datum.

As the HeNe and IR data were acquired simultaneously on two channels of the oscilloscope this distance map can be applied directly to the IR data. A first-order interpolation of the IR dataset was calculated at equal distance intervals of 5 nm (this length is longer than the data spacing in the raw data but sufficiently short to provide ample data over each IR fringe to prevent aliasing).

In general, there may be more than one mode, and therefore more than one interferogram present in the data. In order to measure the dispersion of an individual mode, the data were windowed. With the interferograms suitably windowed, the data were zero padded to the next \( 2^n \) dataset size and a fast Fourier transform (FFT) taken. The absolute components of the FFT correspond to intensity information, i.e., transmission spectrum at the two interfaces. This provides

![Figure 6](https://example.com/fig6.png)  
**Fig. 6** Example interferogram from front face. NB scan distance has been zeroed to center of interferogram.

![Figure 7](https://example.com/fig7.png)  
**Fig. 7** Result of Fourier mode analysis for front face of first-order NCF: (a) intensity and (b) phase. A single maxima is visible in both images indicating a fundamental mode.

![Figure 8](https://example.com/fig8.png)  
**Fig. 8** Example interferogram from the back face for first-order NCF. NB zero path length difference has been centered to the fundamental mode. (a) Light coupled primarily into the fundamental mode and (b) significant coupling into the first-order mode.
a useful check to determine if the system is working correctly. The argument components of the FFT correspond to the phase information and are therefore used to calculate the dispersion of the fiber.

To calculate the group velocity dispersion (GVD), the phase, as a function of angular frequency, is fitted to a second-order polynomial across a nominal bandwidth range. For these experiments, the bandwidth used corresponds to 40 nm, which is smaller than the FWHM of the source (60.5 nm). The phase is fitted to the second-order polynomial for the front and back faces independently. These phase equations are subtracted to determine the phase change across the fiber. The GVD between the two interfaces can then be calculated as

$$d = -\frac{\omega^2}{2\pi c} \frac{\partial^2 f}{\partial \omega^2} \frac{\Delta \theta}{\frac{\Delta \omega}{C}}. \tag{1}$$

where $d$ is the GVD, $c$ is the speed of light, $\omega$ is the angular frequency, and $f$ is the function describing the phase change due to the fiber. Taking the second derivative here eliminates the uncertainty due to an arbitrary zero phase from the unwrapping of the argument of the Fourier transform.

This provides the dispersion between the two interfaces; by dividing the path length within the fiber (twice the NCF length), the dispersion may be calculated as

$$d_{NCF} = -\frac{d_{\text{meas}}}{2l}. \tag{2}$$

where $d_{NCF}$ is the GVD of the NCF, $d_{\text{meas}}$ is the measured GVD between the two interfaces, and $l$ is the length of the NCF under test. Care must be taken with the units to ensure a final result is given in ps · nm⁻¹ · km⁻¹. This value corresponds to the dispersion of the source at the central wavelength of the bandwidth used for the phase fit.

This process can be repeated for several fitted bandwidths to give the slope of the GVD within the overall bandwidth of the source. This process was repeated for 20 separate measurements for averaging and statistical error measurement.

4.2 Fourier Imaging

The data collected from the fast camera may be used to identify modes by measuring the shape of the mode actively interfering within each burst of the interferogram. This is achieved by windowing the data for a specific burst and examining the Fourier transform of the data collected by each individual pixel on the camera separately. Within the FFT, there is a peak associated with the fringes moving across the pixel. By plotting the magnitude of both the absolute (intensity) and argument (phase) of this peak for each pixel, an image of the interfering mode can be reconstructed. More details of this process can be found in Ref. 21.

5 Results

5.1 First-Order NCF

Figure 9 shows an example resampled interferogram from the front face. This shows a clear single mode, single
interface, interference burst and Fig. 7 shows the result of the Fourier analysis which also demonstrates a single mode.

Figure 8 shows example resampled interferograms from the back face. This indicates that a series of modes have been coupled into the NCF. The first (left hand) interference burst is expected to correspond to the fundamental mode, since it has the lowest effective refractive index. There is a second clear mode at an effective path length of $+240$ μm from the fundamental and a series of less well defined low power modes between them. It was found that the proportion of radiation coupled into each mode could be altered by changing the coupling conditions into the fiber as can be seen by comparing Figs. 8(a) and 8(b).

The Fourier mode analysis, Fig. 8, confirms that the left-hand mode is the fundamental while the right-hand mode is a first-order mode. The dispersion of both the fundamental and first-order modes may be measured separately by windowing data suitably. Figure 9 shows the windowed data corresponding to the fundamental and first-order modes.

The length of the fiber was measured using a position tracking microscope as 296.2 mm, the error in this case can be assumed to be insignificant (at worst ±0.5 mm) since the error in the GVD dominates. Figure 11 shows the result of calculated GVD taken from 20 separate measurements of both the fundamental and first-order modes. The mean GVD and 1-sigma error were measured to be $2.17 \pm 0.25$ ps · nm$^{-1}$ · km$^{-1}$ for the fundamental mode and $4.69 \pm 0.17$ ps · nm$^{-1}$ · km$^{-1}$ for the first-order mode, both at 1030 nm.

5.2 Zero-Order NCF

Figure 12 shows an example back interferogram from this fiber which is single mode. The Fourier analysis of the interfering mode confirms that the mode is a fundamental mode (Fig. 13).

As only one mode is present, the windowing conditions for the Fourier transform are not critical. The length of the fiber was measured using a microscope as 542.4 mm, the error in this case can be assumed to be insignificant (at worst ±0.5 mm) since the error in the GVD dominates. Figure 14 shows the results of the GVD calculation. Results are the mean of 20 measurements with a 1-sigma error. The dispersion at 1030 nm is $3.81 \pm 0.03$ ps · nm$^{-1}$ · km$^{-1}$.
Conclusions
Both fibers exhibit low anomalous dispersion. In the 1030-nm fiber, the dispersion of the fundamental mode is, as expected, lower than the first-order mode. Likewise the dispersion of the 515-nm fiber is higher than the 1030-nm fiber, and most likely this is a result of the larger overlap between core mode and (glass) cladding as a result of a smaller core. Although the measured dispersion curves are nonmonotonic, this behavior may potentially be correlated with local loss deatures seen in the transmission spectra in Figs. 4 and 5 due to the complex guidance mechanics of these fibers, e.g., coupling between cladding and fundamental modes linked to, wavelength-dependent loss, variations in the overlap between the propagating mode and glass. (and hence the GVD), or even localized degradation of the fiber structure. Further discussion of this correlation may be found in Ref. 23; however, more efforts are needed to further explore this topic which is beyond the scope of this paper.

Overall the dispersion is low, illustrating the feasibility for guiding high peak power, ultrashort pulses for industrial and telecommunication applications.

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References

Fig. 13 Results of Fourier analysis of the mode measured in the back interferogram for the zero-order NCF: (a) intensity and (b) phase. The mode is fundamental.

Fig. 14 Calculated GVD of the zero-order NCF. Results are the mean of 20 separate measurements with error bars corresponding to 1-sigma error.

6 Conclusions
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