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Exhibition of circular Bragg phenomenon by hyperbolic, dielectric, structurally chiral materials

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Abstract. The relative permittivity dyadic of a dielectric structurally chiral material (SCM) varies helicoidally along a fixed direction; in consequence, the SCM exhibits the circular Bragg phenomenon, which is the circular-polarization-selective reflection of light. The introduction of hyperbolicity in an SCM—by making either one or two but not all three eigenvalues of the relative permittivity dyadic acquire negative real parts—does not eliminate the circular Bragg phenomenon, but significantly alters the regime for its exhibition. Significantly wider circular-polarization-sensitive stopbands may be exhibited by hyperbolic SCMs in comparison to non-hyperbolic SCMs. Physical vapor deposition techniques appear to be suitable to fabricate hyperbolic SCMs. © The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI. [DOI: [10.1117/1.JNP.8.083998](https://doi.org/10.1117/1.JNP.8.083998)]

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1 Introduction

Chiral liquid crystals^{1,2} and chiral sculptured thin films^{3,4} are dielectric examples of structurally chiral materials (SCMs)—which are anisotropic and helicoidally nonhomogeneous along a fixed axis. If that fixed axis is parallel to the z -axis of a Cartesian coordinate system with unit vectors $\hat{\mathbf{u}}_x$, $\hat{\mathbf{u}}_y$, and $\hat{\mathbf{u}}_z$, the frequency-domain constitutive relations of dielectric SCMs may be set down as

$$\left. \begin{aligned} \mathbf{D}(\mathbf{r}) &= \varepsilon_0 \underline{\underline{\varepsilon}}_r(z) \bullet \mathbf{E}(\mathbf{r}) \\ &= \varepsilon_0 \underline{\underline{S}}_z(z) \bullet \underline{\underline{S}}_y(\chi) \bullet (\varepsilon_a \hat{\mathbf{u}}_z \hat{\mathbf{u}}_z + \varepsilon_b \hat{\mathbf{u}}_x \hat{\mathbf{u}}_x + \varepsilon_c \hat{\mathbf{u}}_y \hat{\mathbf{u}}_y) \bullet \underline{\underline{S}}_y^T(\chi) \bullet \underline{\underline{S}}_z^T(z) \bullet \mathbf{E}(\mathbf{r}) \\ \mathbf{B}(\mathbf{r}) &= \mu_0 \underline{\underline{H}}(\mathbf{r}), \end{aligned} \right\}, \quad (1)$$

where the superscript T denotes the transpose; μ_0 and ε_0 are the permeability and permittivity of free space; the rotational nonhomogeneity is expressed through the dyadic

$$\underline{\underline{S}}_z(z) = \hat{\mathbf{u}}_z \hat{\mathbf{u}}_z + (\hat{\mathbf{u}}_x \hat{\mathbf{u}}_x + \hat{\mathbf{u}}_y \hat{\mathbf{u}}_y) \cos\left(\frac{h\pi z}{\Omega}\right) + (\hat{\mathbf{u}}_y \hat{\mathbf{u}}_x - \hat{\mathbf{u}}_x \hat{\mathbf{u}}_y) \sin\left(\frac{h\pi z}{\Omega}\right), \quad (2)$$

with 2Ω as the helical pitch and either $h = +1$ for structural right-handedness or $h = -1$ for structural left-handedness; the dyadic

$$\underline{\underline{S}}_y(\chi) = (\hat{\mathbf{u}}_x \hat{\mathbf{u}}_x + \hat{\mathbf{u}}_z \hat{\mathbf{u}}_z) \cos \chi + (\hat{\mathbf{u}}_z \hat{\mathbf{u}}_x - \hat{\mathbf{u}}_x \hat{\mathbf{u}}_z) \sin \chi + \hat{\mathbf{u}}_y \hat{\mathbf{u}}_y \quad (3)$$

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Fig. 1 Cross-sectional scanning electron micrograph of a chiral sculptured thin film made by thermal evaporation of a chalcogenide glass.

