Near-field chiral excitation of universal spin-momentum locking transport of edge waves in microwave metamaterials

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Abstract. Controlling energy flow in waveguides has attractive potential in integrated devices from radio frequencies to optical bands. Due to the spin-orbit coupling, the mirror symmetry will be broken, and the handedness of the near-field source will determine the direction of energy transport. Compared with well-established theories about spin-momentum locking, experimental visualization of unidirectional coupling is usually challenging due to the lack of generic chiral sources and the strict environmental requirement. In this work, we design a broadband near-field chiral source in the microwave band and discuss experimental details to visualize spin-momentum locking in three different metamaterial waveguides, including spoof surface plasmon polaritons, line waves, and valley topological insulators. The similarity of these edge waves relies on the abrupt sign change of intrinsic characteristics of two media across the interface. In addition to the development of experimental technology, the advantages and research status of interface waveguides are summarized, and perspectives on future research are presented to explore an avenue for designing controllable spin-sorting devices in the microwave band.

Keywords: chirality; metamaterials; microwaves; spoof surface plasmon polaritons; waveguides.

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1 Introduction

The quantum spin-Hall state is an electronic surface state with immunity against defects.1 The momentum is locked to the intrinsic spin of electrons, and backward transports are suppressed unless the spin flips.2 Analogous phenomena have been widely reported in various uniform and metamaterial waveguides, where theories of universal spin-momentum locking4 and spin-orbit interactions5,6 have been well studied. Uniform waveguides include closed metal waveguides, fibers, and plasmonic metals, where the unidirectional transmission can be realized based on nano-gratings,7 circularly polarized (CP) dipoles or Huygens dipoles8 supported by resonant particles.10–14 Metamaterial waveguides consist of various artificial unit cells, where chiral sources carrying spin angular momentum (SAM) and orbital angular momentum (OAM) can interact with unit cells in versatile ways to realize unidirectional coupling.15 Recent research interest is mainly in metamaterial interfaces supporting edge waves. As shown in Fig. 1(a), two metamaterials are stitched together to construct an infinitely thin interface to support edge waves, such as spoof surface plasmon polaritons (SPPs), line waves (LWs), and photonic topological insulators (PTIs). All these kinds of edge waves are related to flipping change of intrinsic characteristics of media across the interface, as shown in Figs. 1(b)–1(d).

It is beneficial to further design generic chiral sources and visualize unidirectional coupling in different metamaterial waveguides. Spoof SPPs exist on the interface between the
dielectric medium with positive permittivity ($\varepsilon_{\text{air}} > 0$) and periodic metallic structures with negative effective permittivity ($\varepsilon_{\text{eff}} < 0$), as shown in Fig. 1(b). Spoof SPPs contain fruitful phenomena related to spin-orbit momentum.\textsuperscript{20,21} It is convenient to use modulated gratings to couple CP spatial waves to unidirectional spoof SPPs on an open metasurface.\textsuperscript{22} However, it is challenging to apply similar technology to one-dimensional infinitely thin spoof SPPs transmission lines\textsuperscript{23,24} due to the small cross section. Therefore, one purpose of this work is to develop a near-field chiral source to visualize spin-momentum locking in spoof SPPs transmission lines. LWs exist in the interface of a pair of metasurfaces with duality symmetry, such as reactance duality ($Z_{\text{TM}} > 0$ and $Z_{\text{TE}} < 0$)\textsuperscript{25-27} or resistance duality (gain and loss),\textsuperscript{28} as shown in Fig. 1(c). LWs have been experimentally observed by linearly polarized feedings;\textsuperscript{29,30} however, unidirectional coupling stays in the simulation stage,\textsuperscript{28,29} where related experiments are still lacking. Therefore, the second part of this work is to visualize the spin-momentum locking of LWs. PTIs show flipping Berry phase in topological space, as shown in Fig. 1(d). The chirality of eigenmodes of unit cells determines the robust transmission direction along the edge.\textsuperscript{31,32} Spin-momentum locking can be realized with a linearly polarized source in Chern PTIs because the time symmetry is broken.\textsuperscript{33-35} However, in valley topological waveguides, chiral eigenmodes require spin-orbit coupling.\textsuperscript{36} The coupling theory was first studied in a pseudo-spin structure\textsuperscript{37} and proved by experiments.\textsuperscript{38} Connections between OAM and valley transmission were also reported.\textsuperscript{39,40} It is important to further measure unidirectional valley PTIs, which is the third part of this work.

