Static and dynamic light scattering of healthy and malaria-parasite-invaded red blood cells

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Abstract. We present the light scattering of individual Plasmodium falciparum-parasitized human red blood cells (Pf-RBCs), and demonstrate progressive alterations to the scattering signal arising from the development of malaria-inducing parasites. By selectively imaging the electric fields using quantitative phase microscopy and a Fourier transform light scattering technique, we calculate the light scattering maps of individual Pf-RBCs. We show that the onset and progression of pathological states of the Pf-RBCs can be clearly identified by the static scattering maps. Progressive changes to the biophysical properties of the Pf-RBC membrane are captured from dynamic light scattering.

Keywords: red blood cell; plasmodium falciparum; light scattering; malaria; electric field.

Static and dynamic light scattering techniques have been widely used to study the structure and dynamics of scattering objects. Static (elastic) light scattering measures the angular distribution of the scattering intensity to infer structural information of scatterers, which is utilized to probe the structure of living cells or tissues. Dynamic (quasielastic) light scattering is the extension of elastic light scattering to study dynamic inhomogeneous systems. Several techniques have been used to study light scattering, including photon correlation spectroscopy, diffuse wave spectroscopy, dynamic scattering microscopy and single-cell partial-wave spectroscopy. Recently, Fourier transform light scattering (FTLS), which numerically calculates far-field scattering patterns from the electric field (E-field) measurement, has been developed.

Light scattering of red blood cells (RBCs) has also been extensively studied. Static light scattering of RBCs has been widely used in flow cytometry for measuring size and hemoglobin (Hb) concentration distribution. Numerical models have been introduced to simulate static light scattering of RBCs. Dynamic light scattering has been used to study the dynamic motion of RBC membranes. The RBC membrane cortex is sufficiently soft and elastic, and it exhibits dynamic membrane fluctuations driven by both thermal and metabolic energies. These membrane fluctuations are influenced by mechanical properties of the membrane, and serve as an important indicator of RBC deformability, which in turn plays an important role in the evolution of a number of human diseases.

When invaded by the malaria-inducing parasite P. falciparum host RBCs undergo substantial changes. The parasite causes modifications in the structure, mechanical properties, and biochemical characteristics of the host RBCs. In response to these changes, the characteristic biconcave shape of the RBC is lost, the dynamics of membrane fluctuations are altered, and the Hb concentration in RBC cytoplasm decreases. These changes could affect both static and dynamic light scattering of Pf-RBCs. In this study, the E-field maps of individual Pf-RBCs were measured and utilized to determined both static and dynamic light scattering distributions. We show that the static light scattering patterns of Pf-RBCs are significantly different among different disease states at specific scattering angle windows. We also present dynamic light scattering to characterize transitions from intact membranes of healthy RBCs to modified membranes of Pf-RBCs.

We prepared RBCs in four different groups following the standard protocol: healthy RBCs, and three parasite matura-
tions stages of Pf-RBCs with 14 to 24 h (late ring stage), 24 to 36 h (trophozoite stage), and 36 to 48 h (schizont stage) after the invasion of the P. falciparum merozoite. We first measured the light-intensity scattering patterns of individual Pf-RBCs by FTLS. The physical principle of FTLS is to measure the complex E-field at the image plane and then numerically propagate this E-field to the far-field scattering plane. To quantitatively measure the E-field maps of Pf-RBCs, we employed diffraction phase microscopy (DPM).

For each individual RBC, we measured the E-field $I(x,y,t) = A(x,y,t)\exp[j\phi(x,y,t)]$, where $A(x,y,t)$ is the amplitude, and $\phi(x,y,t)$ is the phase at a position of $(x,y)$ at time $t$ [Figs. 1(a) and 1(b)]. This E-field is divided by the E-field without samples to normalize the intensity of the incident beam. From the measured E-field, the far-field scattering intensity is calculated by using a 2-D Fourier transform,

$$I(q_x,q_y,t) = \frac{1}{2\pi} \int \int E(x,y,t)\exp(-jq_xx) \times \exp(-jq_yy)dxdy,$$

where $q_x$, $q_y$ are spatial frequencies. The time-averaged (static) scattering intensity map $I(q_x,q_y)$ of a healthy RBC is shown in Fig. 1(c).

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We then retrieved the scattering patterns of Pf-RBCs at different pathological states. By utilizing the FTLS method, we can easily locate an individual Pf-RBC in the field of view and measure both imaging and scattering maps of the sample simultaneously. To our knowledge there has been no prior study of light scatterings of Pf-RBCs. The light scattering patterns with respect to the different parasitization stages are plotted as a function of scattering angle from 0 to 41 deg after azimuthal average and converting the spatial frequency to angle, by using the relation $q = 2\pi n \sin \theta / \lambda$, where $\lambda$ is the wavelength of the laser, and $n$ is the refractive index of the medium. The scattering patterns of healthy RBCs show the distinct periodic oscillatory features, which are consistent with previous measurements and simulations. For the Pf-RBCs, not only did the oscillatory patterns change, especially for higher angles (>10 deg), but the scattering intensities at 0 deg also decreased by 16.6% (ring-), 30.7% (trophozoite-), and 65.7% (schizont stage) compared to healthy RBCs. This indicates clearly identifiable decreases in refractive index between the RBC cytoplasm and the medium, which is consistent with the previous Hb concentration measurement. This trend can be explained by the reduction in Hb concentration in the cytoplasm as the invading parasite digests Hb from its host RBCs. To test whether these scattering patterns can distinguish the different parasite maturation stages from healthy RBCs, we performed the two-tailed Mann–Whitney rank sum tests. The $p$-values of Pf-RBCs versus healthy RBCs were smaller than 0.01 for the low scattering angle range (0 to 2 deg and 4 to 5 deg). At this angle range, each parasite development stage of Pf-RBCs can be statistically differentiated based on the static light scattering signals; averaged $p$-values are 0.005 (ring versus trophozoite stage) and <10^{-7} (trophozoite versus schizont stage). This suggests that the presence of the Pf-RBCs, and even the particular parasite development stage, can be clearly detected by static light scattering techniques at these specific angles.