containing $\chi \in [0 \text{ deg}, 90 \text{ deg}]$ as the angle of rise of the helical morphology; and ϵ_a , ϵ_b , and ϵ_c are the three z -independent eigenvalues of the relative permittivity dyadic $\underline{\epsilon}_r(z)$. Typically, dissipation is small enough to be ignored and $\epsilon_{a,b,c} > 0$; hence, $\underline{\epsilon}_r(z)$ is positive definite.⁵

Figure 1 shows a cross-sectional image of a chiral sculptured thin film. For SCMs of this kind, the adequacy of the continuum constitutive equations (1) at sufficiently large free-space wavelengths has been established experimentally.^{6,7} A nanoscopic-to-continuum model based on the Bruggeman homogenization formalism has also been developed.⁸

The optical signature of an SCM is a circular-polarization-sensitive stopband. The center wavelength and the width of this stopband depend on the direction of the wavevector of an incident circularly polarized plane wave. Most significantly, the stopband is exhibited when the incident plane wave's handedness is the same as the structural handedness of the SCM, but not otherwise. The stopband is best seen when the thickness of the SCM exceeds a certain number of helical pitches.^{6,9–11} When dissipation is small enough to be ignored, $\underline{\epsilon}_r(z)$ is positive definite, and the variations of $\epsilon_{a,b,c}$ with respect to the free-space wavelength λ_0 are also small enough to be ignored, the circular-polarization-sensitive stopband can be delineated as⁴

$$\frac{\lambda_0}{2\Omega} \in \begin{cases} \left[\frac{\sqrt{\epsilon_c}, \sqrt{\epsilon_d}}{\sqrt{\epsilon_d}, \sqrt{\epsilon_c}} \right] \cos^{1/2} \theta, & \epsilon_c < \epsilon_d, \\ \left[\frac{\sqrt{\epsilon_d}, \sqrt{\epsilon_c}}{\sqrt{\epsilon_c}, \sqrt{\epsilon_d}} \right] \cos^{1/2} \theta, & \epsilon_c > \epsilon_d, \end{cases} \quad (4)$$

where θ is the angle of incidence with respect to the z -axis and

$$\epsilon_d = \frac{\epsilon_a \epsilon_b}{\epsilon_a \cos^2 \chi + \epsilon_b \sin^2 \chi}. \quad (5)$$

Provided that $\text{Re}[\epsilon_\sigma] \gg |\text{Im}[\epsilon_\sigma]|$ for all $\sigma \in \{a, b, c\}$, the estimates provided by Eq. (4) can be used with ϵ_c replaced by $|\epsilon_c|$ and ϵ_d by $|\epsilon_d|$. The exhibition of the circular-polarization-sensitive stopband is called the circular Bragg phenomenon.

During the last 10 years, attention has been paid to dielectric-magnetic materials with indefinite permeability and permittivity dyadics.^{12,13} Although the practical realization of such materials remains a matter of conjecture, there is no doubt of the existence in nature of dielectric materials the real parts of whose permittivity dyadics are indefinite.⁵ Graphite,¹⁴ triglycine sulfate,^{15,16} sapphire,¹⁷ and bismuth¹⁶ are examples. Metal nanowire arrays¹⁸ and periodic metal/dielectric multilayers¹⁹ provide examples of manufactured anisotropic dielectric materials whose effective permittivity dyadics have indefinite real parts.²⁰ Periodic graphene/dielectric multilayers have also been proffered as candidates.²¹ Although dissipation due to conduction in metals and graphene has been predicted to be offsetable by using dielectric materials with optical gain,²² the effective-medium approximations underlying such predictions must be handled with some care.²³

Experience with ambichiral materials^{24,25} indicates that hyperbolic, dielectric SCMs ought to be practically realizable as nanoengineered periodic multilayers. A variety of physical deposition techniques—such as thermal evaporation, electron-beam evaporation, and sputtering²⁶—can be used to deposit alternating layers of a metal and a dielectric material on a suitably rotating planar substrate.⁴ In these fabrication techniques, collimated vapor fluxes of both materials must be directed very obliquely toward the substrate in order to engender biaxiality. Furthermore, the nominal thickness of each metal layer must be a small fraction of the nominal thickness of each dielectric layer,²³ and all layers must be electrically thin.^{27,28} Equation (1) would still apply, although the use of the nanoscopic-to-continuum model⁸ developed for chiral sculptured thin films may be perilous if the metal volume fraction is not sufficiently small.²⁹ Anyhow, either one or two of $\text{Re}(\epsilon_a)$, $\text{Re}(\epsilon_b)$, and $\text{Re}(\epsilon_c)$ could be negative, with the remainder being positive. Then, with dissipation assumed to be sufficiently small, the estimates provided by Eq. (4) would become dubious. Indeed, the question arises: will a hyperbolic SCM exhibit the circular Bragg phenomenon?

