Explicit dosimetry for 2-(1-hexyloxyethyl)-2-devinyl pyropheophorbide-a-mediated photodynamic therapy: macroscopic singlet oxygen modeling

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Abstract. Type II photodynamic therapy (PDT) is based on the photochemical reactions mediated through an interaction between a photosensitizer, ground-state oxygen (\(^{3}{O_2}\)), and light excitation at an appropriate wavelength, which results in production of reactive singlet oxygen (\(^{1}{O_2}\)). We use an empirical macroscopic model based on four photochemical parameters for the calculation of \(^{1}{O_2}\) threshold concentration \(\left( {^{1}{O_2}_{\text{th}}^{\text{sh}}} \right)\) causing tissue necrosis in tumors after PDT. For this reason, 2-(1-hexyloxyethyl)-2-devinyl pyropheophorbide-a (HPPH)-mediated PDT was performed interstitially on mice with radiation-induced fibrosarcoma (RIF) tumors. A linear light source at 665 nm with total energy released per unit length of 12 to 100 J/cm and source power per unit length (LS) of 12 to 150 mW/cm was used to induce different radii of necrosis. Then the amount of \(^{1}{O_2}_{\text{th}}^{\text{sh}}\) calculated by the macroscopic model incorporating explicit PDT dosimetry of light fluence distribution, tissue optical properties, and HPPH concentration was correlated to the necrotic radius to obtain the model parameters and \(^{1}{O_2}_{\text{th}}^{\text{sh}}\). We provide evidence that \(^{1}{O_2}_{\text{th}}^{\text{sh}}\) is a better dosimetric quantity for predicting the treatment outcome than PDT dose, which is proportional to the time integral of the products of the photosensitizer concentration and light fluence rate. © 2015 Society of Photo-Optical Instrumentation Engineers (SPIE)

Keywords: photodynamic therapy; explicit dosimetry; singlet oxygen; 2-(1-hexyloxyethyl)-2-devinyl pyropheophorbide-a photosensitizer; photodynamic therapy-induced necrosis; in vivo mice study.

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1 Introduction

Photodynamic therapy (PDT) is currently undergoing intensive clinical investigations as an adjuvant treatment for proliferative disorders including cancer.1-3 PDT involves the administration of a photosensitizer, which preferentially accumulates in diseased cells, followed by light excitation at a specific wavelength.1,3-5 The photosensitizer transfers energy to ground-state tissue oxygen (\(^{3}{O_2}\)) and generates reactive singlet state oxygen (\(^{1}{O_2}\)), which is the main cytotoxic species causing a therapeutic effect upon reacting with the surrounding biological molecules. Although PDT targets and destroys the malignant cancer cells in a way that causes significantly less side effects compared with current standard treatments such as surgery, radiation therapy, and chemotherapy,1,3-5 there are still obstacles preventing the widespread clinical use of PDT. Because PDT is a triple component treatment that includes interactions between light, photosensitizer, and \(^{3}{O_2}\), a well-defined single PDT dosimetry quantity that ties in with these components and correlates better with PDT efficacy than the well-established quantity of PDT dose will also be beneficial to ensure reliable clinical outcome for PDT clinical trials.

Under well-oxygenated conditions, PDT dose, which is proportional to the time integral of the product of local photosensitizer concentration and light fluence rate, is the most well-defined dosimetric quantity and a good predictor of treatment outcome in explicit PDT dosimetry.6,7 However, theoretical and in vivo mouse studies have shown that due to oxygen consumption by PDT, severe hypoxia can be created at high fluence rates (\(\phi\)) during light illumination and can result in less effective PDT treatment.6,7 To quantitatively account for the biological damage done by PDT, it was suggested to account for \(^{1}{O_2}\) production during PDT based on its luminescence signals at a wavelength of 1270 nm.6,9 Correlating the concentration of reactive singlet oxygen, \(^{1}{O_2}_{\text{th}}^{\text{sh}}\), with the treatment outcome has been a long-term goal in PDT dosimetry. However, the weak and short lifetime of the luminescence signals due to the rapid reactions of \(^{1}{O_2}\) with biological environments is a major obstacle to the use of this method in clinical and interstitial applications.6,9 An empirical four-parameter macroscopic model was proposed to calculate the apparent \(^{1}{O_2}\) concentration.6,7 This model utilizes the complete set of PDT kinetic equations, light diffusion, and oxygen supply mechanism, which can be applied in any clinical treatment geometry. In this macroscopic model, the four PDT parameters of specific oxygen consumption rate (\(\xi\)), ratio of photobleaching to reaction between \(^{3}{O_2}\) and cellular targets (\(\sigma\)), ratio of triplet state (T) phosphorescence to reaction between T and \(^{3}{O_2}\) (\(\beta\)), and oxygen supply rate to tissue (\(\gamma\)) can be determined by introducing a fitting quantity called the “reacted singlet oxygen threshold concentration” \(\left({^{1}{O_2}}_{\text{th}}^{\text{sh}}\right)^{\text{ox}}\).