This work presents near-field experiments to visualize unidirectional edge waves in various metamaterial waveguides. By flipping the chirality of the source, we can control the direction of energy coupling. The presented experimental methodology is universal and tutorial to realize spin-sorting metamaterial devices in the microwave band. We further compare characteristics of different waveguides, summarize research status, and present perspectives regarding the following challenges and future spin-sorting metamaterial devices implanted with modern coding techniques.

Fig. 1 Spin-momentum locking exists at the interface of two metamaterials. (a) The chirality of the source decides the transmission direction. Unidirectional transmission at the interface between: (b) spoof SPPs: air and corrugated structures ($\varepsilon_{\text{air}} > 0$, $\varepsilon_{\text{eff}} < 0$); (c) LWs: dual-impedance surfaces ($Z_{\text{TM}} > 0$, $Z_{\text{TE}} < 0$); and (d) PTIs: Berry phase flips.

2 Results

2.1 Angular Momentum

Chiral sources carrying SAM and OAM are the key to couple metamaterial waveguides with spin-momentum locking. Figures 2(a) and 2(b) show two feeding configurations used in this work.

SAM (helicity $\sigma = \pm 1$) is realized by the spinning electric vector consisting of orthogonal electric components with $\pi/2$-phase difference. We take a short review of the spin-momentum locking theory.\textsuperscript{4} The complex wavevector of evanescent waves is in a general form as $k = k' + ik''$. $k'$ is the real part related to the phase constant, and $k''$ is the imaginary part related to the decay. $k'$ and $k''$ are orthogonal, and we can divide evanescent waves into two polarizations denoted by $\hat{s}$ and $\hat{p}$. $\hat{s}$ is perpendicular to the plane formed by $k'$ and $k''$, while $\hat{p}$ is in the plane,

\[
\hat{s} = i \frac{k \times k^*}{|k| \times k^*}, \quad (1)
\]

\[
\hat{p} = i \frac{k \times (k \times k^*)}{|k| \times k^*}, \quad (2)
\]

and, we further substitute the complex form of wavevector into Eq. (2) and obtain

\[
\hat{p} = i \left[ \frac{k''}{|k|} k' \right] + i \frac{k'}{|k|} \left[ \frac{k''}{k'} \right], \quad (3)
\]

where the combination of orthogonal vectors indicates a $\pi/2$-phase difference in $\hat{p}$, verifying an elliptically polarized field whose spin direction can be represented by the purely real $\hat{s}$. As the slow-wave effect is enhanced, both real and imaginary parts of the wavevector become larger ($|k'| \approx |k''| \gg k_0$), and the field becomes nearly perfectly CP. Therefore, we can lock
the direction of coupling by placing a CP source around the interface, as shown in Fig. 2(c). As examples, various CP-sensitive metamaterials were proposed to realize unidirectional performance.11,42

OAM is dependent on the chiral phase distribution of the field. The polarization of the probes is identical, but the chiral phase carries OAM with the vortex charge \( l = 0, \pm 1, \pm 2, \ldots \), which represents the total phase change \( (2\pi \times l) \) along a closed circle. SAM and OAM can transfer between each other by focusing or scattering.6,43 As shown in Fig. 2(d), assuming an incoming CP electric field \( E \) in the global circular basis of \((x + iay)\)-polarizations and the \( z \) component, we can obtain the scattering field \( E_s \) from a particle as45

\[
E_s = \begin{bmatrix} 1 + a & -be^{-i\phi} & -\sqrt{2}abe^{-i\phi} \\ -be^{i\phi} & 1 + a & -\sqrt{2}abe^{i\phi} \\ -\sqrt{2}abe^{-i\phi} & -\sqrt{2}abe^{i\phi} & 2b^2 \end{bmatrix} E, \tag{4}
\]

where \( a = \cos^2 \theta \) and \( b = \sin^2 \theta \). The off-diagonal elements are responsible for SAM-OAM conversion, which is the theoretical background for unidirectional coupling based on lens and nanoparticles.11,44,45