To measure the dynamic light scattering in individual Pf-RBCs, we measured the E-field maps of Pf-RBCs for about 2 s at 120 frames per s. For each E-field map, we calculated the intensity fluctuations $\langle I(\tau)I(0)\rangle / \langle I(0)^2 \rangle$ [Fig. 2(a)]. The spectrum of the

![Fig. 1](image-url) (a) Amplitude and (b) phase map of a healthy RBC. (c) The retrieved light scattering pattern of the same cell. Light-intensity scattering patterns of (d) healthy RBCs, (e) ring, (f) trophozoite, and (g) schizont stage of Pf-RBCs. (h) $p$-values of scattering patterns (different intraerythrocytic stages of Pf-RBCs are compared to the healthy RBCs).

![Fig. 2](image-url) Dynamic light scattering of Pf-RBCs. (a) Normalized temporal autocorrelations of a healthy RBC as a function of decay time and scattering angle. (b) Normalized temporal autocorrelation of a healthy RBC at two representative scattering angles and fitted curves. (c) Line width $\Gamma$ extracted from healthy and Pf RBCs as a function of scattering angle. Symbols represent the mean value and the error bars indicate the standard error for 15 RBCs. (d) Scatter plot of $\omega_0$ versus $\Gamma$ taken for healthy and Pf RBCs. Each symbol represents mean values of 15 RBCs at scattering angles (0 to 21 deg). Lines indicate the boundaries of each group.
scattered light can be described approximately as Lorentzian, having a peak frequency $\omega_0$ and a line width $\Gamma$, and its autocorrelation is described as a damped cosine function:

$$G(\tau) = A + B \cos(\omega_0 \tau + \varphi) \exp(-\Gamma \tau) \exp(-\beta^2 \tau^2).$$  \hspace{1cm} (1)

The phase term $\varphi$ is added to include the deviation of the spectrum from an exact Lorentzian form, and the $\beta$ term represents the instrumental variations. For individual RBCs, the intensity autocorrelation was calculated at each scattering angle, from which $\omega_0$ and $\Gamma$ were retrieved by fitting to Eq. [1] [Fig. 2(b)]. The extracted values of $\Gamma$ showed significant differences between healthy RBCs and Pf-RBCs for the scattering angles 0 to 25 deg. Peak frequencies $\omega_0$ did not show significant differences between the pathological states (results not shown). The $\omega_0$ and $\Gamma$ values for the scattering angles 0 to 21 deg are plotted in Fig. 2(d). Compared to Pf-RBCs, healthy RBCs show small values for $\omega_0$ and $\Gamma$ (around 2 and 3.5 Hz, respectively), and small cell-to-cell variations. However, the values of Pf-RBCs span larger areas (2 to 8 Hz for $\omega_0$ and 1 to 8 Hz for $\Gamma$). We employed the support vector machines method, a machine learning technique for classification, to generate contour lines that separate different stages of Pf-RBCs [Fig. 2(d)]. To better address the alterations in the dynamic light scattering signals accompanied with the progress of intraerythrocytic stages of *P. falciparum*, we performed a t-test using a new complex parameter $\psi_0 = \omega_0 + i \beta$. The $p$-values are $<10^{-17}$, $<10^{-8}$, and $<10^{-5}$ for ring versus Healthy, trophozoite versus ring, and schizont versus trophozoite, respectively. For a simple flat lipid bilayer model, $\omega_0$ is directly related to membrane tension and $\Gamma$ to viscosity of medium. However, for a complex curved RBC membrane cortex, there is no theoretical model to relate dynamic light scattering signals, and thus it is not straightforward to quantitatively extract mechanical parameters from the values for $\omega_0$ and $\Gamma$. Nevertheless, we can qualitatively interpret that the increase of $\omega_0$ can result from increased stiffness or decreased mass for membrane cortex, and the increase in $\Gamma$ from increased viscosity. Taken together, this result indicates that mechanical properties of RBC membrane undergo significant modifications during pathological states induced by parasite maturation within the RBC, which can result from the stiffening of the membrane cortex and the formation of membrane-bounded proteins.

In conclusion, by analyzing the E-field images with the FTLS technique, we report static and dynamic light scattering maps of individual Pf-RBCs, and demonstrate a novel methodology to identify and distinguish pathological intraerythrocytic stages of *P. falciparum* malaria. The static scattering maps of individual cells showed that the scattering pattern can distinguish the specific disease states. The dynamic scattering results suggest alterations in mechanical properties of Pf-RBC membranes, consistent with other independent experimental measurements that employed optical tweezers. These results demonstrate that light scattering can only detect Pf-RBCs, but can also be utilized to assess biological questions about the pathophysiology of the malaria infection, as well as other RBC-related diseases.

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**References**