The aim of this study was to use the macroscopic model to optimize the magnitude of the photochemical parameters (\(\xi, \sigma, \gamma, \beta\)) and \(^{1}{O_2}_{\text{th}}^{\text{sh}}\) for in vivo 2-(1-hexyloxyethyl)-2-devinyl pyropheophorbide-a (HPPH)-mediated PDT. A series of PDT, including a range of total energy released per unit length, 12 to 100 J/cm [light source strength (LS) = 12 to 150 mW/cm and exposure times from 400 to 3600 s], was
used to induce different necrotic radii in mouse models bearing radiation-induced fibrosarcoma (RIF) tumors. Based on the data obtained from the control mice (no HPPH injection, but catheter insertion and light exposure), the spontaneous necrosis and the necrosis induced by catheter insertion or light exposure were subtracted from the final necrosis measurements. The spatially and temporally resolved $[^1\text{O}_2]_{\text{rx}}$ was calculated based on the measurements of the tissue optical properties as well as $\phi$ and HPPH concentration in the tumor. Then the PDT-induced necrotic radius was fit to the calculated $[^1\text{O}_2]_{\text{rx}}$ to obtain the HPPH photochemical parameters and the range of $[^1\text{O}_2]_{\text{rx}}$.

A preliminary study of HPPH-mediated PDT did not account for spontaneous necrosis, or necrosis induced by catheter insertion and/or illumination, that should be subtracted from the final necrosis measurements. The resulting parameters of $\xi$ and $[^1\text{O}_2]_{\text{rx}}$ were erroneous and were corrected in this study.\(^{11}\) In order to provide a straightforward comparison of PDT dose to $[^1\text{O}_2]_{\text{rx}}$, the magnitude of the radius of necrosis due to PDT was correlated to $[^1\text{O}_2]_{\text{rx}}$ as well as the total PDT dose at the same tumor depth.

## 2 Theory and Method

### 2.1 Theory of the Macroscopic $^1\text{O}_2$ Model

By simplifying and combining the energy transfer processes in PDT, a set of governing equations is produced which describes the creation of $[^1\text{O}_2]_{\text{rx}}$. These equations are dependent on various parameters such as the light source ($s$), optical absorption ($\mu_s$) and reduced scattering ($\mu_s'$) coefficients, and photochemical parameters ($\xi$, $\sigma$, $g$, $\beta$). The empirical macroscopic model includes the spatial distribution of $\phi$ and the complete set of equations describing the photochemical reactions in type II PDT is used to calculate $[^1\text{O}_2]_{\text{rx}}$. In this model, the spatial distribution of $\phi$ in the tumor is calculated via Eq. (1), based on the diffusion approximation. Spatial and temporal distribution of the ground state photosensitizer ($S_0$) and $^3\text{O}_2$ and $^1\text{O}_2$ concentrations are obtained by solving a set of coupled time-dependent differential equations initially proposed by Foster et al.\(^{12,13}\) and later expanded by Hu et al.\(^{14}\) and our group\(^{7,10,15}\) for macroscopic modeling. As the singlet and triplet state photosensitizers ($[S_1]$ and $[T]$) as well as $^1\text{O}_2$ decay or react with cellular targets immediately after they are created, their lifetimes are very short (nanoseconds to microseconds). Therefore, their temporal changes ($d[S_1]/dt$, $d[T]/dt$, and $d[^1\text{O}_2]/dt$) are set to zero to derive the following equations:

$$\frac{\partial \phi - \mu_s' \cdot \nabla \phi}{\mu_s} = s, \quad (1)$$

$$\frac{d[S_0]}{dr} + \left( \xi \frac{\phi [S_0] + \delta [^3\text{O}_2]}{[^1\text{O}_2] + \beta} \right) [S_0] = 0, \quad (2)$$

$$\frac{d[^1\text{O}_2]}{dt} + \left( \xi \frac{\phi [S_0]}{[^3\text{O}_2] + \beta} \right) [^3\text{O}_2] - g \left( 1 - \frac{[^1\text{O}_2]}{[^1\text{O}_2]_0} \right) = 0, \quad (3)$$

$$\frac{d[^1\text{O}_2]_{\text{rx}}}{dr} = f \cdot \left( \frac{\phi [S_0]}{[^3\text{O}_2] + \beta} \right), \quad (4)$$

where $g$ is the maximum oxygen supply rate, and the particular form was validated in a separate study based on uniformly distributed vascular structures.\(^{15}\) $\delta$ is the correction parameter for low photosensitizer concentration, and $[^1\text{O}_2]_0$ denotes the initial oxygen concentration. $f$ represents the fraction of $[^1\text{O}_2]$ interacting with the tissue substrate. A more detailed derivation of the equations and parameters can be found elsewhere.\(^3\)

### 2.2 Establishment of the Mouse Tumor Models for In Vivo Studies

The animal protocol (803929) was approved by the University of Pennsylvania Institutional Animal Care and Use Committee (IACUC). RIF tumors were propagated on the shoulders of female C3H mice (~9-weeks old; NCI-Frederick, Frederick, Maryland) by the subcutaneous injection of a suspension of $1 \times 10^6$ cells/μl. When the tumors reached ~8 mm in diameter and depth (~10 days after the injection of in vitro maintained cells), the mice received 0.25 mg/kg HPPH via tail vein injection. Then following the HPPH drug-light interval of 24 h, interstitial PDT was delivered to induce tumor necrosis (see Figs. 1(a) and 1(b)). Animal husbandry was provided by the University of Pennsylvania Laboratory Animal Resources in Association for Assessment and Accreditation of Laboratory Animal Care (AALAC)-accredited facilities according to protocols approved by the University of Pennsylvania IACUC.

### 2.3 Measurements of the Tissue Optical Properties and Intertitial 2-(1-Hexyloxyethyl)-2-Devinyl Pyropheophorbide-a Concentration

Optical properties in vivo are the critical quantities that determine in tissues. As shown in Fig. 1(a), two parallel catheters
were inserted into the tumor, one in the center of the tumor and the other 3 mm from the central catheter, close to the bottom of the tumor edge to measure the tissue optical properties, $\mu_a$ and $\mu'_s$. A 2-mm point source emitting 665-nm light was inserted into the central catheter. The light fluence profile along the second catheter was obtained using an isotropic detector and a motorized system to scan the tumor length. The measured fluence values were fitted using the diffusion approximation to extract the absorption and scattering properties of the tumor.