In order to answer this question, a one-point boundary-value problem was formulated and solved. In this problem, the half space $z < 0$ is vacuous while the half space $z > 0$ is occupied by the hyperbolic SCM, and a circularly polarized plane wave is obliquely incident on the interface $z = 0$ from its vacuous side. As it is known that the circular Bragg phenomenon develops as the thickness of an SCM increases,^{4,10} an SCM half space should conceptually deliver the best developed circular Bragg phenomenon. The underlying boundary-value problem is introduced briefly in Sec. 2, the detailed procedure to solve it being available elsewhere.³⁰ Numerical results are provided and discussed in Sec. 3. An $\exp(-i\omega t)$ dependence on time t is implicit, with

Fig. 2 Reflectances R_{LL} , R_{RL} , R_{RR} , and R_{LR} as functions of $\lambda_0/2\Omega$ and θ , when $\epsilon_a = 3.26(1 + 0.001i)$, $\epsilon_b = 4.46(1 + 0.001i)$, $\epsilon_c = 3.78(1 + 0.001i)$, $\chi = 60$ deg, and $h = 1$. The color coding employs the spectrum of the rainbow with the deepest violet denoting 0 and the deepest red denoting 1.0.

ω denoting the angular frequency and $i = \sqrt{-1}$. The free-space wavenumber is denoted by $k_0 = \omega\sqrt{\epsilon_0\mu_0} = 2\pi/\lambda_0$.

2 Boundary-Value Problem

Let the half space $z < 0$ be vacuous, while the half space $z > 0$ be occupied by an SCM described by Eqs. (1)–(3). An arbitrarily polarized plane wave is obliquely incident on the interface $z = 0$ from the vacuous half space. Without significant loss of generality, let the wave vector of this plane wave lie wholly in the xz -plane and make an angle $\theta \in [0 \text{ deg}, 90 \text{ deg}]$ with respect to the $+z$ -axis. Accordingly, the electric field phasor of the incident plane wave may be written as

$$\mathbf{E}_{\text{inc}} = \left(a_L \frac{i\hat{\mathbf{u}}_y - \mathbf{p}_+}{\sqrt{2}} - a_R \frac{i\hat{\mathbf{u}}_y + \mathbf{p}_+}{\sqrt{2}} \right) \exp[ik_0(x \sin \theta + z \cos \theta)], \quad z \leq 0, \quad (6)$$

where a_L and a_R are the known amplitudes of the left- and right-circularly polarized components, respectively, and the vectors

$$\mathbf{p}_{\pm} = \mp \hat{\mathbf{u}}_x \cos \theta + \hat{\mathbf{u}}_z \sin \theta \quad (7)$$

are of unit magnitude. The reflected plane wave's electric field phasor is given by

$$\mathbf{E}_{\text{ref}} = \left(-r_L \frac{i\hat{\mathbf{u}}_y - \mathbf{p}_-}{\sqrt{2}} + r_R \frac{i\hat{\mathbf{u}}_y + \mathbf{p}_-}{\sqrt{2}} \right) \exp[ik_0(x \sin \theta - z \cos \theta)], \quad z \leq 0, \quad (8)$$

Fig. 3 Same as Fig. 2, except that $\epsilon_b = 4.46(-1 + 0.001i)$.

with unknown amplitudes r_L and r_R . The procedure to determine r_L and r_R in terms of a_L and a_R is described in detail elsewhere.³⁰

The reflection amplitudes are related to the incidence amplitudes by the four reflection coefficients entering the 2×2 matrix in the following relation:

$$\begin{bmatrix} r_L \\ r_R \end{bmatrix} = \begin{bmatrix} r_{LL} & r_{LR} \\ r_{RL} & r_{RR} \end{bmatrix} \begin{bmatrix} a_L \\ a_R \end{bmatrix}. \quad (9)$$