To feed the chiral probe array, we designed a broadband power divider with the \( \pi/2 \)-phase-shifting function. Figure 2(e) shows the five-port feeding network designed for measurements. The fabricated circuit consists of three power-dividers and three pairs of phase shifters,46 whose detailed structure is presented in the Supplementary Material. Figures 2(f) and 2(g) show the measured amplitude and phase relationships at different ports. Results indicate that signals at the four out-ports keep almost the same amplitude with the desired phase shift from 5 to 12 GHz.

2.2 Spoof SPPs

The proposed platform to observe spoof SPPs is shown in Fig. 3(a), where ideal absorptive terminals are based on two kinds of slots loading with gradient resistors,17 as shown in Fig. 3(b). The corrugated metallic structure supports spoof SPPs on the interface, and the electric field vectors have spin momentum, deciding the energy transport direction shown in Fig. 3(c). The depth of the slot decides the cut-off frequency of spoof SPPs, as shown in Fig. 3(d). When the frequency is above 5 GHz and below 15 GHz, the shallow slots can support spoof SPPs, while deep slots avoid detouring waves. Therefore, spoof SPPs are bounded along the route along the \( y \) axis. Animated comparisons of spoof SPPs on different structures are shown to demonstrate the importance of the terminal designs.

The experimental setup is shown in Fig. 4(a). The CP source consists of a pair of orthogonal electric probes of negligible electric size and is placed at the center of the structure. With the CP source, we use two linearly polarized electric probes to record the transmission energy at two terminals of the structure. The right hand circularly polarized (RHCP) source can direct energy toward the right, and the energy level received at the left terminal is much lower, as shown in Fig. 4(b). We further set up RHCP and left hand circularly polarized (LHCP) sources to record the energy distribution along the edge, as shown in Fig. 4(c), verifying that sources with opposite chirality can direct energy toward opposite directions. The two-dimensional (2D) electric field distribution of the planar structure is shown in Fig. 4(d), where the forward transport is much stronger than the backward transport. Figure 4(e) demonstrates a conformal situation where spoof SPPs can travel on a curved surface and unidirectional coupling can still be observed in Fig. 4(f), indicating the robustness of spin-momentum locking on the flexible surface. Experiments match well with simulations, as shown in Videos 1 and 2.
Two metasurfaces with opposite reactance are designed, as shown in Fig. 5(a), where the enlarged illustration shows the configuration of a CP source with a pair of orthogonal electric dipoles with a π/2-phase difference. The periodic serpentine acts as an inductive surface and can be named $Z_{TM}$ surfaces because the fundamental surface mode is transverse magnetic (TM) polarization. The interdigitated patch array acts as a capacitive surface and can be named $Z_{TE}$ surfaces because the fundamental mode is transverse electric (TE) polarization.
surface mode is transverse electric (TE) polarization. The cross section of the electric field distribution is shown in Fig. 5(b). The electric field vector is mainly perpendicular to the $Z_{TM}$ surface but parallel to the $Z_{TE}$ surface. At the interface between two surfaces, energy is concentrated, and electric field vectors twist. Simulated dispersion curves of two surface modes and LWs are plotted in Fig. 5(c), and the equivalent surface reactance can be extracted from the phase constant. The authors proposed and analyzed the structures recently, but related experiments to visualize the spin-momentum locking are challenging and have been solved in this work.