PDT is influenced by the concentration of the photosensitizer. In order to determine the photosensitizer concentration in the tumor, a single side-cut fiber was connected to a dichromatic filter, and served as both an excitation source and a detector. This was inserted into the detector catheter placed 3 mm from the cylindrical diffusing fiber (CDF) to record the interstitial HPPH fluorescence emission spectrum along the catheter axis. The photosensitizer was excited using a 405-nm diode laser. The raw spectrum was fitted to the basic spectrum of HPPH and autofluorescence in the absence of HPPH using singular value decomposition (SVD). The attenuation of the photosensitizer fluorescence signal due to the light absorption and scattering by tissue can be corrected by applying a correction factor (CF), which is a function of $\mu_a$ and $\mu'_s$. First, a calibration curve was determined between raw fluorescence SVD and various HPPH concentrations ranging from 0 to 0.7 mg/kg (0 to 1.1 $\mu$M). Then a set of liquid phantoms was prepared with varying optical properties ($\mu_a = 0$ to 0.6 cm$^{-1}$, $\mu'_s = 7$ to 20 cm$^{-1}$) and a constant HPPH concentration of 0.39 $\mu$M (0.25 mg/kg) using Intralipid (Fresenius Kabi, Uppsala, Sweden) as the scatterer and ink (Parker Quink) as the absorber. Optical properties of each phantom were measured and fluorescence spectra were obtained. An empirical CF of the following equation was used to convert SVD to the corrected SVD ($\text{SVD}_{\text{cor}}$):

$$\text{CF} = A \cdot \frac{\exp(B \cdot \sqrt{3\mu_a\mu'_s})}{\mu'_s},$$  \hspace{1cm} (5)

$$\text{SVD}_{\text{cor}} = \text{SVD} \cdot \text{CF},$$ \hspace{1cm} (6)

where $A$ and $B$ are the constants determined from fitting the fluorescence SVD for different optical properties to a single value.

After applying the CF [Eq. (5)] to the raw fluorescence SVD, fluorescence $\text{SVD}_{\text{cor}}$ obtained from phantom experiments with the same photosensitizer concentration should have the same magnitude. Three separate phantoms with different concentrations of scatterers were used and fit with the equation above to produce a corrected SVD magnitude and values of $A = 1.7$ and $B = 0.52$ [see Fig. 2(a)]. Fluorescence measured \textit{in vivo} from mice studies was corrected using Eq. (5), and absolute concentration of HPPH was obtained using the calibration curve between the $\text{SVD}_{\text{cor}}$ and HPPH concentration in micromoles [see Fig. 2(b)]. Due to the heterogeneous distribution of the photosensitizer in the tissue, in our current assumption we use an average HPPH concentration based on the profile measured over the catheter for all mice in the same group; the standard deviation of HPPH concentration includes the uncertainties of this assumption.

![Figure 2](https://www.spiedigitallibrary.org/journals/Journal-of-Biomedical-Optics/Journal-of-Biomedical-Optics-Vol-20-Issue-12_Fig-2.jpg)

\textbf{Fig. 2} (a) Fluorescence singular value decomposition (SVD) amplitude for phantom experiments with different optical properties but the same HPPH concentration. An empirical correction factor (CF) of the form in Eq. (5) was obtained by fitting the fluorescence SVD amplitudes to the same value. CF = 1 corresponds to SVD obtained in a phantom with optical properties of $\mu_a = 0.4$ cm$^{-1}$ and $\mu'_s = 14.4$ cm$^{-1}$. (b) Corrected fluorescence singular value decomposition ($\text{SVD}_{\text{cor}}$) versus HPPH concentration (in $\mu$M).

\section*{2.4 \textit{Ex Vivo} Measurements of the 2-(1-Hexyloxyethyl)-2-Devinyl Pyropheophorbide-a Concentration}

Interstitial fluorescence measurements of the photosensitizer concentration as described above were performed for all tumors before PDT. To evaluate the accuracy of the \textit{in vivo} interstitial fluorescence measurements, \textit{ex vivo} measurements of the HPPH concentration were performed in another set of mice (five mice) and compared with their \textit{in vivo} measurements. Mice with tumors were administered HPPH at the same concentration as PDT-treated mice. After the 24 h drug–light interval, the tumors were excised, protected from light, and stored at $-80^\circ$C. For \textit{ex vivo} analyses, homogenized solutions of the tumors were prepared using Solvable (PerkinElmer, Waltham, Massachusetts). The fluorescence of the homogenized sample was measured by a spectrofluorometer (FluoroMax-3; Jobin Yvon, Inc.) with an
excitation wavelength of 405 nm and an emission range from 630 to 750 nm with an emission maximum at 667 nm. The photosensitizer concentration in the tissue was calculated based on the change in fluorescence resulting from the addition of a known amount of HPPH to each sample after its initial reading. The \textit{in vivo} measurements were correlated to \textit{ex vivo} data using a linear fit to examine their agreement based on the goodness of the fit ($R^2$).