The copolarized reflectances of the SCM half space are denoted by $R_{LL} = |r_{LL}|^2$ and $R_{RR} = |r_{RR}|^2$, and the cross-polarized ones by $R_{LR} = |r_{LR}|^2$ and $R_{RL} = |r_{RL}|^2$. The principle of conservation of energy requires that $R_R = R_{RR} + R_{LR} \leq 1$ and $R_L = R_{LL} + R_{RL} \leq 1$.

3 Numerical Results and Discussion

Parametric calculations were made with the SCM assumed to be structurally right-handed ($h = 1$), with all three of $\epsilon_{a,b,c}$ chosen to have very small and positive imaginary parts (that are indicative of weak dissipation). The reflectances R_{LL} , R_{RL} , R_{RR} , and R_{LR} were computed as functions of the angle of incidence θ and either (i) the normalized wavelength $\lambda_0/2\Omega$ for fixed angle of rise χ or (ii) χ for fixed $\lambda_0/2\Omega$.

In order to set a baseline for discussion, Fig. 2 displays all four reflectances as functions of the normalized wavelength $\lambda_0/2\Omega$ and the angle of incidence θ , when $\chi = 60^\circ$ and the SCM is of the regular (i.e., nonhyperbolic) type: $\epsilon_a = 3.26(1 + 0.001i)$, $\epsilon_b = 4.46(1 + 0.001i)$, and

Fig. 4 Same as Fig. 2, except that $\epsilon_a = 3.26(-1 + 0.001i)$, $\epsilon_c = 3.78(-1 + 0.001i)$, and $\chi = 15^\circ$.

$\varepsilon_c = 3.78(1 + 0.001i)$. A sigmoid ridge of high values of R_{RR} is evident in this figure. The limits provided in Eq. (4) with ε_σ replaced by $|\varepsilon_\sigma|$, $\sigma \in \{a, b, c\}$, are satisfied by this ridge. For $\theta \lesssim 70$ deg, R_{LL} is negligible in that portion of the $(\lambda_0/2\Omega) - \theta$ plane which is occupied by the high- R_{RR} ridge; additionally, both cross-polarized reflectances are very small. The huge excess of R_{RR} over R_{LL} accompanied by very small values of the two other reflectances is the chief manifestation of the circular Bragg phenomenon.

When the sign of $\text{Re}(\varepsilon_b)$ was altered from positive to negative, the SCM of Fig. 2 became hyperbolic and the sigmoid high- R_{RR} ridge of that figure disappeared. However, a search with somewhat higher values of $\lambda_0/2\Omega$ soon revealed a portion of the $(\lambda_0/2\Omega) - \theta$ plane in which (i) R_{RR} exceeds R_{LL} by a large margin and (ii) the excess of R_R over R_L is even greater, with R_{LL} very close to 0. In Fig. 3, circular-polarization-selective reflection is clearly evident for $\lambda_0/2\Omega \in [1.95, 2.4]$ and $\theta \in [0 \text{ deg}, 20 \text{ deg}]$ as well as in the upper left neighborhood of that rectangular zone, for the hyperbolic SCM.

Next, for the computation of the reflectances presented in Fig. 4 as functions of $\lambda_0/2\Omega$ and θ , the following parameters were used: $\varepsilon_a = 3.26(-1 + 0.001i)$, $\varepsilon_b = 4.46(1 + 0.001i)$, $\varepsilon_c = 3.78(-1 + 0.001i)$, and $\chi = 15$ deg. Thus, two of the three eigenvalues of $\underline{\varepsilon}_r(z)$ now have negative real parts. Circular-polarization-selective reflection with R_{LL} almost equal to 0 is evident in Fig. 4 for $\lambda_0/2\Omega \in [2, 2.2]$ and $\theta \in [0 \text{ deg}, 70 \text{ deg}]$ as well as on the outskirts of this rectangular zone in the $(\lambda_0/2\Omega) - \theta$ plane.