We set up the experimental environment as shown in Fig. 6(a). CST Studio Suite is utilized to conduct simulations, and results are shown in Fig. 6(b). The CP source is placed beneath the metasurface. A linearly polarized probe is used to record the electric field distribution on the surface. The measured electric field distribution is shown in Fig. 6(c). Excited by the LHCP source, energy is directed toward the left side. We compare the animation of simulated and measured field distributions in Video 3, and the consistency can verify the existence of unidirectional transport. The visualization of LWs is not as clear as that of spoof SPPs because two metasurfaces on both sides can support the surface waves whose operating frequencies overlap with LWs, as shown in Fig. 5(c). It is challenging to suppress the unwanted surface waves when we excite the LWs with a CP source that has the omnidirectional radiation pattern. More work remains to be done to improve the structure of feeding probes.

2.4 PTIs

The valley waveguide under study is based on 10-mm height alumina rods with two PEC plates on top and bottom layers to restrict waves in the structure as TM modes with an out-of-plane electric field ($E_z$), as shown in Fig. 7(a). A cardboard made by a laser engraving procedure is placed in the middle of two PEC plates to fix dielectric rods. Figure 7(b) shows the analysis of the unit cell. We can observe the opening of the
Dirac cone at highly symmetric points when the structure transforms from $C_6$-to $C_3$-symmetric, and the corresponding intrinsic OAM ($l = \pm 1$) of the eigenmode is reflected in the phase distribution. Therefore, we can place a chiral source with OAM ($l = C_6^{-1}$) at the center of a unit cell to couple the unidirectional valley transport. The Berry curvature is calculated based on the four-point formula procedure. The superlattice simulation is shown in Fig. 7(c); the dispersion curves and energy confinement at the interface verify the existence of topological edge waves within the bandgap.

It is interesting to further discuss the performance of different OAM sources. We consider two parameters: different vortex charge $|l|$ and different phase stepping $\Delta \phi$. By modeling different sources (Supplementary Material), we analyze the corresponding unidirectional coupling spectra, as shown in Figs. 7(d) and 7(e). Two findings are summarized as follows.

1. The first-order OAM ($l = \pm 1$) is the best choice to realize the unidirectional coupling of the first-order valley PTIs because the eigen phase distribution of a unit cell decides that the vortex charge number equals $\pm 1$.

2. $\pi/2$-phase sampling is sufficient. By fixing the vortex charge ($l = 1$) and changing the sampling number, we can optimize the performance slightly when $\Delta \phi$ decreases from $2\pi/3$ to $\pi/2$, but the performance no longer shows any improvement when further decreasing $\Delta \phi$. The experimental setup is shown in Fig. 8(a), where the source carrying OAM ($l = 1$) is placed in the center of a unit cell beside the interface. It is a general concept that robust unidirectional PTIs can radiate at open terminals without obvious reflection. However, it is still unclear whether we can change the terminal shape without generating reflection. Inspired by horn antennas, we propose a horn-type terminal to guide valley PTIs toward the center of the open terminal as shown in Fig. 8(b). The traditional open terminal as a counterpart has a splitting distribution at the aperture. We record the field distributions at different terminals to verify the correctness of the simulation, as shown in Fig. 8(c). The concentrated and the splitting distributions match well with simulations, although the unidirectional coupling exists in both structures. Transmission is recorded by a linearly polarized probe, as shown in Fig. 8(d), where unidirectional valley PTIs exist within the bandgap. Animations of the valley PTIs at different terminals are compared in Videos 4 and 5.

3 Perspectives

Based on the generic chiral sources, we conducted microwave experiments to visualize unidirectional coupling in different metamaterial waveguides. We compare the key characteristics in Table 1 and present perspectives regarding applications and challenges in the future.
Three waveguides all have chiral sorting abilities. Incident waves with SAM and OAM can excite the unidirectional transmission. As similar evanescent waves, LWs inherit most features of spoof SPPs, but the unidirectional LWs based on OAM remain unsolved. Unlike the spoof SPPs and LWs stemming from the complex wavevector of evanescent waves, the unidirectional PTIs rely on the eigenmodes carrying SAM and OAM. Spoof SPPs and LWs can exist over a broad band, indicating the potentials in broadband communication systems; however, PTIs only exist within a narrow photonic bandgap. The narrow bandwidth of PTIs limits the communication capability but has advantages in designing high-Q and robust cavities in laser applications.