### 2.5 Necrosis Induced by Photodynamic Therapy

After the \textit{in vivo} measurements of the HPPH concentration (see Sec. 2.3), the tumors were treated interstitially using a 1-cm-long CDF coupled to the 665-nm diode laser (B&W Tek, Newark, Delaware 19713); LS ranged from 12 to 150 mW/cm, and the total energy released per unit length ranged from 12 to 100 J/cm. To measure the necrotic radius around the linear source, the tumors were excised from euthanized animals and fixed in formalin 24 h after PDT. Then multiple sections, each \(\sim 200\) to 400 \(\mu\)m apart, were cut perpendicular to the catheter insertion axis and stained with hematoxylin and eosin. Sectioning was performed at the Pathology Core Labs of the Children’s Hospital of Philadelphia. With the assistance of a pathologist, the slides were scanned digitally (ScanScope CS, Aperio Technologies, Inc., Vista, California). Digital slides [see Fig. 1b)] were then read to calculate the area ($A_r$) and radius ($r_r$) of the necrosis around the treatment fiber using the equation $A_r = \pi r_r^2$. The noncircular shape of the necrosis could be caused by inhomogeneities in photosensitizer distribution, oxygen distribution, as well as tissue optical properties; these are assumed to be homogeneous in our current model. For current data processing, an average radius of the necrosis was calculated for the multiple sections collected from each tumor. As the tumors shrank during processing, a shrinkage factor (SF) was also introduced in the calculation of the necrotic radius. SF was determined based on the measurements of the tumor size prior to fixing in formalin and the same measurements after a minimum of 24 h in formalin. The spontaneous necrosis and the necrosis induced by catheter insertion were also subtracted from the final necrosis result, based on data obtained from the control mice with no HPPH injection but catheter insertion and light exposure. Although each treatment condition included one mouse for the control, the PDT-induced necrotic radius for each group of mice was calculated by $SF \times (r_r - r_0)$, where $r_0$ is the mean necrotic radius calculated from all individual controls. This was because of the potential variation due to measurement uncertainties. Table I presents the calculated necrotic radius induced by different treatment conditions and the control necrotic radius for each group of mice after SF correction. The measured SF, tissue optical properties, and interstitial drug concentration have also been summarized for each group of mice; all values have been presented as mean \pm standard deviations.

### 2.6 Diffusion Approximation Solution of the Light Transport

The light transport equation is specified by Eq. (1), which can be solved analytically for a uniformly distributed CDF. The spatial distribution of fluence rate, $\phi$, within the tumor can be expressed

### Table 1: Tissue optical properties and photosensitizer concentrations before HPPH-mediated PDT as well as the treatment conditions. Each group contains four mice bearing RIF tumors: three for the treatment and one mouse as a control. The measured values are presented with their standard deviations.

<table>
<thead>
<tr>
<th>LS$^a$ (mW/cm)</th>
<th>Time$^b$ (s)</th>
<th>HPPH ((\mu)M)</th>
<th>Energy$^c$ ((\mu)J/cm$^2$)</th>
<th>PDT dose$^d$ ((\mu)J/m$^2$)</th>
<th>$\mu_s$ (cm$^{-1}$)</th>
<th>$\mu_t$ (cm$^{-1}$)</th>
<th>Tumor SF$^e$</th>
<th>Necrosis radius$^f$ (mm)</th>
<th>Control radius (mm)</th>
<th>PDT-induced necrosis$^g$ (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>1000</td>
<td>0.38 (\pm) 0.03</td>
<td>12</td>
<td>3.62</td>
<td>0.85 (\pm) 0.03</td>
<td>8.9 (\pm) 0.7</td>
<td>1.24 (\pm) 0.09</td>
<td>2.3 (\pm) 0.6</td>
<td>2.3</td>
<td>0.06 (\pm) 0.5</td>
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<tr>
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<td>0.40 (\pm) 0.03</td>
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<td>9.1 (\pm) 0.5</td>
<td>1.21 (\pm) 0.09</td>
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<td>2.5</td>
<td>0.8 (\pm) 0.6</td>
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<td>30</td>
<td>660</td>
<td>0.6 (\pm) 0.3</td>
<td>20</td>
<td>9.81</td>
<td>0.74 (\pm) 0.08</td>
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<td>0.5 (\pm) 0.4</td>
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<td>4.4 (\pm) 0.5</td>
<td>2.3</td>
<td>2.2 (\pm) 0.5</td>
</tr>
</tbody>
</table>

$^a$Light source strength.
$^b$Light exposure time.
$^c$Total delivered energy per length.
$^d$PDT dose was calculated from the time integration of the HPPH concentration and light fluence rate.
$^e$Tumor shrinkage factor.
$^f$Measured necrotic radius without subtracting the control radius.
$^g$Measured necrotic radius with subtracting the mean control necrotic radius. The mean necrotic radius (the spontaneous necrosis and the necrosis induced by light and/or catheter insertion) was 2.2 \(\pm\) 0.2 mm, obtained from nine controls belonging to the nine groups of the mice.
\[ \phi(r) = \frac{\text{LS}, 3 \mu_s'}{4\pi \sqrt{r^2 + \mu_s'^2}} e^{-\mu_{\text{eff}} \sqrt{r^2 + \mu_s'^2}} \text{d}z , \]

where \( r \) is the distance to the point of interest along the radial axis given the center of the CDF as origin; \( \text{LS} \) is the source power per unit length or linear source strength (mW/cm); and \( l \) is the CDF length. The magnitudes of the tissue optical properties, \( \mu_s \) and \( \mu_s' \), are obtained for each mouse from the measurements in Sec. 2.3. \( \mu_{\text{eff}} \) is calculated from

\[ \mu_{\text{eff}} = \sqrt{3\mu_s \mu_s'} . \]

Figure 3(a) presents the ratio of \( \phi \) inside the tumor and LS versus tumor depth. The ratio of \( \phi \) and mean light fluence rate (\( \phi_{\text{Mean}} \)), which is calculated based on the mean tissue optical properties (\( \mu_s = 0.8 \pm 0.1 \text{ cm}^{-1}, \mu_s' = 9.3 \pm 0.9 \text{ cm}^{-1} \)), has been shown in Fig. 3(b); the values for \( \mu_s \) and \( \mu_s' \) have been presented with their standard deviation. \( \phi_{\text{Mean}} \) is defined as the light fluence rate distribution for the mean tissue optical properties, shown as the dark dashed line in Fig. 3(a).