Fig. 5 Reflectances R_{LL} , R_{RL} , R_{RR} , and R_{LR} as functions of χ and θ , when $\varepsilon_a = 3.26(1 + 0.001i)$, $\varepsilon_b = 4.46(-1 + 0.001i)$, $\varepsilon_c = 3.78(1 + 0.001i)$, $\lambda_0/2\Omega = 1.918$, and $h = 1$. The color coding employs the spectrum of the rainbow with the deepest violet denoting 0 and the deepest red denoting 1.0. The thin white strips for $\theta < 20$ deg and $\chi \approx 40$ deg indicate a failure of the computational algorithm (Ref. 30).

The circular-polarization-sensitive stopband for normal incidence can be identified as $1.87 \lesssim (\lambda_0/2\Omega) \lesssim 1.95$ in Fig. 2, $1.95 \lesssim (\lambda_0/2\Omega) \lesssim 2.4$ in Fig. 3, and $1.8 \lesssim (\lambda_0/2\Omega) \lesssim 2.3$ in Fig. 4. Thus, a significant conclusion from these three figures is that hyperbolicity tends to widen the stopband. However, this conclusion may have to be modified when material dispersion manifested through the λ_0 -dependences of $\varepsilon_{a,b,c}$ is taken into account.

The exhibition of the circular Bragg phenomenon by a regular SCM for fixed values of $\lambda_0/2\Omega$ and θ is delineated by Eq. (4). One just has to ensure the appropriate choices of ε_c and ε_d , the correct choice of the latter parameter being determined by the correct choices of ε_a , ε_b , and χ . If all three of the eigenvalues of $\underline{\varepsilon}_r(z)$ are fixed as well, then an appropriate value of $\sin \chi$ must be found. But no physical value of χ may emerge. Therefore, the exhibition of circular-polarization-selective reflection by hyperbolic SCMs was investigated in the $\chi - \theta$ plane for fixed values of ε_a , ε_b , ε_c , and $\lambda_0/2\Omega$.

Figure 5 shows all four reflectances computed as functions of $\chi \in [0 \text{ deg}, 90 \text{ deg}]$ and $\theta \in [0 \text{ deg}, 90 \text{ deg}]$, when $\varepsilon_a = 3.26(1 + 0.001i)$, $\varepsilon_b = 4.46(-1 + 0.001i)$, $\varepsilon_c = 3.78(1 + 0.001i)$, and $\lambda_0/2\Omega = 1.918$. Thus, only one of the three eigenvalues of $\underline{\varepsilon}_r(z)$ has a negative real part. At least four distinct zones of high values of R_{RR} accompanied by almost zero values of R_{LL} and very low values of both cross-polarized reflectances can be identified in this figure.

Similar data computed for $\varepsilon_a = 3.26(-1 + 0.001i)$, $\varepsilon_b = 4.46(1 + 0.001i)$, and $\varepsilon_c = 3.78(-1 + 0.001i)$ are displayed in Fig. 6. Now, two of the three eigenvalues of $\underline{\varepsilon}_r(z)$ have negative real parts. Circular-polarization-selective reflection with $R_{LL} \approx 0$ and very low values of R_{LR} and R_{RR} is evident for $\chi \in [0 \text{ deg}, 15 \text{ deg}]$ and $\theta \in [0 \text{ deg}, 70 \text{ deg}]$.

Fig. 6 Same as Fig. 5, except $\varepsilon_a = 3.26(-1 + 0.001i)$, $\varepsilon_b = 4.46(1 + 0.001i)$, and $\varepsilon_c = 3.78(-1 + 0.001i)$.

To conclude, the concept of hyperbolic SCMs was introduced in this communication. The hyperbolicity was found to significantly alter—but not eliminate—the exhibition of the circular Bragg phenomenon, which has long been known to be the distinctive signature of nonhyperbolic SCMs such as cholesteric liquid crystals⁹ and chiral sculptured thin films.⁶ Although practical realization of hyperbolic SCMs has yet to occur, physical vapor deposition offers suitable techniques to fabricate these materials. Significantly wider circular-polarization-sensitive stopbands may be exhibited by hyperbolic SCMs in comparison to their nonhyperbolic analogs.

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