Another difference is the wave velocity. Spoof SPPs and LWs are slow waves, while the closed PTIs waveguides can support both slow and fast waves without leakage. From the perspective of assembly process, people can use flexible substrates, such as polyimide, to guide the spoof SPPs and LWs along curved surfaces, indicating the potential applications in wearable networks. PTIs usually exist in solid hole-slab or pillars, losing the flexibility. However, the unique immunity against defects is under topological protection, which can be the key for non-reciprocal devices and on-chip high robust links.

The scale of semiconductor devices is much smaller than the wavelength; therefore, it is crucial to explore device-assisted metamaterials beyond the conventional structural designs. Recently, plenty of exotic spoof SPPs components have been reported, such as parametric amplifiers, active Fano sensors, and nonlinear harmonic generators. Compared to vigorous active spoof SPPs, the device-assisted technology is still a virgin land in LWs and PTIs because they require loading devices in the form of 2D arrays. The concept of device-assisted LWs was first reported as a terahertz tunable simulation model based on graphene, lacking further experimental work. Meanwhile, the first device-assisted PTIs platform was reported recently, and more fruitful work remains to be explored.

The future direction of spin-sorting metamaterials could be in the hybrid form of massive loading devices and novel structures. Related embedding fabrication and controlling technologies have shown significant achievements in recent digital

### Table 1 Characteristics of Three Waveguides in the Microwave Band

<table>
<thead>
<tr>
<th>Metamaterial waveguides</th>
<th>Chiral sorting</th>
<th>Working bandwidth</th>
<th>Wave velocity</th>
<th>Transmission robustness</th>
<th>Potential applications</th>
<th>Device-assisted</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spoof SPPs</td>
<td>SAM/OAM</td>
<td>Broadband</td>
<td>Slow</td>
<td>Flexibility</td>
<td>Wearable, compact circuits</td>
<td>Vigorous</td>
</tr>
<tr>
<td>LWs</td>
<td>SAM/OAM</td>
<td>Broadband</td>
<td>Slow</td>
<td>Flexibility</td>
<td>Multifunctional metasurfaces</td>
<td>Unexplored</td>
</tr>
<tr>
<td>PTIs</td>
<td>SAM/OAM</td>
<td>Narrow</td>
<td>Slow/fast</td>
<td>Immunity</td>
<td>Isolators and cavities</td>
<td>Early stage</td>
</tr>
</tbody>
</table>
Digital coding metamaterial waveguides with spin-momentum locking. (a) Spoof SPPs: manipulating the wavevector and bi-directional chiral sorting. (b) LWs: manipulating impedance to tailor the arbitrary transmission and control the scattering performance of metasurfaces at the same time. (c) PTIs: manipulating the topological invariant to realize dynamic chiral sorting multiplexers.

4 Conclusion

We developed the experimental technologies to visualize the unidirectional transports of edge waves in three different metamaterial waveguides in the microwave band. The key mechanism behind spoof SPPs, LWs, and PTIs is the abrupt sign change of different intrinsic properties of artificial media across the interface. We discussed the advantages and research status and presented an outlook for future metamaterial devices based on modern digital coding technology and controllable spin-momentum locking.

Acknowledgments

Z.X. proposed the concept, conducted simulations, designed experiments, and wrote the main content. J.T. set up the experimental equipment, fabricated samples, and did measurements under the guidance of Z.X. J.T. participated in experiments, organized data, and prepared supplemental information. D.F.S. and T.J.C. supervised the project. All authors discussed the results and co-wrote the paper. This work was supported by the State Key Laboratory of Millimeter Waves (Grant No. K202202). T.J.C. acknowledges the support of the National Key Research and Development Program of China (Grant Nos. 2017YFA0700201, 2017YFA0700202, and 2017YFA0700203). The authors declare no competing interests.

Code, Data, and Materials Availability

Supporting materials are available. The data that support the findings of this study are available from the corresponding author upon reasonable request.

References

29. Z. Xu et al., “Line waves existing at junctions of dual-impedance metasurfaces,” ACS Photonics 8(8), 2285–2293 (2021).

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