### 2.7 Fitting Necrotic Radius Using \(^1\text{O}_2\) to Extract Model Parameters

The information of \( \phi \) distribution within the tumor as well as the initial HPPH concentration for each mouse (measured in Sec. 2.3) is passed to Eqs. (2)–(4) in order to calculate the spatiotemporal distribution of the photosensitizer (\( S_i \)) as well as \( ^1\text{O}_2 \) and \( ^3\text{O}_2 \) concentrations.

The magnitude of \( [^3\text{O}_2] \) in tissue is related to partial oxygen pressure (\( P_{o_2} \)) by the coefficient of \( ^3\text{O}_2 \) solubility in tissue (\( \alpha \)) as \( \alpha P_{o_2} \), from which we can calculate \( [^3\text{O}_2]_0 \). It is reported that \( P_{o_2} \) can change from 25.8 to 35.5 mmHg in normal tissue and \( \alpha = 1.3 \mu M/mmHg \). As \( [^3\text{O}_2]_0 \) can change from 33.5 to 46.2 \( \mu M \), we considered an average value of 40 \( \mu M \) in our calculations.

The calculated spatial distribution of \( [^1\text{O}_2]_{\text{rx}} \) is used to fit the necrotic radius and extract the four photosensitizer-specific reaction-rate parameters: specific oxygen consumption rate (\( \xi \)), ratio of photobleaching to reaction between \( ^1\text{O}_2 \) and cellular targets (\( \sigma \)), ratio of triplet state (\( T \)) phosphorescence to reaction between \( T \) and \( ^1\text{O}_2 \) (\( \beta \)), oxygen supply rate to tissue (\( q \)), as well as reacted singlet oxygen threshold concentration (\( [^1\text{O}_2]_{\text{rx,sh}} \)). In the fitting routine, the nonlinear solver starts from initial points selected based on the previous published data for the other photosensitizers (Photofrin, ALA – PiranoidX, and mTHPC), reaching different locally optimal solutions. \( \xi, \sigma, g, \) and \( [^1\text{O}_2]_{\text{rx,sh}} \) are assigned randomly within the ranges of \( 10 \) to \( 100 \) \( \times 10^{-5} \text{ cm}^2 \text{ mW}^{-1} \text{ s}^{-1} \), \( 1 \) to \( 10 \) \( \times 10^{-5} \mu M^{-1} \), 0.7 to 1.5 \( \mu M/s \), and 0.5 to 1.0 \( \mu M \), respectively. The current algorithm will encounter convergence issues when given too many free-floating parameters. As the calculated \( [^3\text{O}_2]_0 \) is less sensitive to \( \beta \) and \( \delta \) quantities compared with the other model parameters, these parameters are fixed at \( \beta = 11.9 \mu M \) and \( \delta = 33 \mu M \) throughout the subsequent fitting procedure; these values with unknown variance are obtained from the literature.

Our fitting routine varies \( \xi, \sigma, g, \) and \( [^1\text{O}_2]_{\text{rx,sh}} \) so that \( [^1\text{O}_2]_{\text{rx}} \) at the necrotic radius for each mouse remains close to the \( [^1\text{O}_2]_{\text{rx,sh}} \) by minimizing the following error function:

\[ f = \sqrt{\frac{\sum_{i=1}^{N} (^[1\text{O}_2]_{\text{rx}}(r_i) - [^1\text{O}_2]_{\text{rx,sh}})^2}{N(N - 1)}} . \]

where \( [^1\text{O}_2]_{\text{rx}}(r_i) \) is the computed reacted singlet oxygen at a necrotic radius for \( i \) th mouse and \( N \) represents the number of mice.

Our intention was to find the parameters that produce a global minimum for Eq. (9), rather than to restrict the fitting parameters to within the certain predefined range. About 400 different combinations of the initial parameters have been used in our fitting routine to propose the best globally optimal solution. The fitting outcome for each set of initial parameters is a single value for \( \xi, \sigma, g, \beta, \) and \( [^1\text{O}_2]_{\text{rx,sh}} \), applicable to the entire set of animal measurements; Table 2 presents the best obtained fitting parameters with their standard deviations. While each animal’s specific optical properties and sensitizer concentration are used in the calculation, these fundamental parameters were kept the same across animals.
Table 2 The magnitude of the photochemical parameters for HPPH.

<table>
<thead>
<tr>
<th>Symbols</th>
<th>Initial values&lt;sup&gt;a&lt;/sup&gt;</th>
<th>Calculated values&lt;sup&gt;b&lt;/sup&gt;</th>
</tr>
</thead>
<tbody>
<tr>
<td>ε&lt;sup&gt;1&lt;/sup&gt; (cm&lt;sup&gt;-1&lt;/sup&gt; μM&lt;sup&gt;-1&lt;/sup&gt;)</td>
<td>0.108</td>
<td>—</td>
</tr>
<tr>
<td>δ (μM)</td>
<td>33</td>
<td>—</td>
</tr>
<tr>
<td>β (μM&lt;sup&gt;-1&lt;/sup&gt;)</td>
<td>11.9 (Refs. 7&lt;sup&gt;21,22&lt;/sup&gt;)</td>
<td>—</td>
</tr>
<tr>
<td>σ (μM&lt;sup&gt;-1&lt;/sup&gt;)</td>
<td>(1 to 10) × 10&lt;sup&gt;-5&lt;/sup&gt; (1 ± 6) × 10&lt;sup&gt;-5&lt;/sup&gt;</td>
<td>—</td>
</tr>
<tr>
<td>ξ (cm&lt;sup&gt;2&lt;/sup&gt; mW&lt;sup&gt;-1&lt;/sup&gt;)</td>
<td>(10 to 100) × 10&lt;sup&gt;-3&lt;/sup&gt; (70 ± 40) × 10&lt;sup&gt;-3&lt;/sup&gt;</td>
<td>—</td>
</tr>
<tr>
<td>g (μM&lt;sup&gt;-1&lt;/sup&gt;)</td>
<td>0.7 to 1.5</td>
<td>1.5 ± 0.9</td>
</tr>
<tr>
<td>[1O₂]&lt;sub&gt;1.0 mm&lt;/sub&gt; (mM)</td>
<td>0.5 to 1.0</td>
<td>0.6 ± 0.1</td>
</tr>
</tbody>
</table>

<sup>a</sup>The initial guess of the parameters, assigned randomly within the presented ranges.

<sup>b</sup>The obtained values by the macroscopic model with their overall error. Notice that the value of σ is significantly larger than that presented in Ref. 11. This is proportional to a change of ε from 0.047, used in Ref. 11, to 0.108 based on experimental verification of the original literature value being based on log<sub>10</sub> rather than log<sub>2</sub>, as used in the current study. Each value is expressed as mean±standard deviation.

All fitting and simulations have been performed using MATLAB R2013a (64-bit, Massachusetts), which was run on an iMAC OSX version 10.9.5 (processor 3.1 GHz Intel Core 17 and memory 16 GB 1600 MHz DDR3). The calculation time was in seconds for the rate equation and in minutes for the time and spatially coupled differential equations.

### 2.8 Statistical Analyses

Each measurement was independently carried out three times. The magnitude of each measurement is expressed as mean±overall standard deviation. Mann–Whitney tests were used to evaluate whether there was a significant difference between the values obtained in vivo and ex vivo for HPPH concentrations. Analyses were carried out using the SPSS 14.0 software; statistical significance was defined at p < 0.05 level (95% confidence level).

### 3 Results

The distribution of φ in tumor tissue was calculated using the light source characteristics and the measured tissue optical properties (μ<sub>μ</sub> and μ<sub>ε</sub> in Table 1). Based on the results of the calculations, φ/LS drops substantially versus tumor depth as shown in Fig. 3(a). The maximum fluence rate (φ/φ<sub>Mean</sub>) drop was 36% that occurred in 5-mm tissue depth with μ<sub>μ</sub> = 0.95 (1/cm) and μ<sub>ε</sub> = 10.5 (1/cm) [see Fig. 3(b)].

HPPH concentration in tumor was acquired interstitially (see Sec. 2.3). However, accurate ex vivo assessments (see Sec. 2.4) would greatly broaden the applicability of the interstitial in vivo measurements. As shown in Fig. 4, the interstitially measured concentrations have been compared with those obtained ex vivo to evaluate the in vivo measurements; each individual data point represents the average value of three measurements with the standard error of the mean. The best linear fit that could be obtained was y = 1.1x with R² = 0.98 (blue solid line). If one considers a slope of 1 as perfect agreement of the two methods, our comparison shows that the agreement between the in vivo and the ex vivo results is less than 10%. Mann–Whitney tests were additionally used to evaluate whether there is a statistically significant difference between the values obtained in vivo and ex vivo; p-value was calculated to be 0.31, which shows no statistically significant difference.

The amounts of [1O₂]<sub>sh</sub> were calculated using the macroscopic model including the information of the spatial distribution of φ in tumor as well as the tissue optical properties and photosensitizer concentration in tumor (see Table 1). Each group of mice has one measurement of the spontaneous necrosis or that due to needle insertion without PDT. The PDT-induced necrotic radius for each group of mice was calculated by SF × (r<sub>n</sub> − r<sub>t</sub>), where r<sub>n</sub> is the total radius of necrosis. The mean radius of the spontaneous necrosis and the necrosis induced by the catheter insertion, r<sub>t</sub>, has been calculated to be 2.2 ± 0.2 mm after tumor shrinkage correction. The correlation between the amounts of the calculated [1O₂]<sub>sh</sub> at the location of the necrotic radius and the measured necrotic radius induced by PDT has been shown in Fig. 5(a). The spontaneous necrosis, the necrosis induced by the catheter insertion and light, was subtracted from the necrotic radius. The magnitude of LS (mW/cm), total energy released per unit length (J/cm), and the initial HPPH concentration for each group are shown in the legend; the radii are presented with error bars of the measurements. Table 2 presents the initial photochemical parameters and those obtained from the fitting routines. The best fit to the data estimated ξ = (70 ± 40) × 10<sup>-3</sup> cm<sup>2</sup> mW<sup>-1</sup> s<sup>-1</sup>, σ = (1 ± 6) × 10<sup>-3</sup> μM<sup>-1</sup>, g = 1.5 ± 0.9 μM/s, and [1O₂]<sub>sh</sub> = 0.6 ± 0.1 mM; these values are presented with their standard deviation. The fitting parameters did not change very much using several subgroups of mice (data not included) and the variances of the extracted parameters are included in the uncertainties of each parameter. The gray region shown in Fig. 5(a) presents a range for the calculated [1O₂]<sub>sh</sub> (0.55 < [1O₂]<sub>sh</sub> < 0.65 mM). The parameters β and δ have been fixed at 11.9 and 33 μM, respectively. However, we have found that δ has a huge impact on the value of σ obtained.
from the fitting. Based on our fitting algorithm and experimental uncertainties, the error for the parameters $\xi$ and $\sigma$ was quite large. The uncertainty is large enough to include the results obtained from our previous preliminary fitting11 as possible values; please note that the extinction coefficient for HPPH should be 2.3 times higher than what was used in the Ref. 11. As shown in Fig. 5(b), the accuracy of our fitting outcomes has been evaluated by the correlation of the PDT-induced necrotic radius calculated by the macroscopic model and the one calculated from the PDT-induced necrotic area. The necrotic radius was calculated using $[O_2]_{rx} = \cdot O_{2}^{-} 0.6 \text{ mM}$, the dashed line in Fig. 5(a) and the $[O_2]_{rx}$ profile, where they intersect. The data could be best fit with a linear model ($y = 0.99x$) with a goodness of $R^2 = 0.81$.

PDT dose was calculated over the entire PDT interval for each group of mice, using the time integral of the product of light fluence rate obtained from Eq. (6) and local HPPH concentration at 3 mm since the sensitizer concentration and optical properties were measured 3 mm from the CDF. The magnitude of the necrotic radius that occurred due to PDT has been correlated to the total PDT dose ($\mu$J/cm$^2$) in Fig. 6(a). The solid blue line ($y = 0.06x$) shows the best fit to the data using a linear function with the goodness of $R^2 = 0.55$, and the dashed line ($y = 0.0014x^2 + 0.031x$) shows an independent best fit using

![Fig. 5](https://www.spiedigitallibrary.org/journals/Journal-of-Biomedical-Optics) (a) The amounts of the singlet oxygen concentration ($[O_2]_{rx}$) calculated by the macroscopic model versus PDT-induced necrotic radius. The necrotic radius has been calculated for nine groups of mice with tissue optical properties, drug concentration, and treatment condition presented in Table 1. The gray area indicates the possible range of oxygen threshold concentration ($[O_2]_{rx}; \text{sh}$), which is 0.6 ± 0.1 mM; and the dashed line indicates $[O_2]_{rx} = 0.6 \text{ mM}$. (b) Necrotic radius calculated by macroscopic model versus the one calculated from the PDT-induced necrotic area. The error bars show the overall standard deviation of the measurements and the solid line shows the best linear fit to the data with a slope of 1 and a goodness of fit of $R^2 = 0.81$ (see Table 2 for the magnitude of the photochemical parameters and $[O_2]_{rx}$).

![Fig. 6](https://www.spiedigitallibrary.org/journals/Journal-of-Biomedical-Optics) Necrotic radius induced by PDT versus (a) total PDT dose and (b) calculated singlet oxygen concentration ($[O_2]_{rx}$) at 3-mm tumor depth. The data are presented for nine groups of mice with properties and treatment conditions presented in Table 1. The solid lines show the best fit to the data using functional forms, $y = 0.06x$ for (a) and $y = 30.32x^2 - 6.96x + 1.88$ for (b) with goodness of fit of $R^2 = 0.94$ and 0.95 for (a) and (b), respectively. The dashed lines show an independent fit using polynomial curves. The gray area shows the upper and lower bounds of the fit with 95% confidence level.
a polynomial function with the goodness of $R^2 = 0.64$. All the treatments induced necrosis in the tumors except for the treatment condition with an energy per unit length of 12 J/cm (with LS = 12 mW/cm and exposure times of 1000 s). This condition induced necrosis comparable with the control mice. Among all treatment conditions, the case with a total energy released per unit length of 100 J/cm (LS = 150 mW/cm and exposure time of 666 s) has the biggest necrotic radius in the treated tumor.

In order to provide a straightforward comparison of PDT dose to $[^{1}O_2]_{rx}$, the magnitude of the generated $[^{1}O_2]_{rx}$ at 3-mm tumor depth was calculated for the different treatment conditions. Figure 6(b) shows a correlation between the necrotic radius induced by PDT and $[^{1}O_2]_{rx}$ at 3 mm. The solid blue line shows the best fit using the functional form $y = 13.45/1 + e^{(y−1.1)/0.172}$ to the data with goodness of $R^2 = 0.95$, and the dashed line shows an independent polynomial fit, $y = 30.32x^3 − 6.96x^2 + 1.88x$ with goodness of $R^2 = 0.94$.

4 Discussions

PDT offers great promise as a targeted cancer treatment. Studies on this technique have observed dramatic tumor destruction with little damage to the surrounding normal tissue. However, many attempts to use PDT in the clinic have been hindered due to the complex dosimetry problem or have led to inadequate tumor response.

The common approach in clinical PDT dosimetry is PDT dose, which is based on the amount of photosensitizer administered to the patient and the amount of light delivered to the treatment site. However, PDT dose has several problems: (1) The local concentration of photosensitizer varies from site to site in the tissue and from individual to individual. (2) The penetration of light into the target depends on the optical properties of that tissue. (3) Tissue and blood oxygenation is a central component for PDT and also affects the tissue optical properties. (4) If the tissue is hypoxic, or becomes hypoxic as a result of the PDT treatment, the yield of $^{1}O_2$ will be lower than expected. To complicate matters further, all these parameters can change during treatment and each of the parameters can also influence the others.

Modeling of the generated $[^{1}O_2]_{rx}$ is of particular interest for the PDT dosimetry because it is the major cytotoxic agent causing biological effects in type II PDT and can predict the treatment efficacy in the clinic. A series of preclinical explicit dosimetry experiments including a range of LS and different light exposures was performed on mice bearing RIF tumor to generate different amounts of $[^{1}O_2]_{rx}$ and induce different radii of necrosis. Then the amounts of $[^{1}O_2]_{rx}$ were determined using the macroscopic model incorporating the information of the distribution of $\phi$, and photosensitizer in tumor, as well as the tissue optical properties ($\mu_s$ and $\mu'_s$). The $\phi$ distribution was determined by the light source characteristics and the tissue optical properties. The photosensitizer concentration was measured interstitially pre-PDT for each mouse. Ex vivo measurements of the HPPH concentration were used as a validation for the in vivo measurements.

The computed $[^{1}O_2]_{rx}$ was fitted to the in vivo HPPH-mediated necrotic radius in the RIF tumor model (nine groups, each includes three mice) so that $[^{1}O_2]_{rx,sh}$ and the photocatalytic PDT parameters, $\xi$, $\sigma$, and $g$, could be determined. A comparison of the HPPH photochemical parameters ($\xi = 70 \times 10^{-8}$ cm$^2$ mW$^{-1}$ s$^{-1}$, $\sigma = 1 \times 10^{-5}$ $\mu$M$^{-1}$, and $g = 1.5$ $\mu$M/s) with those obtained for photosensitizers Photofrin [$\xi = (2,10 \times 3.7) \times 10^{-8}$ cm$^2$ mW$^{-1}$ s$^{-1}$ and $\sigma = 7.6 \times 10^{-5}$ $\mu$M$^{-1}$], $m$THPC ($\xi = 30.0 \times 10^{-8}$ cm$^2$ mW$^{-1}$ s$^{-1}$, $\sigma = 3.0 \times 10^{-5}$ $\mu$M$^{-1}$) and ALA-PpIX ($\xi = 3.7 \times 10^{-8}$ cm$^2$ mW$^{-1}$ s$^{-1}$, $\sigma = 9.0 \times 10^{-5}$ $\mu$M$^{-1}$) shows a bigger $\xi$ for HPPH as compared with the other photosensitizers, which makes sense, since $\xi$ is proportional to the absorption coefficient of the sensitizer and HPPH has a higher absorption. The $\sigma$ value was estimated to be smaller for HPPH as compared with the other photosensitizers.

$[^{1}O_2]_{rx}$ and PDT dose at 3 mm were used in Fig. 6, since the average radius of necrosis is roughly 3 mm. The dashed lines in Fig. 6 are the polynomial fit of the data. To make it easier to calculate the fit, functional forms of $y = 0.06x$ and $y = 13.45/1 + e^{(y−1.1)/0.172}$ (solid lines in Fig. 6), respectively, were chosen to approximate the polynomial fits. They agreed with the best fit from the polynomial curves reasonably well. The correlations and goodness of fits ($R^2 = 0.95$ for $[^{1}O_2]_{rx}$ versus $R^2 = 0.55$ for PDT dose) demonstrate that $[^{1}O_2]_{rx}$ serves as a better dosimetric quantity than PDT dose for predicting the treatment outcome. This is because $[^{1}O_2]_{rx}$ recognizes $^{1}O_2$ consumption during PDT and accounts for its variations, which are not considered in PDT dose; the general oxygen supply term $\phi$ accounts for the microscopic $^{1}O_2$ diffusion and convection mechanism [see Eq. (3)].

5 Conclusion

PDT efficacy depends on $[^{1}O_2]_{rx}$, which in turn can be determined by $\phi$, photosensitizer concentration, and tissue optical properties. As the direct measurement of $^{1}O_2$ concentration is very difficult in vivo with large variability, theoretical analyses provide a useful complementary approach for calculating the $[^{1}O_2]_{rx}$ generated by PDT. Although results obtained from mathematical modeling will always be vulnerable to assumptions regarding the complex physiology of tumors and generated $[^{1}O_2]_{rx}$, simulations that are well informed by experiments provide insights into phenomena that are not accessible via direct experimentation. As a result, an empirical four-parameter macroscopic model has been developed to calculate the apparent $^{1}O_2$ concentration. This model utilizes the complete set of PDT kinetic equations as well as the dosimetry calculation based on the in vivo measurements of the tissue optical properties, $\phi$, and photosensitizer concentration.

In this study, we used the macroscopic model to fit in vivo HPPH-mediated necrotic radius in the RIF tumor model so that photochemical PDT parameters can be obtained. Then the in vivo threshold dose of the singlet oxygen, $[^{1}O_2]_{rx,sh}$, was determined by correlation of the calculated $[^{1}O_2]_{rx}$ and the tumor necrosis induced by PDT. The PDT dose and $[^{1}O_2]_{rx}$ were calculated at 3 mm because this is roughly the average necrotic radius. The correlations of the PDT dose and $[^{1}O_2]_{rx}$ with PDT-induced necrotic radius showed that $[^{1}O_2]_{rx}$ serves as a better dosimetric quantity than PDT dose for predicting the treatment outcome. We expect that the model parameters and $[^{1}O_2]_{rx,sh}$ obtained from this study can be used directly in clinical trials to potentially better predict the outcome of the HPPH-mediated PDT. This in vivo PDT dosimetry is imperative in understanding the mechanism of the $^{1}O_2$ toxic effect and how this toxicity translates to tissue necrosis observed with the treatment.
In the current model, $\delta$ is set to be 33 $\mu$M. The impact of $\delta$ values on the values of $\sigma$ obtained from fitting needs to be further studied. Due to a lack of published independent validation, the value of $\sigma$ should be taken as preliminary.

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References


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